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Cite as: J. Appl. Phys. **129**, 203103 (2021); <https://doi.org/10.1063/5.0050458>

Submitted: 15 March 2021 . Accepted: 09 May 2021 . Published Online: 25 May 2021

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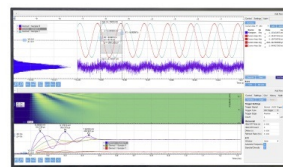
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# Polarization tuning of an $H1$ organic-inorganic nano-cavity

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Submitted: 15 March 2021 · Accepted: 9 May 2021 ·

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## ABSTRACT

We investigate the optical properties of the dipole-like modes of an  $H1$  nano-cavity consisting of a single missing airhole imbedded into a triangular two-dimensional silicon nitride ( $\text{Si}_3\text{N}_4$ ) based photonic crystal coated with a red-fluorescent molecular dye. We modify the size and position of the first six neighboring airholes around the nano-cavity and demonstrate that this allows control over the energy and separation of two dipole-like optical modes ( $M_x$  and  $M_y$ ). This allows us to produce either linearly polarized optical modes or an unpolarized optical mode composed of degenerate modes having orthogonal polarization. We confirm our findings using three-dimensional finite difference time domain calculations.

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## I. INTRODUCTION

A photonic crystal nano-cavity is a structure in which a physical defect is deliberately introduced in an otherwise perfect photonic crystal.<sup>1–3</sup> In such a structure, light of certain frequencies can become trapped in the defect, with the volume of the cavity being around  $(\lambda/n)^3$ .<sup>4–7</sup> Such properties make photonic crystal nano-cavities very attractive systems to study light–matter interactions at the nanoscale in both weak<sup>8,9</sup> and strong coupling regimes.<sup>10,11</sup> Photonic crystal nano-cavities have been explored for applications as single-photon sources,<sup>12,13</sup> sensor devices,<sup>14</sup> and quantum cryptography systems.<sup>15,16</sup> Here, applications require close control over the polarization state of the cavity mode; for example, in quantum cryptography, an unpolarized optical cavity mode is desirable,<sup>17</sup> while single-photon light sources generally require a linearly polarized optical mode.<sup>18</sup>

Families of different 2D photonic crystal nano-cavities have been explored in which a physical defect is created from a linear array of missing holes in a triangular lattice, with cavities created from three, five, and seven missing holes referred to as L3, L5, and

L7 cavities.<sup>19–21</sup> Here, larger cavities generally have a higher quality-factor ( $Q$ -factor) with this parameter being important in applications such as low-threshold lasers.<sup>22,23</sup> However, the optical mode volume ( $V$ ) of a cavity is also of importance as the  $Q/V$  ratio defines the Purcell factor (enhancement of spontaneous emission rate) that occurs when placing an emitter into the cavity, with large spontaneous emission rates being of importance in single-photon light sources.<sup>24,25</sup> To combine both large  $Q$  and small  $V$ , researchers have explored the so-called  $H1$  nano-cavities that are created by defining a single missing airhole defect into a two-dimensional triangular lattice photonic crystal slab.<sup>26–28</sup> Here, a number of different types of  $H1$  structures have been created using materials of different refractive indices. For example, cavities have been realized based on materials having a high refractive index ( $n = 3.46$ ) with a maximum (measured)  $Q$ -factor determined to be around  $10^6$  based on a structure having a slab thickness  $d = 0.575a$ .<sup>27</sup> By using a dielectric material of lower refractive index ( $n = 1.93$ ), it has been predicted<sup>29</sup> that the  $Q$ -factor is expected to be reduced to around 700 based on a slab thickness of  $1.55a$ . The  $Q$ -factor can, however, be

enhanced by modifying the size and position of the first six nearest-neighbor airholes that surround the nano-cavity defect.<sup>28,30</sup>

In this work, we present a modeling and experimental study of the polarization state of an *H1* nano-cavity that is coated with a red-emitting molecular dye [see Fig. 1(a)]. It is known that an *H1* nano-cavity will support a degenerate dipole-like optical mode that in fact corresponds to two modes having the same frequency but with different polarizations.<sup>28,31,32</sup> Here, we demonstrate that the *Q*-factor of an *H1* nano-cavity can be enhanced and the polarization state of the cavity mode controlled<sup>4,28,30</sup> by reducing the symmetry of the surrounding holes in the photonic crystal. This reduction in symmetry is realized via modifying the size and position of the first six neighboring airholes that surround the nano-cavity “missing hole.” We then demonstrate that the degeneracy of the cavity mode can be removed by reducing the structure symmetry, allowing us to tune the polarization of the cavity mode from being *x*-polarized to *y*-polarized or into an unpolarized state. Our cavities are constructed using the dielectric material silicon nitride ( $\text{Si}_3\text{N}_4$ ), which is coated with a thin film of the molecular dye Lumogen Red, allowing the dipole-like mode to be positioned at optical frequencies (650–670 nm). We show that our modified cavities can reach a *Q*-factor of 1875, a value that is almost one order of magnitude compared to an unmodified *H1* cavity.

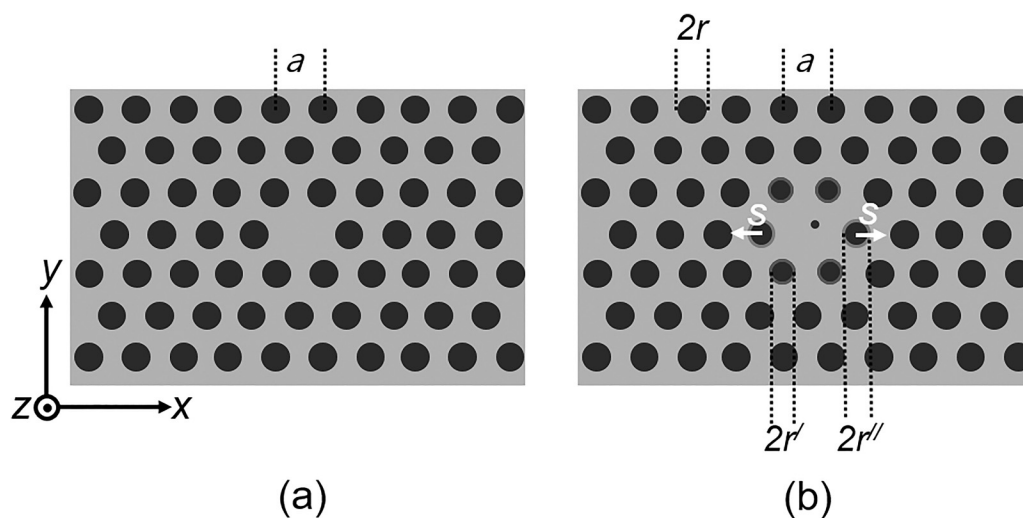
## II. MODELING

The structure of the nano-cavities investigated in this work is shown in Fig. 1. This structure is based on a single missing airhole cavity in a triangular two-dimensional  $\text{Si}_3\text{N}_4$  photonic crystal membrane having a refractive index  $n = 2.1$ , thickness  $d = 200$  nm, lattice constant  $a = 260$  nm, and a hole radius  $r = 0.3a$ . Here, the

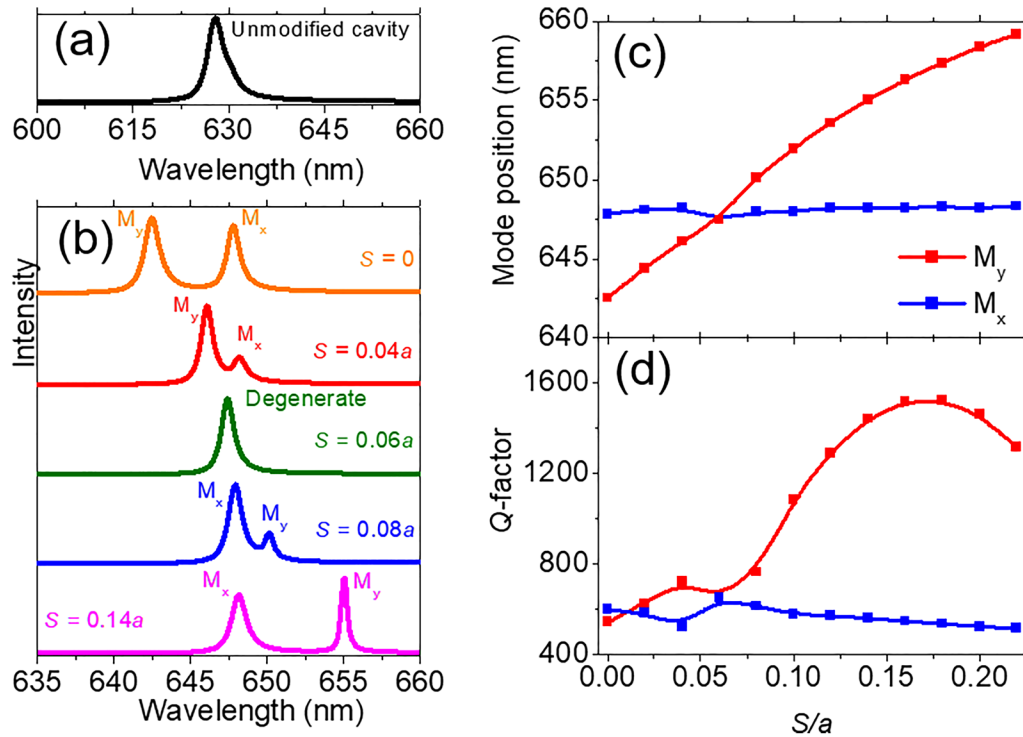
value of  $r$  was chosen based on the results from previous reported studies as it allows a TE bandgap to be created in such photonic crystal devices.<sup>26,33–35</sup> To improve the cavity quality-factor and control its polarization state, we have reduced the size of the first two airholes above and below the cavity (parallel to the *x* axis) to  $r' = 0.23a$ . The size of the airholes neighboring the cavity was also reduced to  $r'' = 0.26a$  and they were displaced by a distance  $s$  away from their original position. We chose the values of  $r'$  and  $r''$  based on the fabrication capability and resolution of our electron beam lithography (EBL) system, with  $r - r' = 10$  nm and  $r'' - r' = 8$  nm. As we show below, this lowering of cavity symmetry created by reducing the size of the first two airholes above and below the nano-cavity breaks the degeneracy of the cavity mode and splits it into two linearly polarized modes,  $M_x$  and  $M_y$ .

We have used three-dimensional finite difference time domain (FDTD) calculations to investigate the optical properties of our nano-cavities.<sup>36</sup> Here, the photonic crystal size was set to be  $34a \times 19\sqrt{3}a$  with boundary conditions implemented by introducing a perfect matching layer around the structure. The *Q*-factor was calculated by imbedding an oscillating dipole emitter of a dipole moment  $P(x, y, z) = (1, 1, 0)$  at a weak symmetry point that was 10 nm away from the cavity center. Here, the dipole source was modeled as a Gaussian oscillating pulse centered at 628 nm with a linewidth of 100 nm. The Poynting vector leaving the cavity was then calculated with emission from a single dipole emitter being sufficient to study the dependence of the *Q*-factor and mode shift on the displacement ( $s$ ) of the side airholes. Here, the cavity *Q*-factor of the structures was calculated by relating the cavity emission linewidth at half maximum  $\Delta\lambda$  to the wavelength of the cavity mode  $\lambda$  via  $Q = \Delta\lambda/\lambda$ .

In Fig. 2(a), we plot the FDTD simulated emission spectrum for an unmodified *H1* nano-cavity (i.e.,  $r = 0.3a$ ,  $s = 0$ ). Our



**FIG. 1.** (a) A schematic diagram of a single missing airhole nano-cavity. (b) A schematic diagram of the location and layout of the holes that surround the nano-cavity explored in this work. The blue dot in (b) represents the location of the dipole emitter used in the FDTD simulations, which is displaced 10 nm from the cavity center in both *x* and *y* directions.



**FIG. 2.** (a) FDTD simulated emission spectrum of an unmodified  $H1$  nano-cavity. (b) The FDTD simulated emission spectra of a modified  $H1$  nano-cavity as a function of displacement ( $s$ ) of the side airholes in a direction corresponding to the  $x$  axis. (c) The position of mode  $M_x$  and  $M_y$  as a function of  $s$ . (d) The  $Q$ -factor of modes  $M_x$  and  $M_y$  as a function of the side airholes displacement  $s$ . In all these calculations,  $a = 260$  nm,  $d = 200$  nm,  $r = 0.3a$ ,  $r' = 0.23a$ ,  $r'' = 0.26a$  and  $n = 2.1$ .

calculations also indicate that this mode is a dipole-like cavity mode composed of two degenerate modes having orthogonal polarization. We find as expected that by reducing the symmetry of the  $H1$  nano-cavity (realized by either modifying the size of the airholes that surround the cavity or by displacing the side airholes), we create a splitting of the cavity mode into two modes having orthogonal polarizations. This is shown in Fig. 2(b), where we plot a series of simulated emission spectra for an  $H1$  nano-cavity having airhole size  $r = 0.3a$ ,  $r' = 0.23a$ ,  $r'' = 0.26a$  and different side-hole shifts  $s$ , where holes have been displaced in a direction parallel to the  $x$  axis. Here, the cavity symmetry is broken through changed hole size (i.e.,  $r \neq r' \neq r''$ ) and we find that the cavity supports two optical modes labeled  $M_x$  and  $M_y$ , that are defined by their polarization direction. Figures 2(c) and 2(d) plot the calculated wavelength and  $Q$ -factor of modes  $M_x$  and  $M_y$ , respectively, as a function of side-hole shift.

Our calculations [see Fig. 2(b)] indicate that mode  $M_x$  is sensitive to modification of the size of the surrounding airholes and causes it to undergo a redshift from 628 to 648 nm as airhole size is reduced from 78 to 59.8 nm for the first two airholes above and below the cavity ( $r'$ ) and from 78 to 67.6 nm for airholes neighboring the cavity ( $r''$ ). This redshift is accompanied by an increase in the cavity  $Q$ -factor from 200 to 650. Interestingly, however, we find [see Figs. 2(c) and 2(d)] that the  $Q$ -factor and wavelength of mode  $M_x$  are not apparently dependent on the airhole side-shift  $s$ . In

contrast, the  $Q$ -factor and wavelength position of mode  $M_y$  has a strong dependence on  $s$ . Indeed, it can be seen that mode  $M_y$  undergoes a 17 nm shift to longer wavelengths as  $s$  is increased from  $s = 0$ – $0.22a$ , a result that we ascribe to an increase in the physical volume of the nano-cavity.

As can be seen in Fig. 2(b), our model indicates that mode  $M_y$  undergoes a spectral overlap with mode  $M_x$  at  $s = 0.06a$  forming a degenerate state. It is apparent that the total integrated area under the peaks of both  $M_x$  and  $M_y$  is almost constant; however, when such modes are close in energy, we see a transfer of area between them. If we simplistically equate the total area of the emission peaks with the amount of energy stored within the cavity, it suggests an effective transfer of electromagnetic energy stored in each mode as they approach degeneracy.<sup>37</sup> Figure 2(d) also reveals that the  $Q$ -factor of mode  $M_y$  has a strong dependence on shifting the side holes in the  $x$  direction, with a maximum value of 1500 predicted for  $s = 0.18a$ , a value almost eight times higher than the  $Q$ -factor of the unmodified cavity. We attribute this increase in  $Q$ -factor to a reduction of radiation losses from guided modes due to the gentle confinement of the field that occurs as a result of the modifications to the cavity structure.<sup>4</sup>

In order to gain further insight into the optical modes identified in Fig. 2, we have calculated the electromagnetic field distribution associated with mode  $M_y$  and  $M_x$ , respectively. The results of these calculations are plotted in Fig. 3 for  $s = 0.14a$ .

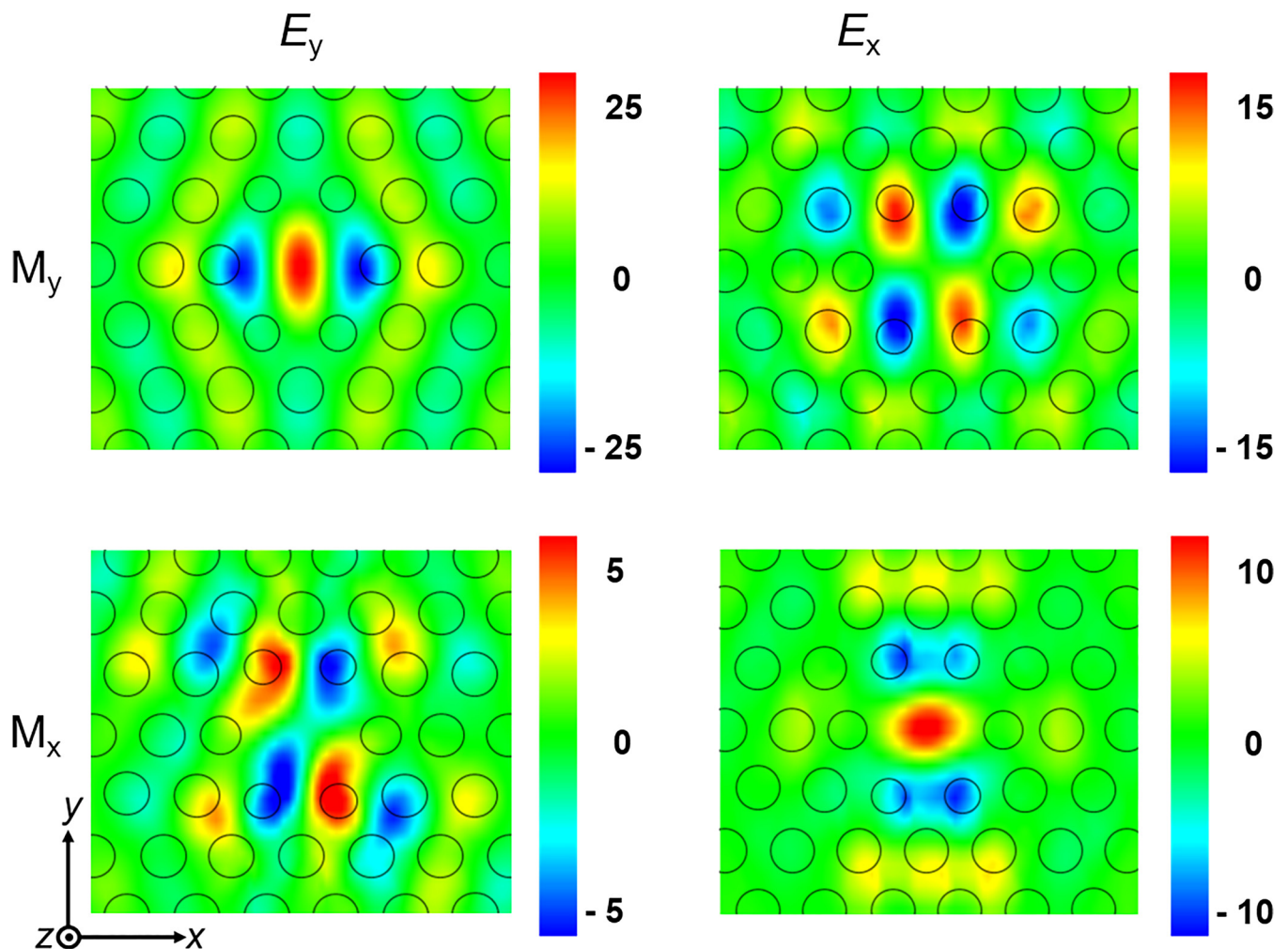


FIG. 3. Electric field distributions at the cavity center at wavelengths corresponding to modes  $M_y$  and  $M_x$  at  $s = 0.14a$ .

Here, it is apparent that both modes  $M_x$  and  $M_y$  have a dipole-like field distribution.<sup>26,38</sup> We can use this calculated field distribution to explain the finding [see Figs. 2(c) and 2(d)] that mode  $M_y$  appears most sensitive to changes in displacements of the side holes in the  $x$  direction position, with such changes not apparently affecting mode  $M_x$ . It is clear that this sensitivity results from the fact that the  $E_y$  component of the  $M_y$  mode electric field distribution is oriented parallel to the  $x$  direction (see Fig. 3). In contrast, it is apparent that the  $E_x$  component of the  $M_x$  field distribution will be most sensitive to modifications of the upper and lower airholes (i.e., resulting from structure changes in the  $y$  direction).

### III. EXPERIMENTAL RESULTS AND DISCUSSION

To explore the results of our FDTD calculations, we fabricated a series of  $H1$  nano-cavities having a lattice constant

$a = 260$  nm, airhole radius  $r = 75$ ,  $r' = 60$ , and  $r'' = 68$  nm into a pre-etched free-standing  $\text{Si}_3\text{N}_4$  membrane of thickness 200 nm, and refractive index  $n = 2.1$ . Cavities were created using electron beam lithography and reactive ion etching techniques. Here, cavities were fabricated into free-standing  $\text{Si}_3\text{N}_4$  membranes purchased from Silson Ltd. The reader is directed to our previous papers that fully describe the lithography and patterning methods used.<sup>39,40</sup> Here, we used such techniques to fabricate a series of different photonic crystal nano-cavities into  $\text{Si}_3\text{N}_4$  membranes, including regular L3, modified L3, and a 1D photonic crystal nano-cavity.<sup>39–41</sup>

Figures 4(a) and 4(b) show scanning electron microscope images recorded at two different magnifications of the nano-cavities fabricated. Following fabrication, a 3 nm thick layer of the molecular dye Lumogen Red was coated onto the cavity surface via thermal evaporation. Here, our previous work has confirmed that characterizing the fluorescence generated by such an organic

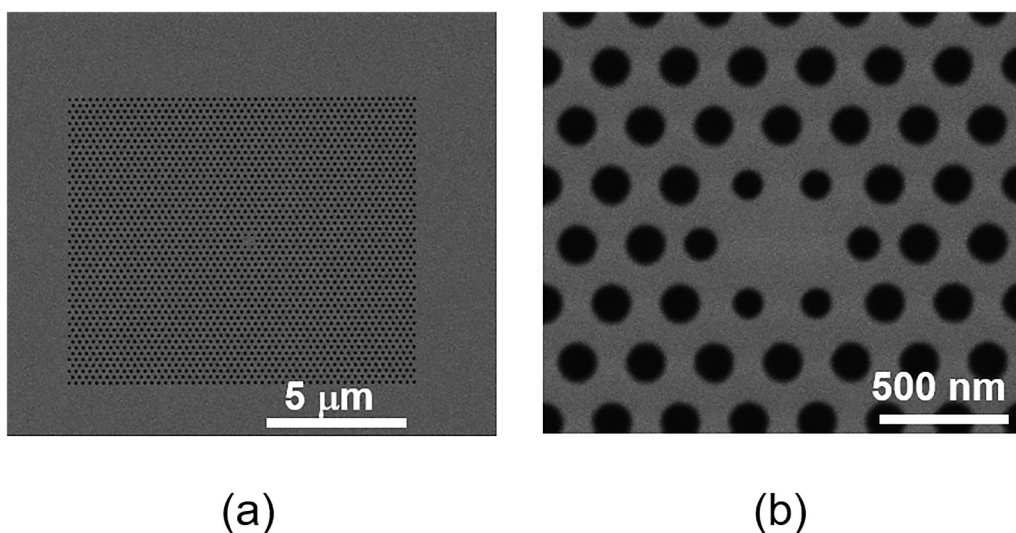


FIG. 4. Parts (a) and (b) show SEM images of a  $\text{Si}_3\text{N}_4$ -based  $H1$  photonic crystal nano-cavity recorded at two different magnifications.

surface layer is an effective method to probe the optical structure of a photonic crystal nano-cavity.<sup>39</sup>

Such structures were studied by generating photoluminescence (PL) using the 442 nm line of a HeCd laser. Here, the laser

was focused onto the sample to a  $2500\ \mu\text{m}^2$  spot having an excitation power density of  $15\ \text{W cm}^{-2}$ , with the laser incident on the surface at an angle of  $45^\circ$  relative to the surface normal (the so-called “dark field” configuration). The resultant PL was

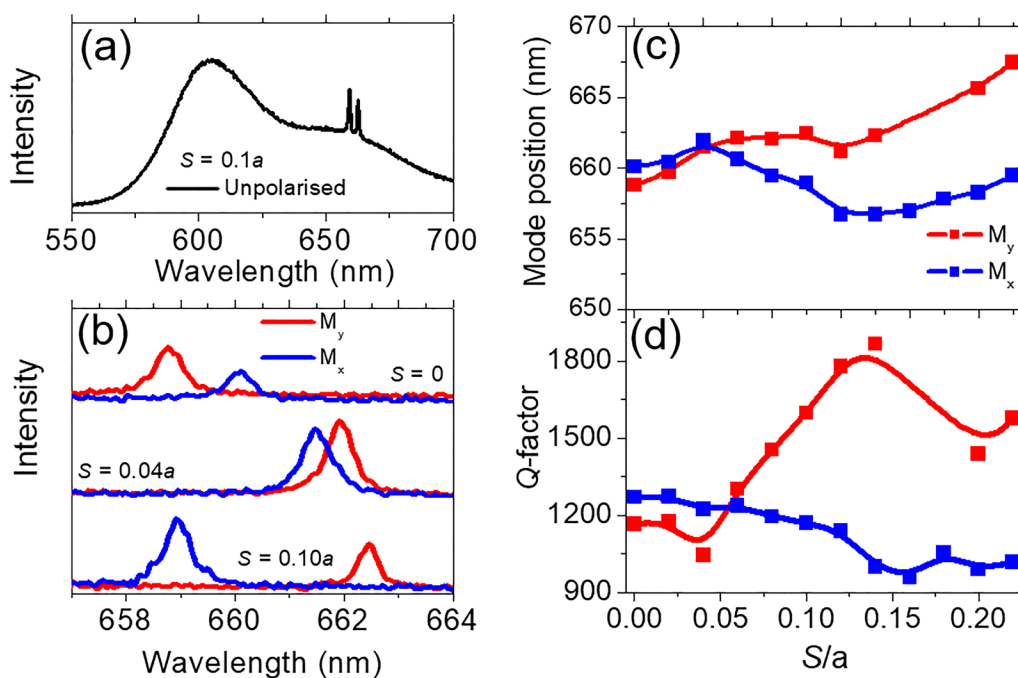


FIG. 5. (a) The fluorescence emission of unpolarized fluorescence emission of the Lumogen Red when coated onto a modified  $H1$  nano-cavity surface. (b) Measured emission spectra of modified  $H1$  nano-cavity as a function of the side airhole displacement  $s$ . (c) The measured spectral position of mode  $M_x$  and  $M_y$  as a function of  $s$ . (d) The measured Q-factor of  $M_x$  and  $M_y$  as a function of the side airhole displacement  $s$ .

collected from the cavity surface at normal incidence using a 50× objective lens with numerical aperture of 0.42. To reject plasma lines from the laser output, a long pass filter having a cutoff at 450 nm was placed just after the objective lens. The PL was then passed through an optical-polarizer oriented either parallel or perpendicular to the cavity  $x$  axis before being imaged into a 0.25 m liquid nitrogen cooled CCD spectrometer. To separate the nano-cavity emission from that of the surrounding region, the spectrometer slit width was reduced to 0.01 mm, with data recorded from the rows that correspond to the cavity image on the CCD.

Figure 5(a) shows a typical unpolarized PL emission spectrum measured from a modified  $H1$  nano-cavity coated with Lumogen Red having a hole size  $r = 0.3a$ ,  $r' = 0.23a$ , and  $r'' = 0.26a$ , where  $a = 260$  nm [see Fig. 1(b)]. As it can be seen, the nano-cavity supports two optical modes. In order to characterize these modes in more detail, the PL emission was measured as a function of the cavity side airhole shift  $s$  and emission polarization (selecting either  $M_x$  or  $M_y$  modes)—see typical emission spectra in Fig. 5(b). For the cavity having  $s = 0$ , the structure is characterized by two optical modes, which we identify as  $M_x$  and  $M_y$  with  $\lambda_{M_x} > \lambda_{M_y}$ . Such findings are in good agreement with the FDTD calculations presented in Fig. 2(b). Note that we observe small changes in the wavelength of mode  $M_x$  as a function of changing  $s$  [see Fig. 5(c)], a result most probably caused by uncontrolled variations in the structure of the photonic crystal rather than from changes in  $s$ . Encouragingly, we find that as  $s$  increases, mode  $M_y$  shifts to longer wavelengths as expected. Furthermore, the intensity of the emission peaks becomes comparable around  $s = 0.04a$  indicating the formation of a near degenerate unpolarized state.

In Fig. 5(d), we plot the experimentally determined  $Q$ -factor of modes  $M_x$  and  $M_y$  as a function of  $s$ . Here, the cavity  $Q$ -factor was deduced by fitting the cavity mode emission to a Lorentzian function. As it can be seen, the  $Q$ -factor of mode  $M_x$  is approximately constant as a function of  $s$ . However, the  $Q$ -factor of mode  $M_y$  has a clear dependence on  $s$  and takes a maximum value of 1875 at  $s = 0.14a$ , a result in close agreement with our FDTD simulations as presented in Fig. 2(d). Here, it can be seen that the measured  $Q$ -factor is slightly higher than the simulated  $Q$ -factor, an effect that we again attribute to structural differences between the modeled and fabricated structures.

#### IV. CONCLUSION

In summary, we have fabricated and modeled the optical properties of the dipole-like mode of an  $H1$  silicon nitride nano-cavity that is coated with a red-fluorescent molecular dye. By modifying the size and position of the six airholes surrounding the cavity, we showed that the  $Q$ -factor of a dipole-like mode can be enhanced by almost an order of magnitude compared to an unmodified  $H1$  cavity. We also confirm that it is possible to manipulate the polarization and the energy separation between the dipole-like cavity modes, with the cavity either characterized by spectrally separate modes having orthogonal polarization or a single unpolarized mode.

#### ACKNOWLEDGMENTS

We acknowledge the UK EPSRC for partial funding of this work via the Programme Grant “Hybrid Polaritonics” (No. EP/M025330/1) and “Nanoscale Organic Photonic Structures” (No. EP/D064767/1). M.M.M. acknowledges the Egyptian Ministry of Higher Education for the award of a Ph.D. studentship.

#### DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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