

# Transmission of butanol isomers in pervaporation based on series resistance model

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## Abstract

Pervaporation (PV) has shown great potential in the separation of butanol aqueous solutions due to their economic and environmental benefits. This work applies polydimethylsiloxane (PDMS) composite membrane to separate four butanol isomers (n-butanol, isobutanol, sec-butanol and tert-butanol) in aqueous solution. Based on physical and chemical properties of butanol isomers, such as solubility, polarity and interaction parameter, we systematically study the transmission difference in the pervaporation process. The influence of feed concentration, temperature and permeate pressure on membrane performance of PDMS composite membrane are investigated. The results show that the contact angles of butanol isomers on the PDMS layer are 51°, 42.7°, 37.7°, 29.1° and the fluxes at 40 °C are 237.6 g·m<sup>-2</sup>·h<sup>-1</sup>, 245.4 g·m<sup>-2</sup>·h<sup>-1</sup>, 224.1 g·m<sup>-2</sup>·h<sup>-1</sup>, 169.4 g·m<sup>-2</sup>·h<sup>-1</sup> for n-butanol, isobutanol, sec-butanol, and tert-butanol, respectively. Moreover, the similar compatibility principle is introduced to the series resistance model so the process simulation matches well with the antagonistic effect of water molecules on mass transfer of butanol isomers. The permeation activation energy is negative, indicating that the dissolution dominates the dissolution and diffusion process. In addition, low vacuum is not conducive to the separation of n-butanol from water. The research on isomers separation through pervaporation may pave a way to separate other solvents of similar properties.

**Keywords:** pervaporation; polydimethylsiloxane; butanol isomers; series resistance model



## 1. Introduction

The extensive application of new energy sources, including solar, wind, and nuclear energy, are impeded by energy storage infrastructure that provides stable power transmission. Lithium-ion batteries have the highest energy density among currently available energy storage systems, but the maximal energy density of lithium-ion batteries is  $2 \text{ MJ}\cdot\text{kg}^{-1}$ , still less than that of liquid fuels ( $27\text{-}47 \text{ MJ}\cdot\text{kg}^{-1}$ ) [1]. To alleviate the global shortage of fossil fuels and reduce the solid emissions, people turn the attention to biofuels [2]. Butanol has a high octane number and energy density. While blended with other fuels, it can allow a relatively higher water content in the system and therefore is convenient for transportation and storage [3].

Butanol is always produced by fermentation of biomass and traditional separation includes adsorption [4], extraction [5, 6], salting out [7], and membrane techniques [8]. The adsorption process is impeded by the high costs of the adsorbents. The extraction and salting out introduce the third part that causes secondary pollution and increases the difficulty of subsequent separation. By contrast, Pervaporation (PV) is an emerging technique with advanced membrane materials [9]. The membrane materials mainly include water-selective membrane and organic-selective membrane [10, 11]. The organic-selective membrane has obvious technical and economic benefits for the separation of azeotropes or isomers at a low concentration [9, 12]. Among organic-selective membrane materials, polydimethylsiloxane (PDMS) is relative cheap with an alternating O-Si-O unit structure. It is the most promising membrane material for separation and recovery of butanol [13]. The differences of separation system, such as solvent solubility in water, boiling point, molecular structure and inherent properties of the solvent, and operating conditions, inevitably affect the mass transfer.

Many researches investigate some important parameters for the PV process, including molecular size, equilibrium partial vapor pressure ( $P_i^{sat}$ ), activity factor ( $\gamma_i$ ), solubility parameter ( $\delta$ ), and interaction parameter ( $\chi$ ). It partly explains the difference in mass transfer of different components. To separate dimethyl carbonate from methanol, the solubility parameter is crucial for the component to pass through [14]. For the separation of binary, ternary and quaternary acetone/butanol/ethanol (ABE)/water mixed systems, the mass transfer of each solvent is correlated with its equilibrium partial vapor pressure and solubility parameters [15]. In addition, the interaction force among the solvents and that between the components and the membrane cause the permeate differences. The separation

1 factor of acetone is much larger than that of n-butanol and ethanol. For phenol and methanol, the  
2 preferential dissolution directly leads to different separation factors of solvents [16]. The solubility  
3 parameter is an important prerequisite for the solvent transfer in the composite membrane [17]. In the  
4 separation of n-butanol, ethanol, and ethyl acetate from aqueous solution, ethyl acetate has higher  
5 selectivity than n-butanol and ethanol due to the better solubility of ethyl acetate in PDMS [18].

6 Furthermore, much attention is focused on modeling of PV membranes with an emphasis of  
7 interface action. The series resistance model is generally used to study the mass transfer of the  
8 components in the boundary layer between the liquid feed and the composite membrane. The results  
9 show that the resistance of the boundary layer has little effect on transfer process and it can be  
10 weakened by increasing flow velocity [19-22]. The study of permeation activation energy shows that  
11 dissolution is the dominant step [23, 24]. Therefore, the resistance of the PV process is concentrated  
12 in the dissolution process. So far, no systematical studies on the mass transfer state of butanol isomers  
13 have been explored. Moreover, due to the similar compatibility principle, the resistance of the  
14 boundary layer comes not only from the thickness of the boundary layer but also from the interaction  
15 between solvents and water. Therefore, single factors such as solubility parameters or polarity cannot  
16 describe the mass transfer of butanol isomers.

17 In this work, we systematically studied the mass transfer differences (binary and ternary) of  
18 butanol isomers in PDMS composite membranes. The preferred selectivity to the pure solvent of  
19 butanol isomers is obtained by calculating the interaction parameters, half-time empirical formula  
20 and swelling formula. The differences in terms of polarity, solubility parameter, and boiling points  
21 between solvents for separation and selectivity are explored by changing the concentration,  
22 temperature, and vacuum. This research is a reasonable guidance to separation of butanol isomers and  
23 other solvents with similar properties.

## 24 2. Experimental Section

### 25 2.1 Materials

26 All of the raw materials and reagents (analytical grade) are purchased from commercial vendors  
27 and used without further purification: n-butanol (99%, Sinopharm Chemical Co. Ltd., China),  
28 isobutanol (99%, Sinopharm Chemical Co. Ltd., China), sec-butanol (99%, Sinopharm Chemical Co.  
29 Ltd., China), tert-butanol (Sinopharm Chemical Co. Ltd., China). The physicochemical properties of

1 solvents are shown in Table S1 of the support information and their polarity follows the order of n-  
2 butanol<isobutanol<sec-butanol<tert-butanol [25]. The commercial PDMS composite membranes  
3 are provided by Nanjing Jiushi High-Tech Co., Ltd. This type of membrane consists of PDMS top  
4 layer, polyvinylidene fluoride (PVDF) intermediate layer and non-woven fabrics substrate layer. The  
5 top layer is 10  $\mu\text{m}$  thickness and mean pore size of intermediate layer is around 76 nm.

## 6 2.2. Commercial membrane characterization

7 Fourier transform infrared spectra (ATR-FTIR, Thermo, Nicolet Nexus 470 spectrometer, USA)  
8 are employed to characterize the surface properties of the PDMS membrane in the range of 500-4000  
9  $\text{cm}^{-1}$ . The morphology of the membrane materials is observed by field emission scanning electron  
10 microscope (FESEM, Hitachi S-4800) using an acceleration voltage of 2 kV. The contact angle is  
11 measured on JC2000D contact angle apparatus (Shanghai ZhongChen Digital Technology Apparatus  
12 Co. Ltd).

## 13 2.3 Swelling experiments

14 Homogeneous PDMS membranes with the thickness of 2 mm are prepared referring to the  
15 reported [26]. The solubility and diffusion rate of butanol isomers in the PDMS homogeneous  
16 membrane is measured by weight method. Put the homogeneous membrane in a vacuum drying oven  
17 at 60  $^{\circ}\text{C}$  for 24 hours and record the mass ( $W_d$ ) of the dry membrane. Soak the membranes of known  
18 weight and thickness ( $l$ ) in pure solvents of n-butanol, isobutanol, sec-butanol and tert-butanol,  
19 respectively. After a given time ( $t$ ), take it out and wipe the membrane surface with a dust-free cloth.  
20 The mass ( $W_t$ ) of swollen homogeneous membrane is recorded and then put back into the pure solvent.  
21 Repeat until no further weight gain and the final mass ( $W_s$ ) of the membrane is the swelling limit.

## 22 2.4 Pervaporation

23 The PV device consists of feed tank, water bath, peristaltic pump, membrane module (membrane  
24 area of 153.86  $\text{cm}^2$ ), cold trap, and vacuum pump (Fig. 1). The feed liquid is cross-flowed through  
25 the membrane module through the peristaltic pump at a flow rate of 68.4  $\text{L}\cdot\text{h}^{-1}$  (Reynolds coefficient  
26  $\approx 253.8$ ), and the retentate is cycled to the raw material tank. The permeation side of the membrane  
27 is connected to the vacuum system to form the driving force. A glass cold trap is installed between  
28 the membrane module and the vacuum pump to collect the permeate at -70  $^{\circ}\text{C}$ . For a high  
29 concentration of butanol, the permeate is stratified so the permeate is diluted 10 times before injecting

1 into gas chromatograph for quantitative analysis. All experimental results are repeated three times  
2 and have an error of <5 %.

3 The feed liquid of 1.2 L is preheated for half an hour and then sampled and analyzed after  
4 stabilized. Three experiments are performed in parallel and the average value is taken. The  
5 concentration of butanol isomers in the feed liquid is 1~3 wt% and the temperature of the feed liquid  
6 is 30~60 °C with the vacuum pressure is 0.3 kPa~4 kPa.

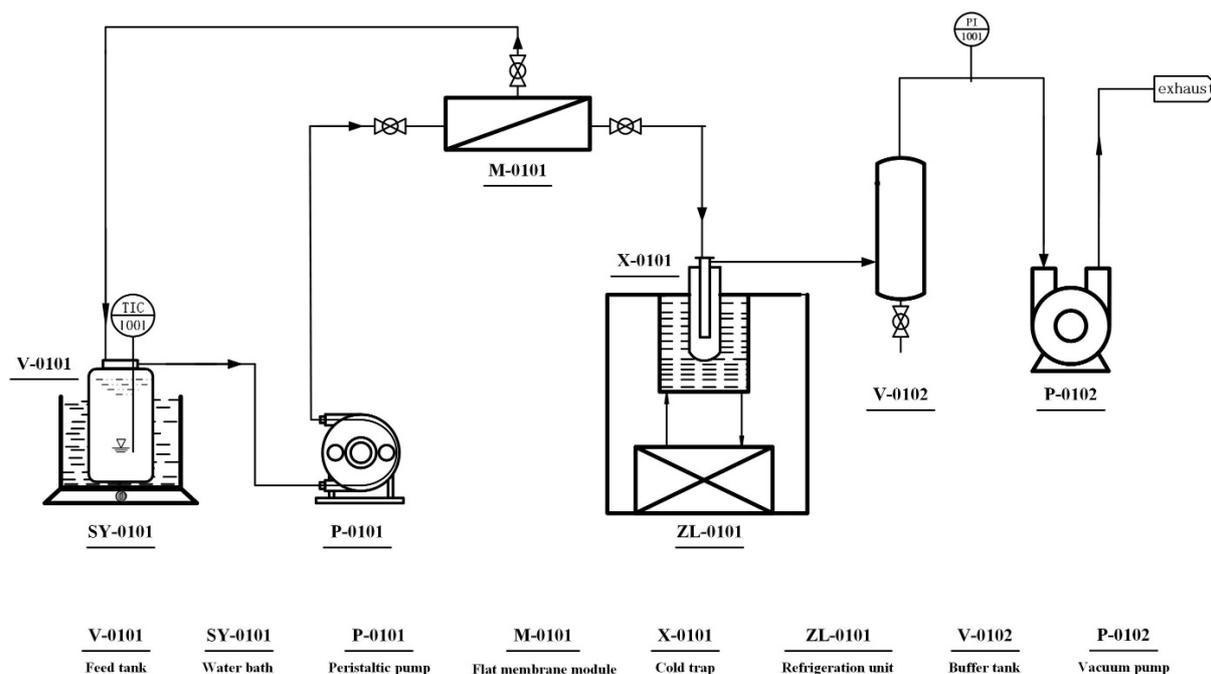


Fig. 1. Experimental device diagram.

## 9 2.5 Data analytic methods

10 Swelling degree (S) of the homogeneous membrane is calculated by Eq. (1). Theoretically, when  
11 a homogeneous membrane is swelled in different solvents, the diffusion coefficients (D) of the  
12 solvents are different. To simplify, we assume that the diffusion coefficient is constant during the  
13 dissolution process. Therefore, the half-time empirical formula [14] is used to calculate the diffusion  
14 coefficient of butanol isomers in a homogeneous membrane, by Eq. (2).

$$15 \quad S = \frac{W_s - W_d}{W_d} \quad (1)$$

$$16 \quad D = \frac{0.04919l^2}{t_{0.5}} \quad (2)$$

17 Where  $W_d$  and  $W_s$  are the weight before and after swelling;  $l$  is the thickness and  $t_{0.5}$  is the time to  
18 achieve solvent uptake  $W_t/W_s = 0.5$ .

1 Assuming that the adsorption isotherm of the solvent for the membrane is linear and the solvent  
2 diffusion coefficient is independent of the solvent concentration, an ideal selectivity is calculated by  
3 Eq. (3):

$$4 \beta_{ideal,i,n} = \frac{S_i D_i}{S_n D_n} \quad (3)$$

5 Where  $i$  represents isobutanol, sec-butanol or tert-butanol, and  $n$  represents n-butanol;  $S$  is swelling  
6 degree.

7 The PV performance of PDMS composite membrane is usually expressed in terms of the flux  $J_i$   
8 and separation factor  $\alpha$ , which are determined by Eqs. (4) and (5):

$$9 J_i = \frac{m_i}{At} \quad (4)$$

$$10 \alpha = \frac{y_i/(1-y_i)}{x_i/(1-x_i)} \quad (5)$$

11 where  $m_i$  is the weight of component  $i$  in the permeate (g);  $A$  is the effective membrane area ( $m^2$ ); and  
12  $t$  is the permeation time interval for the pervaporation (hours);  $y_i$  and  $x_i$  are the weight fractions of  
13 components in the permeate and feed, respectively

14 Since changes in flux and separation factor are easily affected by operating conditions,  
15 normalizing the flux relative to the permeation driving force will help understand the permeability of  
16 the membrane itself to the components. The inherent properties of the membrane can be expressed as  
17 permeability  $P_i$  and selectivity  $\beta$ , which are determined by Eqs. (6) and (7):

$$18 P_i = \frac{J_i \times l}{x_i^f \gamma_i p_i^{sat} - y_i p_i^P} \quad (6)$$

$$19 \beta = \frac{P_i}{P_j} \quad (7)$$

20 where  $l$  is the membrane thickness (No changes in thickness are involved so it can be ignored);  $\gamma_i$  is  
21 the activity of components  $i$ ,  $p_i^{sat}$  is the equilibrium partial pressure of  $i$  in the feed, both are calculated  
22 by the non-random two-liquid model (NRTL) in Aspen;  $x_i^f$  and  $y_i$  are mole fraction of  $i$  in the feed and  
23 permeate,  $p_i^P$  is permeation pressure;  $P_i$  and  $P_j$  are permeability of solvent and water, respectively.

24 The relationship between the flux and temperature can be described by Arrhenius rule [27], it is  
25 obtained by Eq. (8):

$$26 J = J_0 \exp\left(-\frac{E_a}{R_g T}\right) \quad (8)$$

27 Where  $J_0$  is the pre-exponential factor;  $E_a$  is the apparent activation energy ( $J \cdot mol^{-1}$ );  $R_g$  is the gas  
28 constant ( $J \cdot mol^{-1} \cdot K^{-1}$ );  $T$  is the kelvin temperature (K).  $E_a$  represents the relationship between flux and

1 temperature, and there is also a relationship between permeability  $P$  and driving force  $\Delta p$ , which  
2 derived the Eq. (9):

$$3 \quad J = \frac{P}{l} \Delta p \rightarrow \frac{P}{l} = \frac{J}{\Delta p} = \frac{P_0}{l} \exp\left(-\frac{E_p}{R_g T}\right) \quad (9)$$

4 The permeation activation energy  $E_p$  of the influence of temperature on membrane permeability  
5 is the slope of the relationship between  $\ln(J/\Delta p)$  and  $1/T$ , not  $\ln J$  and  $1/T$ . When the pressure on the  
6 permeate side is lower than the feed side, the  $E_p$  value can be calculated by Eq. (10), subtracting the  
7 enthalpy of evaporation ( $\Delta H_v$ ) from the apparent activation energy [28]:

$$8 \quad E_p = E_a - \Delta H_v \quad (10)$$

9 Where  $E_p$  is the permeation activation energy of each component ( $\text{J}\cdot\text{mol}^{-1}$ );  $\Delta H_v$  is the heat of  
10 vaporization of each component ( $\text{J}\cdot\text{mol}^{-1}$ ). This equation expresses the influence of the enthalpy  
11 change caused by the phase change on the permeability behavior of the component [29].

12 The interaction parameter  $\chi$  is calculated by Flory-Huggins equation [30], by Eq. (11):

$$13 \quad \chi = \frac{V_i}{R_g T} (\delta_2 - \delta_1)^2 \quad (11)$$

14 Where  $\delta_1$  and  $\delta_2$  are the solubility parameters of PDMS and solvent respectively ( $\text{J}^{1/2}\cdot\text{cm}^{-3/2}$ );  $V_i$  is the  
15 molar volume of component  $i$  ( $\text{cm}^3\cdot\text{mol}^{-1}$ ). The smaller the interaction parameter, the stronger the  
16 affinity, the higher the solubility of the solvent in PDMS.

17 The total mass transfer coefficient represents the mass transfer rate of butanol isomers in a  
18 certain membrane area in a certain period,  $K_{ov}$  is calculated by Eq. (12):

$$19 \quad K_{ov} = \frac{V}{At} \ln\left(\frac{x_i}{x_{i,t}}\right) \quad (12)$$

## 20 3. Results and Discussion

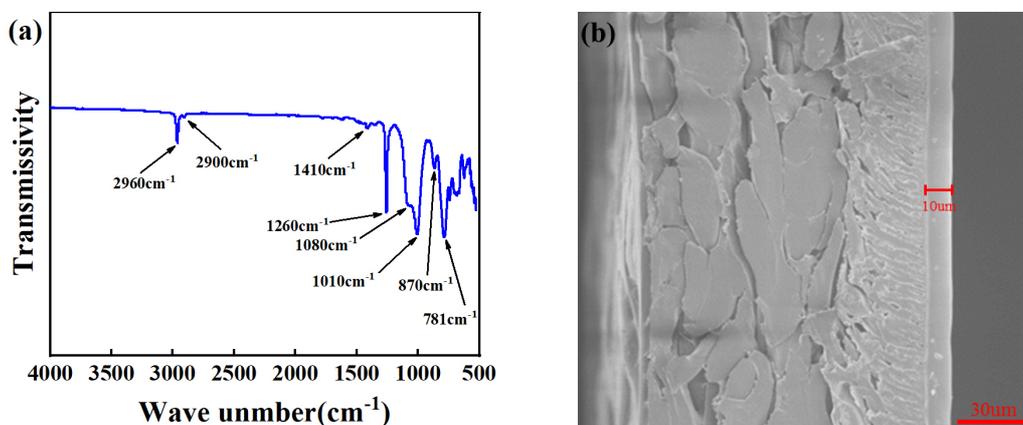
### 21 3.1 Characterization of PDMS selective layer

#### 22 3.1.1 Surface properties and cross-section morphology of PDMS

#### 23 membrane

24 The FTIR spectra show the absorption peaks at  $2960 \text{ cm}^{-1}$  and  $2900 \text{ cm}^{-1}$  (Fig. 2), which indicates  
25 the asymmetric stretching vibration and symmetric stretching vibration of the PDMS side chain (C-  
26 H bond), respectively. The peaks near  $1410 \text{ cm}^{-1}$  and  $1260 \text{ cm}^{-1}$  are the absorption peaks of Si-C  
27 bonds. The peaks at  $1080 \text{ cm}^{-1}$  and  $1010 \text{ cm}^{-1}$  indicate the asymmetric stretching vibration of the Si-

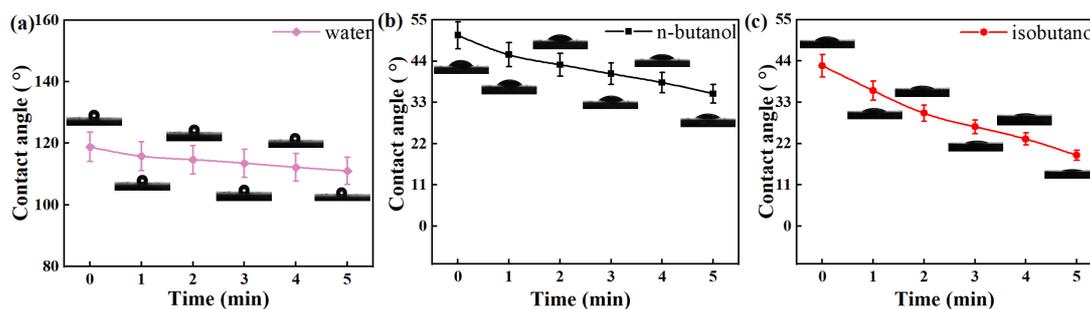
1 O-Si bonds, while  $870\text{ cm}^{-1}$  and  $781\text{ cm}^{-1}$  peaks are attributed to its symmetric stretching vibration.  
2 The results show that the commercial composite membrane conforms to the reported [31]. The cross-  
3 sectional morphology of the PDMS composite membrane is observed by a FESEM. The thickness of  
4 the functional layer is  $10\text{ }\mu\text{m}$  and the interface is compatible without any fault (Fig. 2b).



5  
6 Fig. 2. (a) ATR-FTIR spectra and (b) cross-section morphology of PDMS selective layer.

### 7 3.1.2 The affinity of PDMS membrane to butanol isomers and water

8 The affinity between the PDMS composite membrane and the solvents is measured by the  
9 surface dynamic contact angle instrument. Fig. 3 shows that the PDMS layer has a higher hydrophobic  
10 angle and a lower affinity butanol angle, indicating that butanols preferentially dissolve in the  
11 functional layer. Comparing Fig. 3b-e, it can be found that the contact angle of butanol isomers  
12 follows the order of  $n\text{-butanol} > \text{isobutanol} > \text{sec-butanol} > \text{tert-butanol}$ , consistent with the interaction  
13 parameter rule in SI (Table S1).



14

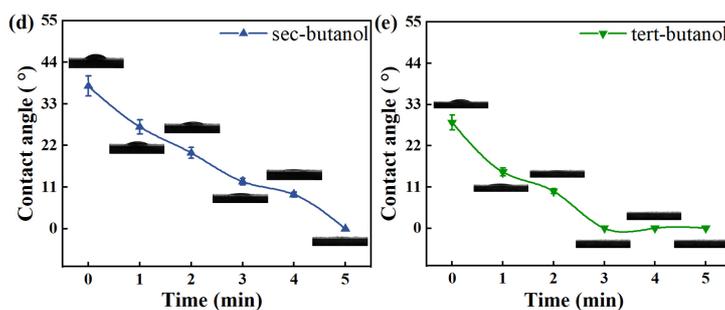


Fig. 3. (a) Water dynamic contact angle and (b-e) butanol dynamic contact angle of the PDMS membranes.

### 3.1.3 Swelling of pure solvent in PDMS membrane

The process of dissolving the butanol isomers in the PDMS composite membrane is a process of breaking the polymer chain and swelling the membrane, which changes the microstructure of the composite membrane and affects the flux and separation factor of the composite membrane [15]. Fig. 4a depicts the swelling process of pure solvents of n-butanol, isobutanol, sec-butanol, and tert-butanol in the PDMS homogeneous membrane. As the interaction parameters between different solvents and PDMS decrease, the solubility of the solvent in the composite membrane gradually increases. The specific swelling degree is shown in Fig. 4b. As the molecular volume of the component increases and the molecular structure becomes more complex, although the interaction between the solvent and the PDMS layer becomes larger, the time required to reach the swelling equilibrium also becomes longer. This indicates that the molecular structure and molecular volume will affect the diffusion rate of butanol isomers in the PDMS composite membrane.

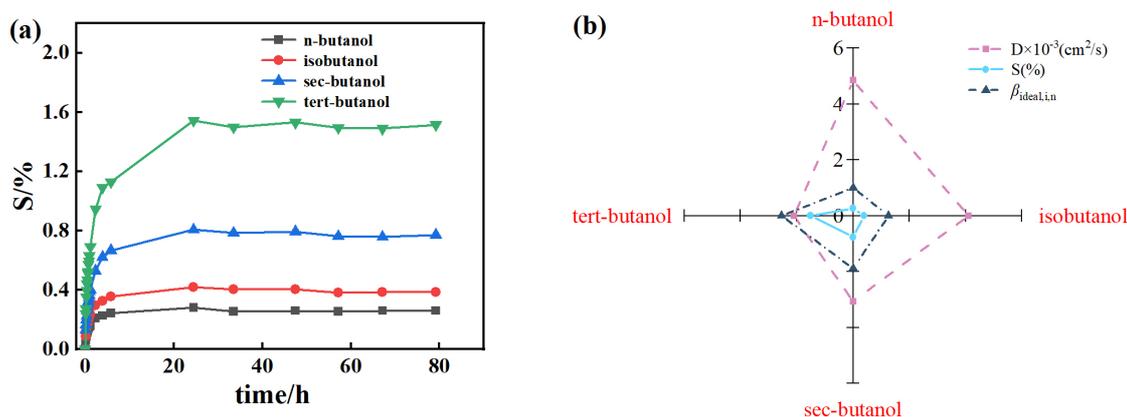


Fig. 4. (a) Swelling degree of PDMS membrane in butanol isomers; (b) Solubility and diffusion of butanol isomers in PDMS.

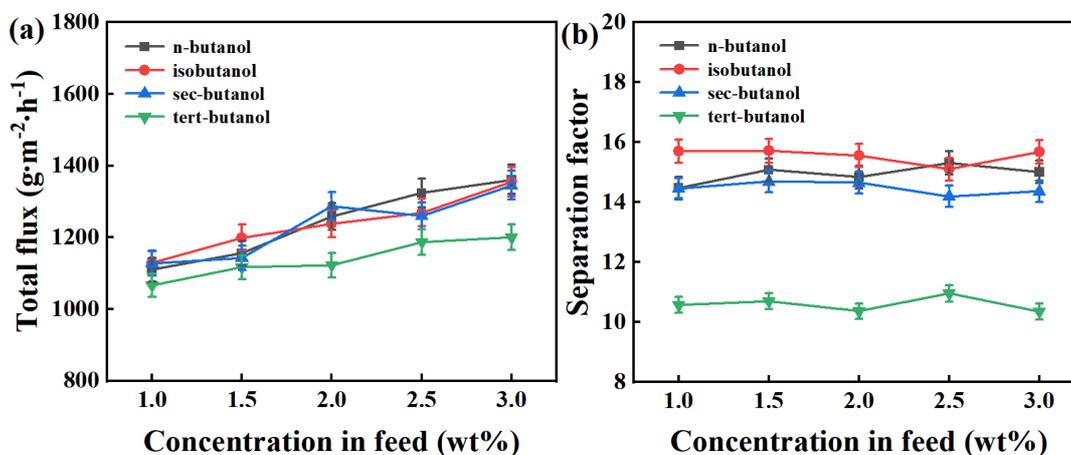
In order to quantitate the diffusion of butanol isomers, the half-time empirical formula is used to estimate the diffusion coefficient of pure solvent in the PDMS homogeneous membrane. First, the

1 second-order polynomial fitting is performed on the curve of swelling degree with time while its  $R^2$   
2  $\geq 0.9$ . Through Eq. (2) to obtain the diffusion coefficient of each solvent, as shown in Fig. 4b. The  
3 tight cross-linking network in the homogeneous membrane of PDMS makes the molecular structure  
4 and volume of the solvent particularly sensitive to the resistance of the diffusion process. Combining  
5 the molecular volume and structure of the components (Table S1) and the diffusion coefficient of  
6 each component (Fig. 4b), it can be seen that its diffusion coefficient gradually decreases as the  
7 component structure becomes more complex and the molecular volume becomes larger. Moreover,  
8 the swelling degree of each component has opposite trends. The dynamic swelling of polyethylene  
9 (PE) membrane in pure butanol solvent had the similar outcomes [32]. This is due to the differences  
10 of solubility and molecular structure of the components.

## 11 3.2 PV performance

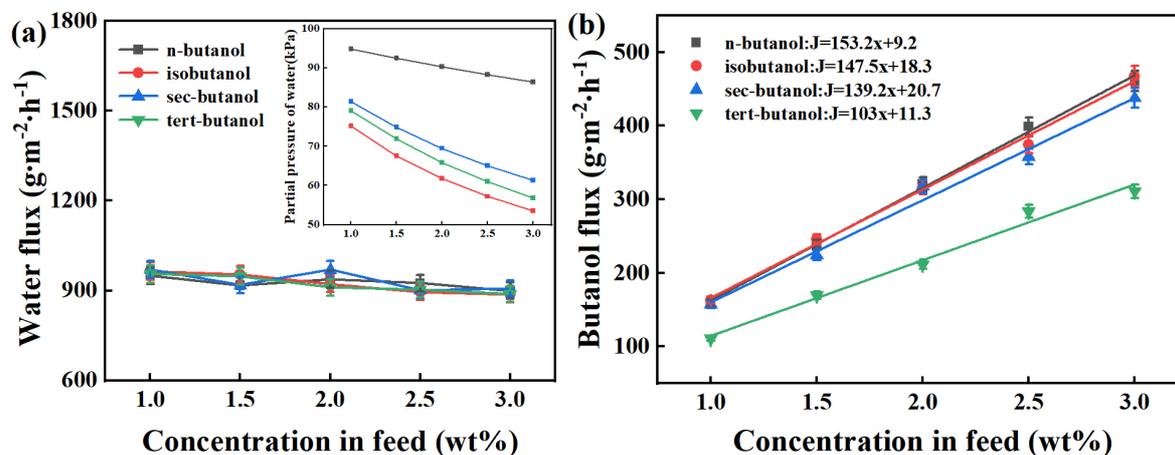
### 12 3.2.1 Effect of feed concentration in binary system

13 The pervaporation process is jointly controlled by dissolution and diffusion, and therefore, the  
14 concentration of the solvent in the feed plays a crucial role. Fig. 5 describes the flux and separation  
15 factor of the PDMS composite membrane for the butanol isomer/water binary system with different  
16 feed concentrations at 40 °C. For any one type of butanol, as the feed concentration increases, the  
17 total flux gradually rises (Fig. 5). The separation factor maintains constant and the order is isobutanol  
18 (15.5)>n-butanol (14.9)>sec-butanol (14.4)>tert-butanol (10.6). This result in Fig. 5(b) is contrary to  
19 the interaction parameters, and does not comply with “stronger affinity will lead to higher permeation”  
20 [15], for reasons which will be discussed later.



21  
22 Fig. 5. Effect of feed concentration in butanol/water binary system on (a) total flux and (b) separation factor (feed  
23 temperature: 40 °C, Vacuum: 0.3 kPa).

1 Fig. 6a shows that the water fluxes in the four systems remain unchanged as the feed  
 2 concentration increases. The sufficient water in the feed results in the solubility of water molecules  
 3 in the membrane unchanged, as well as the mass transfer force of water molecules. Therefore, the  
 4 increase in total flux in Fig. 5a is mainly due to the increase of butanol permeation.



5  
 6 Fig. 6. Effect of butanol isomers (dual system) feed concentration on (a) water flux, partial pressure and (b)  
 7 butanol flux (feed temperature: 40 °C, Vacuum: 0.3 kPa; the inserted is the correlation between the partial pressure  
 8 of water and the feed concentration of butanol isomers).

9 The Fig. 6b shows that the flux of each butanol component increases linearly with the increase  
 10 of the feed concentration. Therefore, the linear fit of the flux of each butanol with the concentration  
 11 is performed by the least square method while its  $R^2 \geq 0.99$ . The transmission resistance ( $f_{3,i}$ ) of  
 12 butanol isomers in the PDMS composite membrane (Figure S2) follows the order of tert-butanol>sec-  
 13 butanol>isobutanol>n-butanol, consistent with the solvent diffusion coefficient in Fig. 4b.

14 The permeability and selectivity can better understand the transmission of butanol isomers in  
 15 the PDMS composite membrane [25]. As shown in Fig. 7, the permeability of butanol isomers  
 16 increases with the increasing feed concentration of butanol. As a result, the PDMS composite  
 17 membrane exhibits constant selectivity for the four structures of butanol isomers, which are 3.2, 0.55,  
 18 0.74, 0.46 for n-butanol, isobutanol, sec-butanol, and tert-butanol, respectively. It can be seen from  
 19 Fig. S1b that the partial pressure of butanol increases with the increasing feed concentration of  
 20 butanol, which makes the  $P_i^{sat}$  of the water drop (Fig. 6a). The water flux is unchanged during the  
 21 separation process but water permeability increases with the increasing feed concentration of butanol  
 22 isomers. Therefore, it can be concluded that the equilibrium partial pressure of water has little  
 23 influence on the water flux while feed concentration of butanol changes.

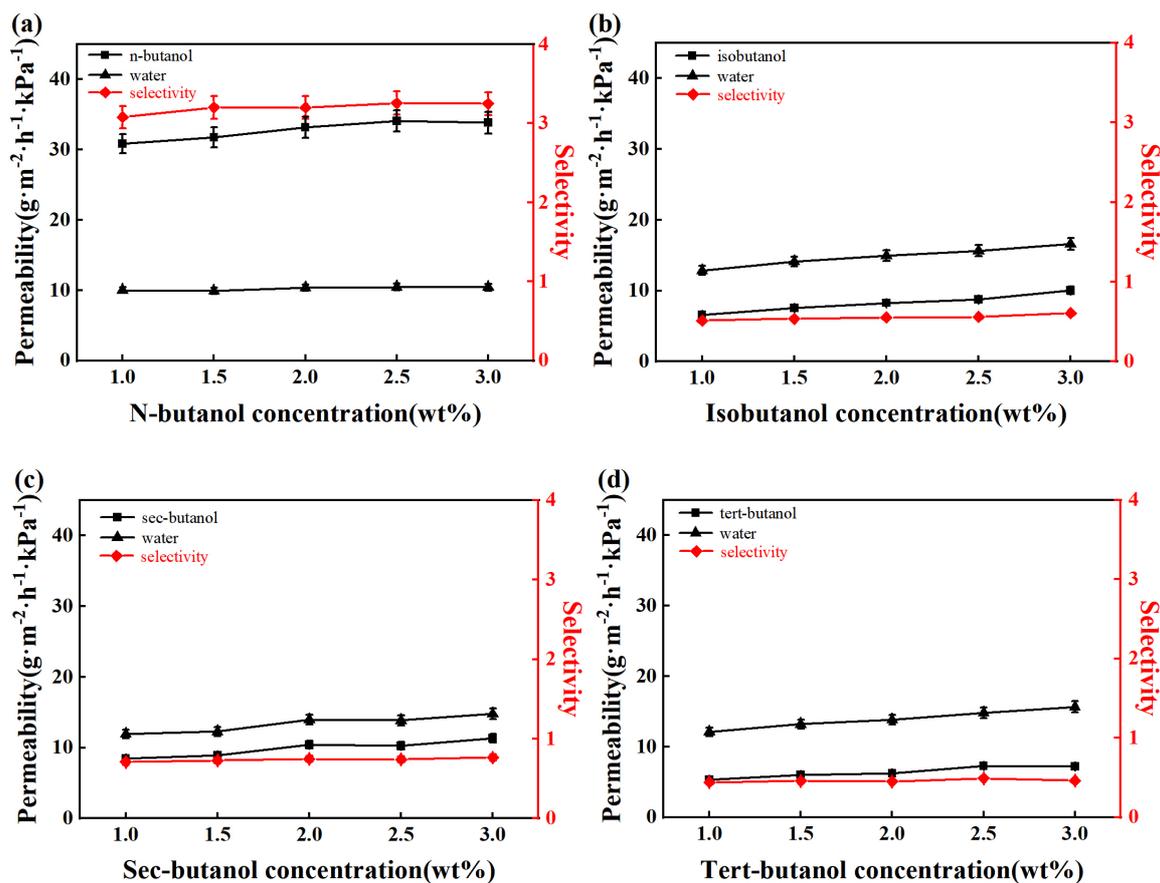


Fig. 7. Effect of feed concentration in butanol/water binary system on permeability and selectivity

(a) n-butanol (b) isobutanol (c) sec-butanol (d) tert-butanol (feed temperature: 40 °C, Vacuum: 0.3 kPa).

It is worth noting that in the same feed concentration, the permeability of n-butanol is the highest, followed by sec-butanol, isobutanol and tert-butanol. Although the flux of isobutanol is higher than that of n-butanol and sec-butanol, the equilibrium partial pressure of isobutanol is much higher than that of other components, resulting in lower permeability of isobutanol than n-butanol and sec-butanol. Therefore, the solvent separation factor of the PDMS composite membrane in Fig. 5b may be dominated by the polarity between the components (shown in Section 2.1). For instance, n-butanol with its smallest polarity can allow it to pass through the PDMS composite membrane at the fastest rate [18]. For tert-butanol, the most polar of the four isomers, it will form large water clusters with water [33], increasing mass transfer resistance. It can be seen from Table S1 that tert-butanol is miscible with water, while n-butanol, isobutanol and sec-butanol are partially miscible with water. Its solubility follows an order of n-butanol < isobutanol < sec-butanol, indicating that the force between water molecules and butanol isomers will produce different mass transfer resistance ( $f_{i,i}$ ), which leads to different separation factors. The polar components have better compatibility and a stronger

1 interaction with water. In addition, the PDMS composite membrane is a hydrophobic and may also  
2 affect the transfer of butanol isomers. The water fluxes in the n-butanol/water and isobutanol/water  
3 systems are similar. With the increase of water ratio in the feed of binary system, the permeability of  
4 tert-butanol is the lowest, while the permeability of n-butanol is greater than that of isobutanol [38].  
5 This phenomenon shows that the interaction between water and tert-butanol is stronger than that  
6 between n-butanol/isobutanol and water. No matter how the water ratio changes, it has little effect on  
7 the flux of n-butanol, isobutanol and sec-butanol, but when the water ratio rises to 70 wt%, the flux  
8 of tert-butanol drops sharply [32]. By investigating the influence of the concentration of butanol in  
9 the feed on the separation of the butanol isomers/water binary system, the interaction parameters  
10 cannot be used to predict the separation effect of solvent and water, as the solubility of butanol isomers  
11 in water may have a certain impact.

### 12 3.2.2 Binary system VS ternary system

13 Based on the research of the butanol/water binary system, water may have an antagonistic effect  
14 on the PV separation process. Therefore, isobutanol, sec-butanol, and tert-butanol are used for  
15 comparison. The two-structure butanol (50 wt%/50 wt%) binary system and the two-structure  
16 butanol/water (1 wt%/1 wt%/98 wt%) ternary system are studied, as shown in Fig. 8. When isobutanol,  
17 sec-butanol and tert-butanol are successively present in the binary mixture, the separation factor of  
18 the three structures of butanol is much higher than that of n-butanol. According to the interaction  
19 parameters in Table S1, the dissolution resistance ( $f_{2,i}$ ) of butanol isomers in the membrane layer  
20 follows the order of tert-butanol<sec-butanol<isobutanol<n-butanol. Therefore, the order for  
21 separation factor of butanol binary system is tert-butanol>sec-butanol>isobutanol>n-butanol, which  
22 is the same as the  $\beta_{ideal,i,n}$  in Fig. 4(b). At this point, the interaction parameter has a decisive effect on  
23 the mass transfer of the components. The separation factor and total flux of the binary mixture of n-  
24 butanol/tert-butanol are 1.87 and 3825.6  $\text{g}\cdot\text{m}^{-2}\cdot\text{h}^{-1}$ , respectively. Compared with the Polyamide/ $\beta$ -  
25 cyclodextrin mixed matrix membrane and Polyamide/modified  $\beta$ -cyclodextrin mixed matrix  
26 membrane [34, 35], the PDMS membrane has more advantages in separating the binary mixture of  
27 n-butanol/tert-butanol.

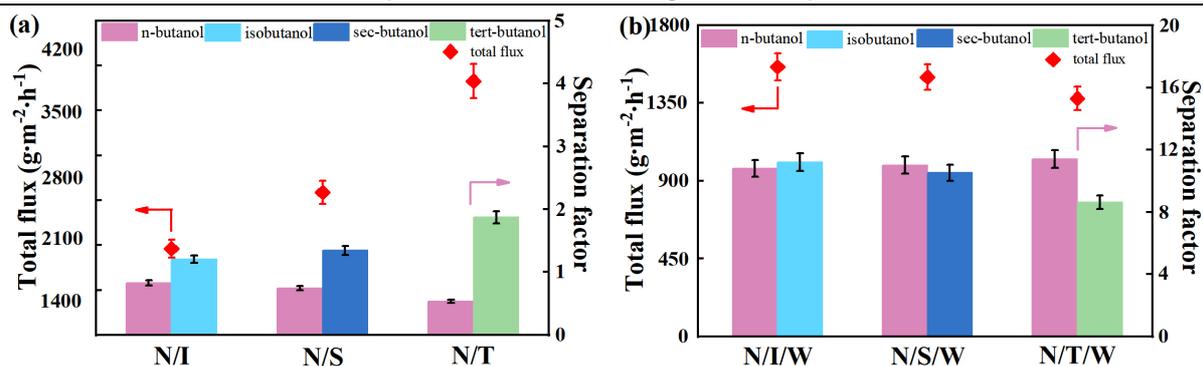


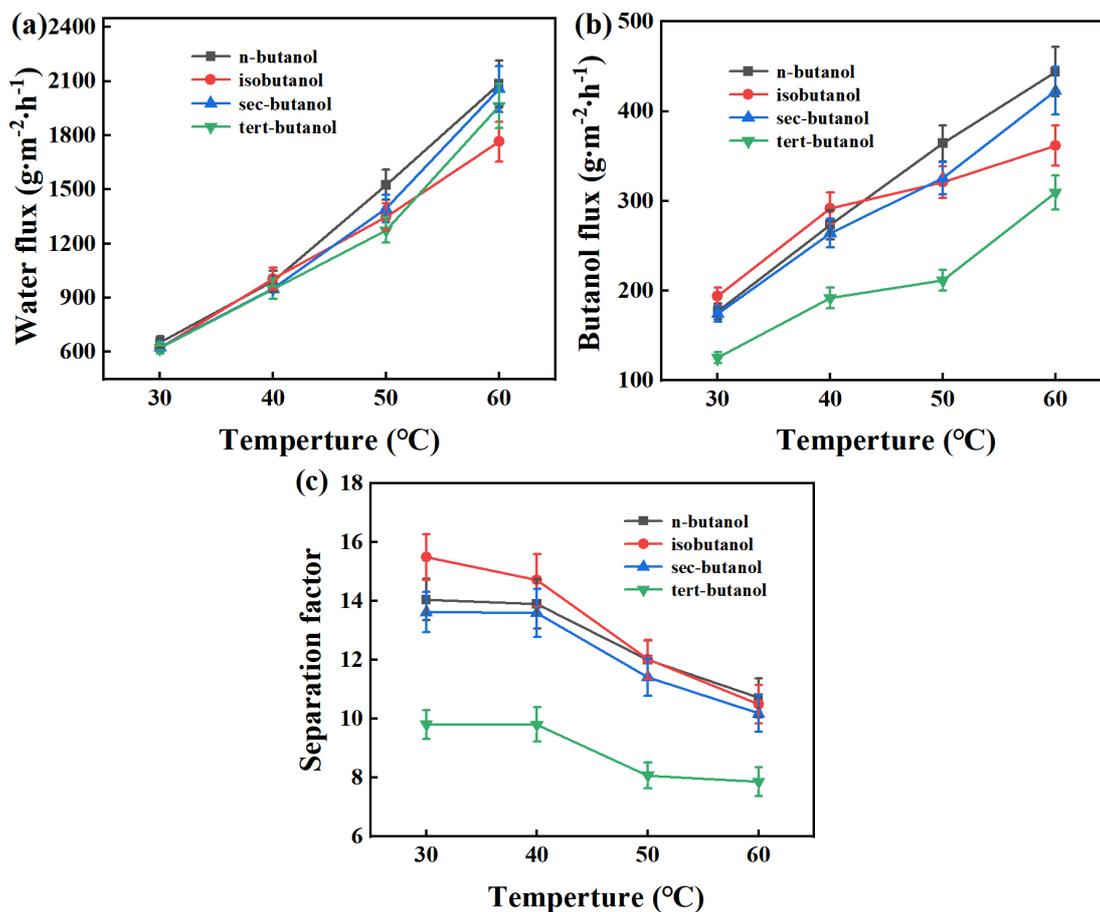
Fig. 8. Total flux and separation factor. (a) Butanol isomers with feed ratio of 1:1; (b) Binary butanol isomers in water with feed ratio of 1:1:98 (feed temperature: 40 °C, Vacuum: 0.3 kPa).

Fig. 8b shows that the separation factors for the ternary system follow an order of isobutanol > n-butanol > sec-butanol > tert-butanol, same as that for the butanol/water binary system. Comparing the total flux in Fig. 8, we can find that with isobutanol, sec-butanol and tert-butanol in the system, the total flux of the binary system is increasing, while the total flux of the ternary system is decreasing. This phenomenon is due to the stronger transmission resistance of water molecules to solvents of high solubility. Therefore, the separation factor of butanol isomers follow the order of polarity. The solubility of n-butanol and isobutanol in water is similar, and the interaction force between isobutanol and the functional layer is greater than that of n-butanol, which results in a greater separation factor of isobutanol than n-butanol. By comparing the binary and ternary systems, the polarity between the solvent and water and the interaction parameters between the solvent and PDMS together determine the separation performance in the pervaporation process.

### 3.2.3 Influence of feed temperature

Temperature plays an important role in the PV process. It not only affects the thermodynamic process of dissolution, but also the kinetic process of component diffusion in the membrane. Therefore, under the butanol concentration of 2 wt%, the effect of the feed temperature is investigated. The results are shown in Fig. 9. As the temperature increases, the flux of each component increases and the separation factor decreases. The temperature increase promotes mass transfer and the migration of polymer chains, which increases the flux [32]. Moreover, the molecular dynamic diameter of water molecules is smaller than that of butanol isomers, which makes it easier to pass through the preferentially organic-permeable membrane and occupy the permeation channel. So the separation factor is reduced. As the temperature increases, the water molecules show similar fluxes

1 in the four systems (Fig. 9a). The flux of butanol isomers is significantly smaller than the water flux  
2 as the pervaporation process is jointly controlled by dissolution and diffusion (Fig. 9b). The higher  
3 temperature increases the thermal motion of molecules and weakens the formation of water clusters.  
4 The diffusion rate of water molecules in the PDMS layer is greater than that of butanol isomers [36].  
5 As a result, the separation factor gradually decreases with increasing temperature (Fig. 9c).



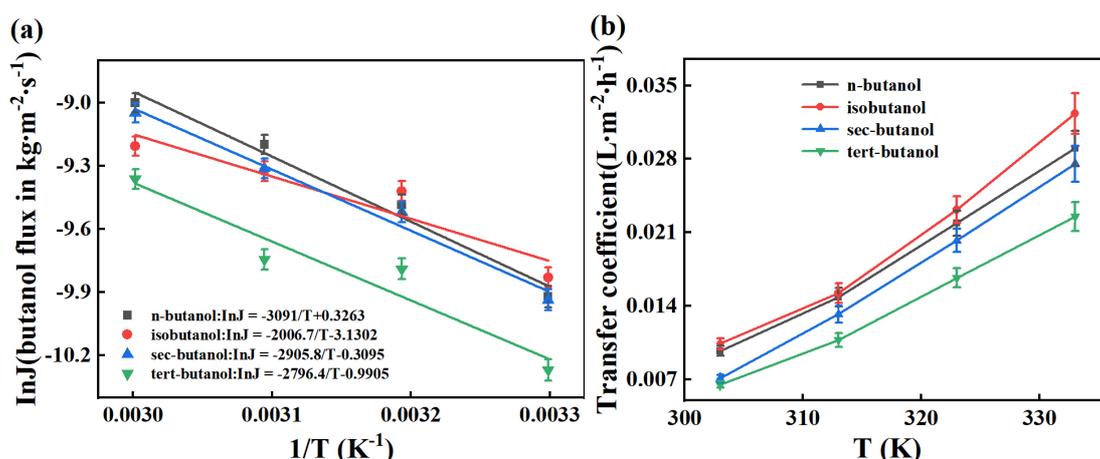
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8 Fig. 9. Effect of feed temperature (binary system) on (a) water flux, (b) butanol flux and (c) separation factor (feed  
9 composition: 2 wt% butanol in water, Vacuum: 0.3 kPa).

10 To observe the energy requirement for mass transfer, the flux of the components corresponding  
11 to the feed temperature fits to the Arrhenitz equation (Fig. 10a). The apparent activation energy of  
12 butanol isomers is listed in Table 1. The apparent activation energy of tert-butanol is the largest,  
13 indicating that higher energy is needed to pass through the PDMS composite membrane [36]. The  
14 final osmotic activation energy of each component is calculated by Eq. (10). When the osmotic  
15 activation energy is negative, the dissolution process dominates the separation process [24]. The  
16 difference in apparent activation energy between butanol isomers may come from the volume  
17 difference and the solubility parameters [34, 37]. By comparing with PE membrane, the mass transfer

1 resistance of PDMS composite membrane is lower than that of PE membranes [32].



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3 Fig. 10. The relation of temperature and flux to fit the Arrhenius formula (a) and total mass transfer coefficient (b)

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(feed composition: 2 wt% butanol in water, Vacuum: 0.3 kPa).

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Table 1. Activation energy of butanol isomers (feed composition: 2 wt% butanol in water, Vacuum: 0.3 kPa).

Component	$\Delta H_v/J \cdot \text{mol}^{-1}$	$E_a/J \cdot \text{mol}^{-1}$	$E_p/J \cdot \text{mol}^{-1}$
N-butanol	43.86	25.7	-18.16
Isobutanol	42.56	16.68	-25.88
Sec-butanol	41.7	24.16	-17.54
Tert-butanol	39.49	23.25	-16.24

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### 3.2.4 Influence of vacuum

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In the PV process, the pressure on the permeate side (degree of vacuum) is much lower than the saturated vapor pressure of each component, thus the solvents vaporize instantly. The influence of the osmotic pressure on the mass transfer of butanol isomers is investigated. With the decrease of vacuum (from 0.3 kPa to 4 kPa), the flux of butanol isomers gradually decreases (Fig. 11), which is consistent with the literature [41]. With the decrease of vacuum, the separation factor of n-butanol decreased but the separation factor of tert-butanol rise [42]. The decrease in the degree of vacuum increases the  $P_f^p$

1 of each component. The saturated vapor pressure of each solvent follows n-butanol<isobutanol<sec-  
2 butanol<tert-butanol (Table S1). The difference in the boiling point of the solvents causes the mass  
3 transfer driving force between the solvents, and thus leads to the difference in the separation factor.  
4 The reduction in vacuum caused the separation factor of n-butanol to drop from 12.1 to 8.9, isobutanol  
5 from 14.3 to 13, tert-butanol increased from 9.4 to 10.3, and sec-butanol unchanged (Fig. 11c). When  
6 the pressure on the permeate side increased from 0.5 kPa to 3 kPa, the separation factor for the n-  
7 butanol/water binary system decreased from 30.5 to 7.4 [43]. When the degree of vacuum is low, the  
8 separation of butanol isomers in the water phase has a limiting effect on high-boiling substances, such  
9 as n-butanol and isobutanol. As the pressure on the permeate side increases, the flux of each  
10 component gradually decreases. Moreover, the separation factor of solvents with a boiling point  
11 higher than water decreases, and the solvents with a boiling point similar to water remains unchanged,  
12 while the solvents with a boiling point lower than water gradually increases.

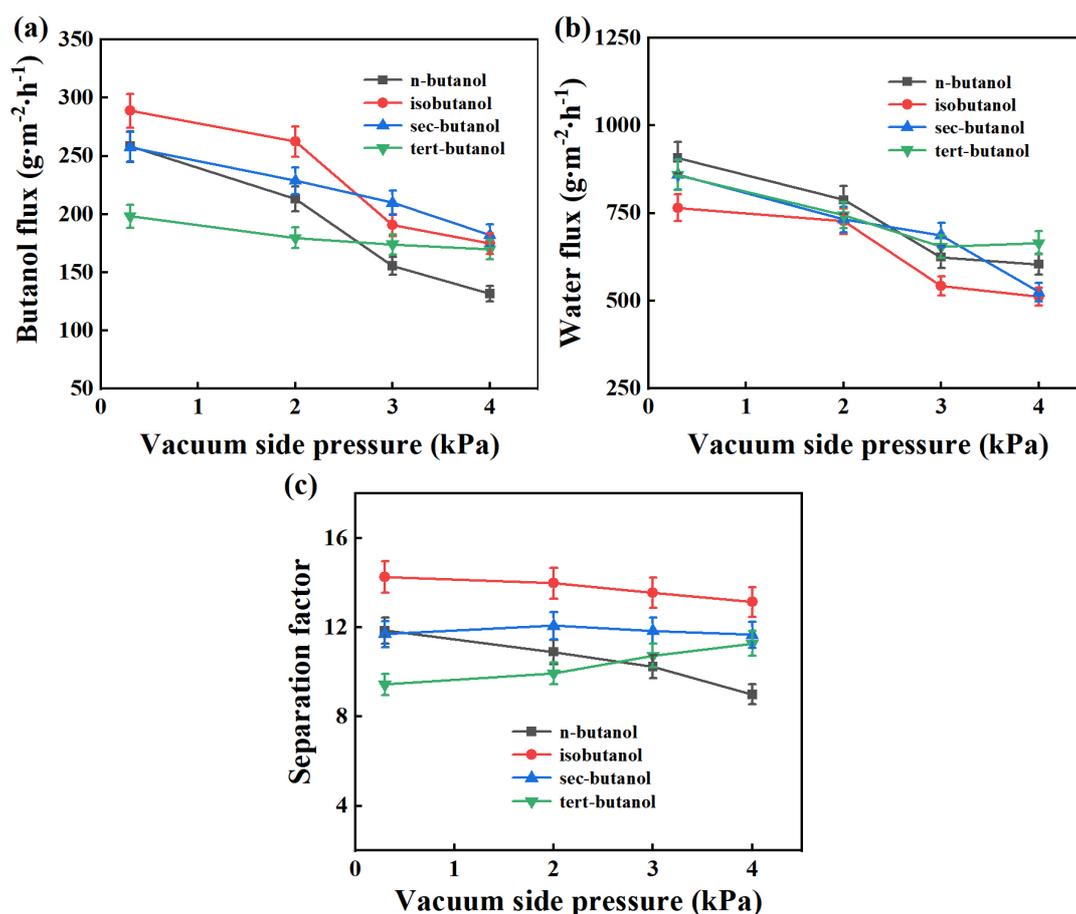
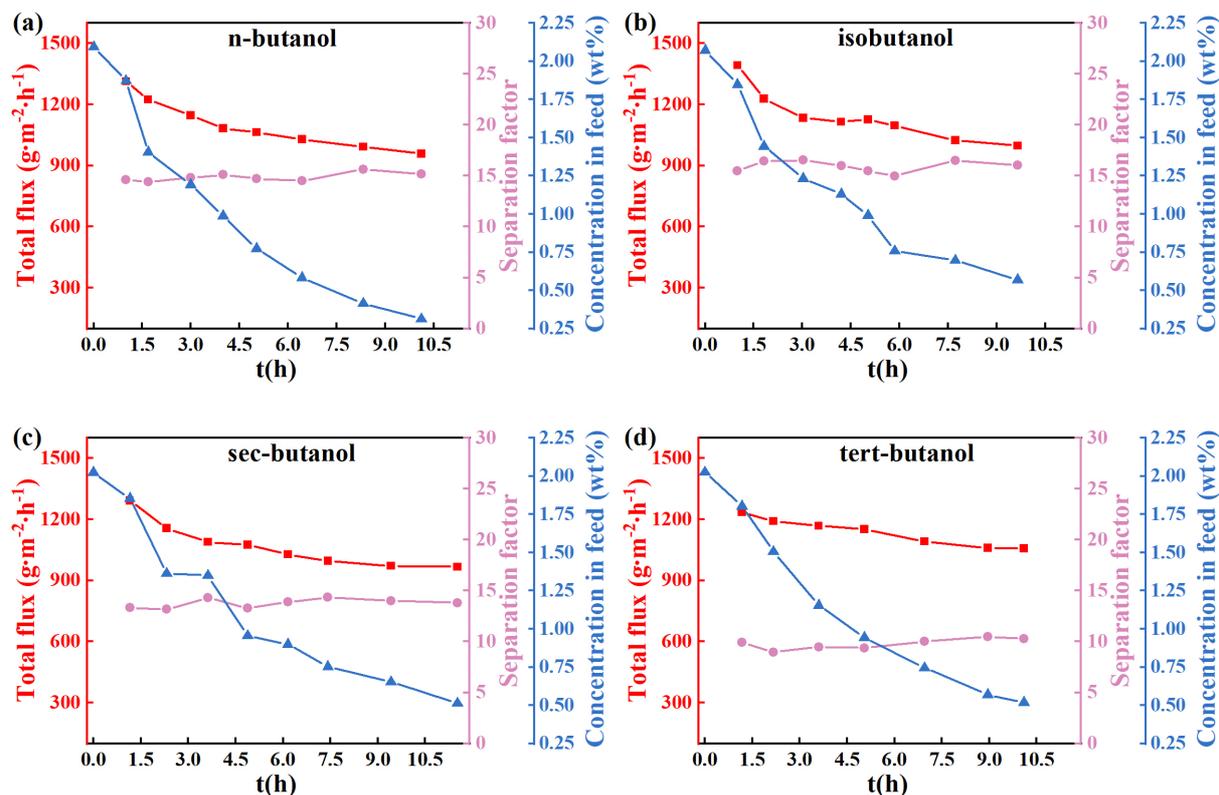


Fig. 11. Effect of vacuum (binary system) on (a) butanol flux, (b) water flux and (c) separation factor (feed composition: 2 wt% butanol in water, feed temperature: 40 °C).

### 3.2.5 Long-term stability and membrane performance comparison

1 Fig. 12 shows the variations of total flux and separation factor with the operation time. 10 h  
2 long-term test of PDMS commercial composite membrane for separating 2 wt% butanol isomers  
3 aqueous solution at 40 °C is performed. It can be observed that the separation factor changed  
4 slightly during the 10 h continuous. In addition, the concentration in feed decreased from 2 wt% to  
5 0.3~0.5 wt%, indicating that the PDMS composite membrane has stable separation performance.



8 Fig. 12. Long-term PV performance of PDMS commercial composite membrane  
9 (feed composition: 2 wt% butanol in water, feed temperature: 40 °C, Vacuum: 0.3 kPa).

10 The pervaporation performance of our PDMS composite membrane is compared with those of  
11 other PDMS membranes reported in the literature as summarized in Fig. S3 and Table S2 (support  
12 information for details). PDMS commercial composite membrane (this study) has a good flux for  
13 butanol/water separation, for instance, the flux of isobutanol/water in literature is 193~210 g·m<sup>-2</sup>·h<sup>-1</sup>,  
14 while the flux of the membrane in this study is 1238.1 g·m<sup>-2</sup>·h<sup>-1</sup>. The pervaporation process shows a  
15 great potential in the application of butanol/water separation.

## 16 4. Conclusions

17 The transmission difference of butanol isomers in the PDMS composite membrane is  
18 systematically studied. As feed concentration increases, the flux of butanol isomers increases and its

1 order follows tert-butanol <sec-butanol <isobutanol <n-butanol. This is consistent with the theoretical  
2 value calculated by the half-time empirical formula. Meanwhile, water flux remains basically  
3 unchanged and has little correlation with its partial pressure. Comparing the binary and ternary  
4 systems, The PV resistance of butanol isomers is concentrated in three steps which based on the series  
5 resistance model: 1) leave the boundary layer; 2) dissolve into the functional layer; 3) diffuse through  
6 the functional layer. Moreover, water molecules have an antagonistic effect on the penetration of  
7 butanol. The separation of butanol isomers in the aqueous solution should combine polarity and  
8 solubility parameters. The separation factors of butanol are n-butanol (14.9), isobutanol (15.5), sec-  
9 butanol (14.4), tert-butanol (10.6).

10 As the temperature rises, the flux of butanol isomers gradually increases while the separation  
11 factors decrease. The permeation activation energy of butanol isomers is n-butanol ( $-18.16 \text{ J}\cdot\text{mol}^{-1}$ ),  
12 isobutanol ( $-25.88 \text{ J}\cdot\text{mol}^{-1}$ ), sec-butanol ( $-17.54 \text{ J}\cdot\text{mol}^{-1}$ ), tert-butanol ( $-16.24 \text{ J}\cdot\text{mol}^{-1}$ ), and the order  
13 is the same as the total mass transfer coefficient. As the pressure on the permeate side increases, the  
14 flux of butanol isomers gradually decreases, the separation factor of n-butanol and isobutanol  
15 gradually decreases, that of sec-butanol is basically unchanged, and that of tert-butanol gradually  
16 rises. This research provides an engineering point of view for PV separation of butanol isomers and  
17 have potential to be applied for separating other solvents with similar properties.

18

## 19 Acknowledgement

20 This work is supported by the National Natural Science Foundation of China (No. 21921006).  
21 We also thank the support of the State Key Laboratory of Materials-Oriented Chemical Engineering  
22 (KL17-04) and THYME project (Research England).

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## 24 Notes

25 The authors declare no competing financial interest.

26

## 27 Supplementary data

28 Supplementary data to this article including physical properties of the components, mass transfer

1 resistance model and membrane performance comparison can be found online at XXX

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## Nomenclature

A	effective area of the membrane, $m^2$
D	diffusion coefficient, $cm^2 \cdot s^{-1}$
$E_a$	apparent activation energy, $J \cdot mol^{-1}$
$E_p$	permeation activation energy, $J \cdot mol^{-1}$
$f_{1,i}$	boundary layer resistance
$f_{2,i}$	PDMS membrane surface resistance
$f_{3,i}$	PDMS membrane internal resistance
$J_0$	pre-exponential factor
$J_i$	flux of component i, $g \cdot m^{-2} \cdot h^{-1}$
$K_{ov}$	total mass transfer coefficient
l	membrane thickness, $\mu m$
$m_i$	weight of component i in the permeate, g
$P_i$	permeability of component i, $g \cdot m^{-2} \cdot h^{-1} \cdot kPa^{-1}$
$P_i^p$	permeate pressure of component i, kPa
$P_i^{sat}$	equilibrium partial vapor pressure of i in the feed, kPa
$R_g$	gas constant, $J \cdot mol^{-1} \cdot K^{-1}$
S	swelling degree
t	permeation time interval for the pervaporation, min
T	kelvin temperature, K
$t_{0.5}$	time when $M_t/M_s$ is 0.5
$V_i$	molar volume of component i, $cm^3 \cdot mol^{-1}$
$W_d, W_t, W_s$	mass of the dry membrane, mass of membrane after t, Saturated swelling mass of membrane, g
$x_i$	weight fractions of components in the feed, wt%
$x_i^f$	mole fraction of i in the feed, mol%
$y_i$	weight fractions of components in the permeate, wt%

$\Delta p$  driving force  
 $\Delta H_v$  enthalpy of evaporation,  $J \cdot mol^{-1}$

## Greek

$\alpha$  separation factor  
 $\beta, \beta_{idea,i,n}$  selectivity and ideal selectivity for isobutanol or sec-butanol or tert-butanol and n-butanol  
 $\gamma_i$  activity of components i  
 $\chi$  interaction parameter  
 $\delta_1, \delta_2$  solubility parameters of PDMS and solvent,  $J^{1/2} \cdot cm^{-3/2}$

## Subscript

PV pervaporation  
PDMS polydimethylsiloxane  
SI support information  
N n-butanol  
I isobutanol  
S sec-butanol  
T tert-butanol  
W water

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