REVIEW

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Anatomical variations of the circle of Willis and their prevalence, with a focus on the posterior communicating artery: A literature review and meta-analysis

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Abstract

The circle of Willis is an anastomotic network of arteries surrounding the base of the brain, providing collateral circulation to prevent ischemia. It has, however, long been established that it exhibits considerable anatomical variation when compared to Thomas Willis' originally described circle. This study aimed primarily to determine an accurate prevalence of the variation of the circle of Willis in the general population and the prevalence of common posterior communicating artery variations. Additional aims were to explain why such a wide range of reported variations exist, and whether different types of studies report significantly different prevalence of variation. A comprehensive literature search identified 764 papers. A three-phase screening process was undertaken, involving a critical analysis of papers, and a total of 33 papers were selected for analysis and literature review. A descriptive statistics test with bootstrap was performed to estimate the average prevalence of variations. The estimated prevalence of general variation, unilateral, and bilateral posterior communicating artery hypoplasia or aplasia was 68.22 ± 14.32%, 19.45 ± 8.63%, and 22.83 ± 14.58%, respectively. Over half of the population exhibit a circle of Willis with some form of variation. To provide a more accurate estimation for the prevalence of variations, a universal classification system needs to be established, collating all the work from high-quality studies, to provide a comprehensive database of the circle's variations. Knowing the prevalence of variations and how they can impact neurosurgical approaches or patterns of ischemic pathology can be crucial in providing effective patient care.

KEYWORDS

cerebral arterial circle, circle of Willis, communicating, hypoplasia, posterior, variation

1 | INTRODUCTION

The circle of Willis (CoW) is an anastomotic arterial network on the base of the brain. Its major role is to provide efficient collateral circulation to cerebral and cerebellar tissue to prevent ischemia, and

subsequent transient ischemic attack or stroke (Karatas, Coban, Cinar, Oran, & Uz, 2015; Karatas, Yilmaz, Coban, Koker, & Uz, 2016; Klimek-Piotrowska et al., 2016). First described in Thomas Willis' landmark work *"Cerebri Anatome"* (Willis, 1664), the CoW is classically described as a symmetrical polygon, derived from anastomoses between

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branches of the internal carotid arteries and vertebral arteries. Modern anatomy textbooks refer to it as a roughly pentagonal circle of vessels on the ventral surface of the brain (Moore, Dalley, & Agur, 2014). It consists of anterior and posterior cerebral arteries, providing arterial supply to the various lobes of the cerebrum and cerebellum. An anterior communicating (AComA) and two posterior communicating (PComA) arteries join these cerebral arteries and help form the collateral arterial network (Moore et al., 2014; Standring & Gray, 2016) (Figure 1).

The CoW is an eponymous term, with several synonyms used throughout the literature. Whilst "circle of Willis" is the most widely utilized term, (and hence, the term used throughout this article), other common synonyms are "*Cerebral Arterial Circle*," or "*Circulus Arteriosus Cerebri*," which are the terms used in Terminologia-Anatomica (Federative Committee on Anatomical Terminology, 1998), and utilized by several studies (Eftekhar et al., 2006; Ardakani et al., 2008). Another synonym within the literature is "Arterial circle of the Brain" (Lazorthes, Santini, & Salamon, 1979).

Since Willis first described it, the CoW has been examined in cadaveric studies and analyses of live patient imaging (LPI), including computed tomography (CT) and magnetic resonance angiography (MRA). Although the CoW, as classically described, is symmetrical, with vessels of an approximately equal diameter bilaterally, it is subject to significant morphological variation. Unfortunately, the multiplicity of anatomical studies of the CoW has not helped to clarify the prevalence of its morphological variation, primarily because of the inconsistency between their outcomes. Studies report a classical CoW to be present anywhere from 4.8% (Fisher, 1965) to 85.4% (Yeniçeri, Çullu, Deveer, & Yeniçeri, 2017) of the population. This wide range of



FIGURE 1 The original Circle of Willis, as described by Thomas Willis in 1664 (Original image). The anterior and posterior cerebral arteries, AComA, and PComA, which are integral to the circle of Willis, are highlighted

reported rates of variation has been proposed as being due to differing methodology or nomenclature between studies (Karatas et al., 2016), ethnic and population discrepancies (DeSilva, Silva, Amaratunga, Gunasekera, & Jayesekera, 2011; Eftekhar et al., 2006; Karatas et al., 2016), and whether a neurologically healthy or diseased population were studied (Kayembe, Sasahara, & Hazama, 1984; Riggs, 1963). The literature can, however, agree on one thing: variation is most commonly seen in the PComA (Riggs, 1963; Fisher, 1965; Lazorthes et al., 1979; Eftekhar et al., 2006,).

For clinicians performing procedures on the CoW, extensive knowledge of its anatomy and potential variations is essential. Understanding common variations, how they impact clinical practice, and the risks of ischemic events are necessary to provide effective and safe care for patients (Zhou et al., 2016).

In this study, a systematic literature review and meta-analysis of published research examining variations of the CoW was performed with the following aims: (a) to suggest a more accurate range for the prevalence of variations of the CoW within the general, neurologically healthy population, (b) to establish an estimated prevalence for the most common types of variation (PComA), (c) to review why such a large discrepancy in the reported prevalence of CoW variation exists, and (d) establish whether a significant difference exists between the results of cadaveric and LPI studies.

2 | MATERIALS AND METHODS

A Medline search was carried out, in July 2017, using two Medical Subject Headings (MeSH). The first related to the CoW, incorporating all used synonyms: "circle of Willis OR Cerebral Arterial Circle OR Circulus Arteriosus Cerebri OR Willis"? circle' ('?' denotes wildcard character). The second related to variations: "varia*OR atypical OR abnormal*OR anomal*OR unusual OR incomplete" ('*' denotes truncation). These search terms were combined with the Boolean operator "AND". This search resulted in 764 studies that underwent a three-phase screening process.

2.1 | Three-phase screening process

A summary of the screening and appraisal process is shown in Figure 2. In Phase One, all studies with the MeSH terms in their titles were selected. The abstracts of all the selected articles were scrutinized, and inclusion and exclusion criteria applied (Table 1). Inclusion criteria included a title referencing the CoW (or synonyms) or variation, and an abstract or title relevant to one of this study's aims. Studies examining *only* fetal specimens or neurologically unhealthy populations were excluded. Exclusion criteria also included case reports, animal studies, or studies focusing on an accessory vessel of the CoW (e.g., recurrent artery of Heubner). One hundred and twenty-nine studies were identified as appropriate for Phase Two screening and were categorized into cadaveric or LPI-based studies, and whether they examined the full or partial CoW



FIGURE 2 A flow diagram summarising the three phase screening process of the literature search, screening and appraisal. (Original image)

	TABLE 1	Inclusion and Exclusion Criteria
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• Title contains a term •	Case reports, editorials and letters Animal studies
 corresponding to MeSH term for 'CoW' or 'variation' Abstract and title deemed relevant to one of the study's aims The study examines a healthy population, or population with cerebral ischemia, or study compares a healthy and diseased population. Paper is available in the English language Paper studied non-fetal specimens/subjects 	Model/computer-generated brain studies Focused on flow patterns or blood distribution patterns Paper focused on a specific examination of an accessory vessel, not in the main CoW (e.g., recurrent artery of Heuber). Fetal studies (with no adult control) Studies comparing imaging or cadaveric preservation methods

rates (van-Raamt, Mali, van-Laar, & van der Graff, 2006), the effect of variations on diseases, such as migraine (Henry et al., 2015), or the use of artificial models of the CoW (Nowinski et al., 2009). Forty-three cadaveric studies and 24 LPI studies were identified as appropriate for Phase Three.

In Phase Three, a detailed analysis of each article was undertaken, and a further 11 cadaveric and 9 LPI studies were excluded, based on a thorough examination against the inclusion and exclusion criteria. For studies examining partial CoWs, only those examining the posterior cerebral arteries or PComA were included (this is the region most commonly exhibiting variation, and examining other specific areas of the circle was beyond the scope of this review).

2.2 | Critical appraisal

The remaining 32 cadaveric and 15 LPI studies underwent a critical appraisal, to assess the quality of research, and to determine whether they were suitable for further review and meta-analysis. The critical appraisal used a bespoke scoring system, based on the Critical Appraisal Skills Programme (CASP) criteria for Cohort and Case-Control Studies (Critical-Appraisal-Skills-Programme, 2017a, 2017b).

In Phase Two, the inclusion and exclusion criteria were applied, whilst reading the introduction, methodology, and conclusion of each article. Studies were excluded for irrelevant focus such as blood flow

Study and location	Sample size	Specimen type and health	Hypoplasia definition	Typical CoW % (n)	Variant CoW % (n)	Hypoplastic PComA % (n)	Aplastic PComA % (n)	Classification system used?	Most common variation
	Cadaveric stud	lies							
(Al-Hussain, Shoter, & Bataina, 2001) (Jordan)	50	No cerebrovascular disease (CeVD)	~1 mm	20% (10)	80% (40)	Overall 33% (33).ª	13% (13).ª	Nun	PComA hypoplasia
(Alpers, 1963) USA	350	Healthy control group	<1 mm	52% (182)	48% (168) •	Unilateral 8%, bilateral 6%	NA	Own	PComA abnormality
(Ardakani et al., 2008) Iran	30	Infants and fetuses, no CeVD.	<0.6 mm	42.1% (12)	57.8% (18)	Unilateral 43% (13) Bilateral 8% (2).ª	Unilateral 19.9% (6) Bilateral 3.3% (1) ^a	Own	PComA hypoplasia
(Battacharji & Hutchinson, 1967) UK	88	Healthy control group.	<1 mm	NA	ΝA	Overall 39% (34).ª	NA	Unknown	PcomA hypoplasia
(DeSilva et al., 2011; DeSilva, Silva, Gunasekera, & Jayesekera, 2009) Sri- Lanka	225	No CeVD	~1 mm	14.2% (32)	85.8% (193)	Unilateral 11.5% (26), bilateral 23% (52)	Ч	Lazorthes	PComA hypoplasia (bilateral)
(Eftekhar et al., 2006) Iran	102	No CeVD	~1 mm	28% (29)	71.6% (73)	Unilateral 27%, bilateral 33%	Unilateral 7%, bilateral 3%	Lazorthes	PComA hypoplasia (bilateral)
(Fisher, 1965) USA	414	Unselected, no exclusion of CeVD	~1 mm	4.8% (20)	95.2% (394) •	Unilateral 6% (24), bilateral 30.4% (126)	AA	NwO	PComA hypoplasia (bilateral)
(Hashemi, Mahmoodi, & Abbas, 2013)Iran	200	No CeVD	~1 mm	34.5% (69)	65.5% (131)	Unilateral 17.5% (37), bilateral 24% (48)	Unilateral 3% (6), bilateral 1% (2)	NwO	PComA hypoplasia (bilateral)
(Kapoor, Singh, & Dewan, 2008) India	1,000	No CeVD	~1 mm	45.2% (452)	54.8% (548)	Unilateral 13.1% (131) Bilateral 3.6% (36)	Unilateral 0.9% (9), bilateral 0.1% (1)	Own	PComA hypoplasia (unilateral)
(Karatas et al., 2016) Turkey	100	No CeVD	~1 mm	8% (8)	92% (92) ^b	Unilateral 24% (24), bilateral 37% (37)	NA	пмО	PComA hypoplasia (bilateral)
(Kayembe et al., 1984) Japan	148	Healthy control group.	~1 mm	46.3% (62)	53.7% (86)	Overall 8.3% (11). ^a	6% (8). ^a	Own	X-ACA
(Klimek-Piotrowska et al., 2016) Poland	100	No CeVD	~1 mm	27% (27)	73% (73)	Unilateral 11% (11), bilateral 16% (16)	AA	Lazorthes	PComA hypoplasia (bilateral)
(Lazorthes et al., 1979) France	200	Unspecified	Not given	14.5% (29)	85.5% (171)	Unilateral 14% (28), bilateral 22% (44)	AA	nwO	PComA hypoplasia (bilateral)
									(Continues)

 TABLE 2
 Summary of studies analyzed. Grey boxes represent values not reported by the study

(Continued)
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Martine trad	nication Most common n used? variation	PComA abnormality	own PComA hypoplasia (bilateral)	PComA hypoplasia	Fetal PComA	PComA hypoplasia		Fetal PComA	Fetal PComA	Fetal PComA PComA hypoplasia/ absence (bilateral)	Fetal PComA PComA hypoplasia/ absence (bilateral) ee- hypoplasia	Fetal PComA PComA hypoplasia/ absence (bilateral) e- hypoplasia hypoplasia/ absence (unilateral)	Fetal PComA PComA hypoplasia/ absence (bilateral) e- hypoplasia/ hypoplasia/ absence (unilateral) thes PComA absence (bilateral)	Fetal PComA PComA hypoplasia/ absence (bilateral) e- hypoplasia/ absence (unilateral) thes PComA absence (unilateral) thes PComA absence (unilateral)
	system u	Own	Unknow	.6%, Own 8%	Own	Own		Own	UMO	uwo O	Own Own Krabbe- Hartk	Own ded Krabbe- Hartk % (15), Own % (5)	Own ded Krabbe- (15), Own % (5) 9.2% Lazorth	own ided Krabbe- % (15), Own % (5) Own % (5) Sun % Sence. Own
Anlastic DCo	n) % (n)	ue NA	AN	Unilateral 15 bilateral 7.	AN	AN		AA	AA	NA ral 42.8%•. Included	NA ral 42.8%•. Included teral 10.5% (18). Inclu	NA ral 42.8%•. Included eral 10.5% (18). Inclu Unilateral 15 bilateral 1	NA ral 42.8%•. Included eral 10.5% (18). Inclu bilateral 15 bilateral 26 bilateral 26	NA ral 42.8%•. Included eral 10.5% (18). Inclu bilateral 15 bilateral 26 bilateral 26 bilateral 26
	Hypoplastic PComA % (I	Overall 27.3% (27) (uniqu classification).	Unilateral 8.9% (88), bilateral 12.7% (126) ^a	Overall 33.3% ^a	Unilateral 18.6%, bilatera 14.3%	Overall 22%		ΥN	٩	NA Unilateral 12.03%, bilate absence.	NA Unilateral 12.03%, bilate absence. Unilateral 10% (17), bilat absence	NA Unilateral 12.03%, bilate absence. Unilateral 10% (17), bilat absence Unilateral 15% (15), bilateral 5% (5)	NA Unilateral 12.03%, bilatel absence. Unilateral 10% (17), bilat absence Unilateral 15% (15), bilateral 5% (5) bilateral 9.20%, bilatera	NA Unilateral 12.03%, bilate absence. Unilateral 10% (17), bilat absence Unilateral 15% (15), bilateral 5% (5) bilatera 4.80% Unilateral 28.7%, bilatera Unilateral 28.7%, bilatera
Worldant CoW	% (n)	42.4% (42) •	80.6% (802)	70.6%	80%	44% •		AN	NA	NA 78.70%	NA 78.70% 67.8% (116)	NA 78.70% 67.8% (116) 72% (72)	NA 78.70% 67.8% (116) 72% (72) 83.2%	NA 78.70% 67.8% (116) 72% (72) 83.2% 58%
Tomical Cow	(n) %	57.6% (57)	19.2% (192)	29.4%	20%	56%		NA	۲Z	NA 21.30%	NA 21.30% 32.2% (55)	NA 21.30% 32.2% (55) 28% (28)	NA 21.30% 32.2% (55) 28% (28) 16.8%	NA 21.30% 32.2% (55) 28% (28) 16.8% 42%
-ila	definition	<1 mm	Not given	~1 mm	~1 mm	Not given		<0.5 mm	<0.5 mm	<0.5 mm <0.8 mm	<0.5 mm<0.8 mm<0.8 mm	 <0.5 mm <0.8 mm <0.8 mm <1 mm 	 <0.5 mm <0.8 mm <0.8 mm <1 mm <1 mm Not given 	 <0.5 mm <0.8 mm <0.8 mm <0.8 mm <0.8 mm <0.8 mm
Customer three and	specimen type and health	No CeVD	Neural dysfunction	Unspecified	No CeVD	Meningitis and atherosclerosis	excluded	excluded No CeVD, male- only	No CeVD, male- only	No CeVD, male- only 3D-TOF-MRA, no CeVD	No CeVD, male- only 3D-TOF-MRA, no CeVD MRA and MRI neurological patients	No CeVD, male- only 3D-TOF-MRA, no CeVD MRA and MRI neurological patients CTA. No CeVD.	No CeVD, male- only 3D-TOF-MRA, no CeVD MRA and MRI neurological patients CTA. No CeVD.	No CeVD, male- only 3D-TOF-MRA, no CeVD MRA and MRI neurological patients CTA. No CeVD. CTA. No CeVD. CTA. No CeVD. 3D-TOF-MRA. Some neurologically unhealthy.
	Sample size	66	994	51	70	50		56	56 LPI studies	56 LPI studies 507	56 LPI studies 507 171	56 LPI studies 507 171 100	56 LPI studies 507 171 100 250	56 LPI studies 507 171 100 250 250 150
	Study and location	(Papantchev et al., 2007) Bulgaria	(Riggs, 1963) USA	(Siddiqi, Tahir, & Lone, 2013) Pakistan	(Saikia, Handique, Phukan, Lynser, & Sarma, 2014) India	(Idowu, Malomo, & Akang, 2010) Nigeria		(Saha, Sarkar, & Mandal, 2015) India	(Saha, Sarkar, & Mandal, 2015) India	(Saha, Sarkar, & Mandal, 2015) India (Chen et al., 2004) Taiwan	(Saha, Sarkar, & Mandal, 2015) India (Chen et al., 2004) Taiwan (El-Barhoun, Gledhill, & Pitman, 2009) Australia	(Saha, Sarkar, & Mandal, 2015) India (Chen et al., 2004) Taiwan (El-Barhoun, Gledhill, & Pitman, 2009) Australia (Karatas et al., 2015) Turkey	(Saha, Sarkar, & Mandal, 2015) India (Chen et al., 2004) Taiwan (El-Barhoun, Gledhill, & Pitman, 2009) Australia (Karatas et al., 2015) Turkey (Klimek-Piotrowska et al., 2013) Poland	(Saha, Sarkar, & Mandal, 2015) India (Chen et al., 2004) Taiwan (El-Barhoun, Gledhill, & Pitman, 2009) Australia (Karatas et al., 2015) Turkey (Klimek-Piotrowska et al., 1998) (Krabbe-Hartkamp et al., 1998) Netherlands

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Most common variation	PComA hypoplasia/ absence (bilateral)	PComA hypoplasia/ absence	PComA hypoplasia/ absence (bilateral)	PComA hypoplasia/ absence (bilateral)	Fetal PComA	PComA hypoplasia (unilateral)	PComA hypoplasia, unilateral	ieine: NA. no data
Classification system used?	чмо	NMO	Chen's (2004, Taiwan, above)	чмо	Own	Own	Own	enetic resonance ima
Aplastic PComA % (n)	14.4% (17). Includes		ncludes absence	47.5% ^b (1066).	Unilateral 1.4% (1), bilateral 7.1% (5)	NA	NA	aneiography: MRI. ma
4ypoplastic PComA % (n)	Jnilateral 12.7% (15), bilateral 1 absent	Overall 30%, includes absent.	Jnilateral 9%, bilateral 32.7%. I	Inilateral 22.8% (512), bilateral Includes absence	Jnilateral 20% (14), bilateral 11.4% (8)	Jnilateral 26.7% (40), bilateral 8.7% (13)	Jnilateral left only: 35.6%	. computerized tomography
Variant CoW % (n)	53%	58.5%	83.4% (250)	92.43% •	75.72%	NA	58.6%	ascular disease: CTA
Typical CoW % (n)	47%	41.5%	16.6% (50)	7.57% (170)	24.28% (17)	AN	41.4%	CeVD. cerebrov
Hypoplasia definition	×0.8 mm	Not given	×0.8 mm	Dependent on artery average	~1 mm	Not given	~1 mm	ce angiography:
Specimen type and health	3D-TOF-MRA. Healthy older patients	3D-TOF-MRA. Infants, no CeVD.	3D-TOF-MRA. Neuroischemia referrals.	3D-TOF-MRA and MRI. No CeVD	3D-TOF-MRA. No CeVD.	MRA. No CeVD	CTA, no CeVD.	eht magnetic resonan
Sample size	118	65	300	2,246	70	150	250	A. 3D time of fli
Study and location	(Macchi et al., 2002) Italy	(Malamateniou et al., 2009), UK	(Naveen, Bhat, & Karthik, 2015) India	(Qiu, Zhang, Xue, Jiang, & Zhang, 2015) China	(Saikia, Handique, Phukan, Lynser, & Jamil, 2014) India	(Voljevica & Kapur, 2005) Bosnia	(Papantchev et al., 2013) Bulgaria	Abbreviations: 3D-TOF-MR,

available. Ab

^aResults did not clearly state whether they were reporting PComA hypoplasia/aplasia as the only variation, or as hypoplasia/aplasia and the presence of another, separate variation (co-variation). ^bResult is considered an extreme value, outside the SD of the present study.

The CASP criteria were modified to make them more relevant to this review and to focus on specific elements, such as the inclusion of specific definitions of the classical CoW, and the provision of specific definitions for hypoplastic vessels. Studies were further scored in six separate categories: addressing a clearly-focused issue, appropriate methodology, appropriate subject/specimen recruitment, minimization of bias and confounding factors, clear reporting of results, and acknowledgment of limitations. A score of >15 out of 24 points was required for a study to undergo further analysis and review. Papers scoring 15 or less were considered to have a less robust methodology or less reliable results. Studies scoring >15 underwent a reference screen to identify other potentially relevant studies, of which the inclusion and exclusion criteria were then applied. One study (Gunnal, Faroogui, & Wabale, 2014) was found in the reference screen, but scored <15 and was excluded. The previously mentioned study that reported 85.4% (Yeniçeri et al., 2017) prevalence of a classical CoW did not score sufficiently highly on the critical appraisal and thus was not included in the analysis.

Three papers, by Riggs, 1963, Fisher (1965) and Lazorthes et al. (1979) scored <15 on the critical appraisal, but were still included in the literature review on the basis that their work is heavily referenced throughout the literature, and are considered landmark studies of CoW anatomy. Notably, Lazorthes et al. (1979) created a well-known classification system of variant CoWs. Hence, it was considered inappropriate to exclude these studies from the literature review. However, since they do not explicitly meet the inclusion criteria, their findings were interpreted with caution and excluded from the meta-analysis.

2.3 | Extracted data

Twenty cadaveric studies, 12 LPI studies, and one study utilizing both cadavers and LPI (Papantchev et al., 2013) passed critical appraisal and underwent a literature review. However, only 17 cadaveric, 12 LPI, and one combined cadaveric and LPI study underwent metaanalysis, following exclusion of Riggs, 1963, Fisher (1965), and Lazorthes et al. (1979), as described above. From each paper, data were extracted and recorded (Table 2), including sample size and the overall percentage prevalence of typical and variant CoWs. The estimated prevalence of PComA variations was also recorded (hypoplasia or aplasia). Some studies reported the prevalence of PComA hypoplasia and aplasia as separate values, and these were combined for analysis, allowing comparison between studies.

2.4 | Statistical analysis

To establish an estimated prevalence of variation, all data underwent descriptive statistical testing, with a 5,000 bootstrap. A comparison of sample sizes against the reported prevalence of variation was analyzed for clusters and outliers to determine if there was a reported sample size above which results may be considered reliable.

Independent samples *t*-test was performed on IBM SPSS Statistics (2015), to establish whether there was a significant difference in the prevalence of variation reported in cadaveric or LPI studies.

3 | RESULTS

Thirty-three studies were included in the final review and analysis. Riggs (1963), Fisher (1965) and Lazorthes et al. (1979) were included in the literature review by reputation but were excluded from the meta-analysis, on the basis that they did not meet the minimum score on the critical appraisal. Studies examined were published between 1965 (Fisher, 1965) and 2016 (Karatas et al., 2016; Klimek-Piotrowska et al., 2016), with sample sizes ranging from 30 (Ardakani et al., 2008) to 2,246 (Qiu et al., 2015). Definitions of a hypoplastic vessel varied between studies: some defined it as a vessel <1 mm diameter (n = 18) and others did not provide a definition (n = 6). The extracted data are summarized in Table 2.

Scatter graphs were created to illustrate the differences in the reported prevalence of variant CoWs in general (Figure 3), and the prevalence of both unilateral (Figure 4) and bilateral (Figure 5) hypoplastic or aplastic PComAs. It was not possible to estimate the minimum sample size a study would need to produce results considered reliable, due to a wide range of reported prevalence and no clear clusters appearing in the scatter graphs. Thus, no study was excluded based on their sample size. The smallest was 30 and this could be considered as a reasonable lower boundary for future work in this field.

3.1 | Prevalence of general variation of the CoW in a neurologically healthy population

Twenty-six studies reported the prevalence of a variant CoW in their sample (Figure 3), ranging between 42.4% (Papantchev et al., 2007) to 95.2% (Fisher, 1965). No significant difference was found between the reported prevalence of variation in cadaveric and LPI studies, t (26) = -0.981, p = .25. Therefore, the reported prevalence from both cadaveric and LPI studies was analyzed together. The average (mean) prevalence of variation of the CoW within a healthy population was 68.22% ± 14.32% (SD). The most frequently reported prevalence of variation was in the range of 71-80% (n = 8); 88.5% of studies analyzed reported the prevalence of a variant CoW as >51%.

3.2 | Prevalence of PComA variation (hypoplasia and aplasia)

Nineteen studies were included in the analysis to determine the prevalence of unilateral and bilateral PComA hypoplasia or aplasia (Figures 4 and 5). Only studies that reported PComA hypoplasia or aplasia as the only variation (i.e., not coexisting with other variations) were included. This ensured that the cases of PComA described could be reliably considered similar and comparable. The examination of FIGURE 3 Prevalence of a variant form of the Circle of Willis (n = 26). Variation is reported between approximately 42% and 92%, and a wide range of reported prevalence of variation can be seen. Cadaveric and LPI studies overlap, and no obvious difference can be seen between them



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FIGURE 4 Prevalence of unilateral PComA hypoplasia (n = 19). A wide range of prevalence of hypoplasia is reported, from approximately 8% to 28%. Cadaveric and LPI studies overlap, and no obvious difference can be seen between them



CoWs with multiple variations was beyond the scope of the present study. Both the prevalence of hypoplasia and aplasia were combined into a single value to allow comparison between studies that reported them as such.

The range of prevalence of unilateral PComA hypoplasia or aplasia (Figure 4) reported was 8% (Alpers, 1963) to 28.7% (Klimek-Piotrowska et al., 2013). There was no significant difference between the reported prevalence in cadaveric and LPI studies (t[17] = -0.74, p = .72), thus their data were analyzed together. The mean prevalence of unilateral PComA hypoplasia and aplasia was 19.45% ± 8.63%. The modal group was 10.1–15%, (n = 6).

The range of prevalence of bilateral PComA hypoplasia and aplasia (Figure 5) reported was 3.7% (Kapoor et al., 2008) to 47.5% (Qiu et al., 2015). There was no significant difference between the prevalence reported in cadaveric and LPI studies, (t[17] = -0.68),

p = .124) thus their data were analyzed together. The mean prevalence of bilateral PComA hypoplasia or aplasia was 22.83% ± 14.58%. The range of prevalence reported was widely distributed (Figure 5), and no clear modal group could be defined.

Differences between the results of cadaveric 3.3 and LPI studies

As highlighted above, independent samples t-tests showed no significant difference between the prevalence of variation reported in cadaveric and LPI studies, in general variation or PComA variation. On visual examination of the scatter graphs (Figures 3, 4, and 5), there is a significant overlap between the two types of study, with no discernible pattern or correlation between them.



FIGURE 6 Variations of the Circle of Willis examined in this study, and their prevalence following meta-analysis. A: "Normal" CoW, with no variations, present in 31.78 ± 14.32%. B(1): Unilateral PComA hypoplasia, B(2): Unilateral PComA aplasia. Together, the prevalence of B(1) and B (2) was 19.45 ± 8.63%. C(1): Bilateral PComA aplasia, C(2): Bilateral PComA hypoplasia. Together, the prevalence of C(1) and C(2) was 22.83 ± 14.58%. Note how C(1) and C(2) may completely sever communication between the anterior and posterior halves of the CoW

4 | DISCUSSION

4.1 | Prevalence of general variation of the CoW

It is clear from the literature that variations of the CoW are very common (68.22% \pm 14.32). For clinicians treating ischemic attacks, strokes, and aneurysms, understanding potential variations is crucial. For example, clinicians treating aneurysms need to be aware that the anatomy is highly likely to exhibit some variation from Willis' originally described circle.

Standard anatomy textbooks often acknowledge that the CoW is highly variable (Moore et al., 2014; Standring & Gray, 2016), noting that there is some variation in approximately 50% of the population (DeSilva et al., 2011). Here, a meta-analysis of the highest quality studies, following screening and critical appraisal, has been performed, and other well-reputed studies (Fisher, 1965; Lazorthes et al., 1979; Riggs, 1963) have been considered whilst reviewing the literature. Whilst the range of reported prevalence of general variation found is wide (42%–92%), descriptive statistics suggest that the average mean prevalence of a variant CoW is $68.22\% \pm 14.32$, in a healthy population.

The results of this review, therefore, find variation is likely to be present in well over half of the general population. The modal reported prevalence 71–80% (30.8% studies) (Figure 3) and 53.84% (n = 14) of the studies analyzed suggest a prevalence of 68.22% or above, and this increases the confidence that the prevalence of a variant CoW is likely to be much higher than currently thought (~70%). Figure 6 displays illustrations of the variations examined in this meta-analysis.

With this in mind, it should be strongly emphasized in standard textbooks and anatomical teaching that Willis' original circle is somewhat unlikely to be encountered. For clinicians commonly performing procedures on the CoW, or for anatomists examining it, an awareness of this is essential to help them prepare to encounter unusual or unfamiliar anatomy.

4.2 | Prevalence of variation of the PComA

Despite the wide range of reported prevalence of general variation, most authors agree the PComA is the vessel most likely to display variation. In the final analysis, 96.88% of studies (Table 2) reported PComA as the most frequently anomalous vessel. This meta-analysis suggests that PComA hypoplasia/aplasia is present unilaterally in 19.45% \pm 8.63, and bilaterally in 22.83% \pm 14.58 of the population.

Clinically, PComA hypoplasia and aplasia are very significant. The PComA is essential for connecting the anterior and posterior halves of the CoW. A non-patent or non-existent PComA may compromise the ability of the CoW to provide collateral circulation. In this study, bilateral hypoplasia/aplasia was shown to be more common than unilateral, although there was a much wider range of reported prevalence (Figure 5). Clinically, however, this variation is particularly significant: the two halves of the CoW could be anatomically and functionally isolated from each other with no communication between the internal carotid system and vertebrobasilar system. This is illustrated particularly in Figure Six (images C1 and C2). In a condition such as internal carotid artery stenosis, cerebral circulation may rely on collateral blood supply from the vertebrobasilar system. Without a functioning PComA, it is possible that the route for collateral circulation may be compromised, and could contribute to ischemic pathology. (Karatas et al., 2016; Saikia, Handique, Phukan, Lynser, & Sarma, 2014). Whilst some individuals could potentially develop other collateral circulation in the case of a non-functioning PComA, this is highly variable among individuals, and the ability to develop collaterals in pathological conditions (such as ischemic stroke) is not uniform.

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Having repeated the literature search at the time of publication, a further relevant cadaveric study, meeting inclusion criteria was found (Cilliers, Vorster, & Page, 2018). This study reported that in 39 cadavers, a variant circle (defined as different to Lazorthes' type 1) (Lazorthes et al., 1979) was present in 59% specimens. Unilateral PComA hypoplasia was present in 23.1% and bilateral hypoplasia in 10.3%. Cilliers et al.'s (2018) results are in tandem with the other studies examined in this analysis and aligned with the statistical results (Figures 3 and 4).

4.3 | Clinical applications of variations of the CoW, particularly the PComA

Being familiar with the most common CoW variations and their prevalence can be of vital importance to clinicians. Many authors have suggested an increased risk of ischemic stroke in the presence of CoW variations (Chuang, Liu, Pan, & Lin, 2008; Hoksbergen et al., 2003; Mukherjee, Jani, Narvid, & Shadden, 2018). Chuang et al. (2008), for example, highlight that hypoplasia of the PComA is associated with an increased risk of infarction, particularly in the thalamic region. Understanding the anatomy of common variations and their prevalence can help us predict the likelihood of patients suffering a stroke, and which regions are likely to be affected. In the absence of traditional risk factors for stroke, such as ICA stenosis, it would be feasible to consider whether an anatomical variation is the CoW is the causative factor.

Mukherjee et al. (2018) suggest that variant CoW anatomy can have an impact on the trajectory of microemboli, and hence lead to infarctions in distal, more unusual areas of the brain. Therefore, being aware of variations and their frequency can help us understand atypical stroke patterns, and predict their likelihood. If a specific variation, of which the prevalence is known, was associated with a particular stroke pattern, it would be possible to predict the likelihood of this stroke pattern occurring.

For neurosurgeons managing aneurysms, being aware of the potential variations in anatomy is essential. Additionally, being aware of their prevalence may also be of crucial importance. Considering, for instance, the prevalence of PComA hypoplasia of approximately 19.45% unilaterally and 22.83% bilaterally, if an aneurysm treatment modality involved vessel sacrifice of one of the PComAs, or relied on

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one or both of the PComAs to provide collateral circulation throughout the procedure, knowing the likelihood of the variant anatomy could be incredibly useful. It would allow a surgeon to assess the risk of a particular approach, and consider the likelihood of the need for an alternative approach, once the patient is undergoing surgery. Having this prior knowledge can assist a surgeon in becoming better prepared for procedures, and more likely to have prepared an alternative approach, in the case of variant anatomy. Furthermore, understanding which variations are common and their prevalence can help inform clinicians as to whether an endovascular or surgical approach is least likely to disturb the blood supply.

4.4 | Large discrepancies in the reported prevalence of CoW variation exists, and wide ranges of results

This analysis produced a very wide range of results in all domains studied (Figures 3–5). As a result, the estimated prevalence showed large *SD*. Differences in methodology and nomenclature are likely to account for the large range of results seen throughout the literature. Four main reasons have been identified for this wide range.

Firstly, studies on the variability of the CoW have been undertaken using heterogeneous methods. Cadaveric studies used a variety of dissection techniques, and LPI studies ranged between using 3D Time-of-Flight MRA (3D-TOF-MRA) and CT Angiography (CTA). As discussed below, no significant difference was found between cadaveric and LPI studies. Furthermore, a variety of sample sizes have been used throughout the research, ranging from 30 to 2,246 (Table 2), and it was not possible to identify an appropriate sample size for exclusion in the present study. Hence, with a variety of methods and sample sizes being used, it is unsurprising that variation exists between studies.

Secondly, nomenclature varies between studies, particularly with regards to the definition of a hypoplastic vessel. Throughout the literature, various definitions have been used (Table 2), with <1 mm the most commonly used (56.25%), particularly in cadaveric studies. Several other studies have used <0.8 mm to define a hypoplastic vessel (15.63%), appearing more frequently in LPI studies. 18.75% of studies analyzed failed to provide any definition for a hypoplastic vessel (Table 2). With differing definitions throughout the literature, it is likely that what one study considered a hypoplastic vessel was not considered hypoplastic by another. If a study was using <0.8 mm as the definition, for example, they will have excluded vessels 0.8–1.0 mm diameter, which others may have considered hypoplastic, and this may have falsely decreased their overall reported prevalence of hypoplasia.

Thirdly, different classification systems have been used to categorize variations, throughout the literature. Lazorthes et al. (1979) describe 22 separate variant CoWs, whilst Krabbe-Hartkamp et al. (1998) describe 10 anterior and 10 posterior CoW variations. Some authors have used or adapted these systems (Table 2) when describing their findings. However, 46.88% of studies in this review did not use any established classification system. With different studies using different or no classification systems, a comparison is difficult and reduces confidence that two studies describe the same variation and are truly comparable.

Finally, population differences in anatomy likely exist. Studies have been performed on five continents, and it is reasonable to expect variation in the frequencies of anatomical variants between populations. Interestingly, PComA hypoplasia/aplasia was reported as particularly high in Chen et al.'s (2004), Li et al.'s (2011) and Qiu et al.'s (2015) studies, all performed in a similar region of Asia (Table 2). Hence, some differences in prevalence are likely to be due to population-specific anatomical variation.

4.5 | Differences between cadaveric and LPI studies

There is no statistically significant difference between the results of cadaveric and LPI studies. On visual examination of the scatter graphs (Figures 3, 4, and 5), the results of different study types overlap, and there is no discernible pattern or correlation between them.

Throughout the literature, authors have suggested cadaveric and LPI studies should not be compared and analyzed together for several reasons (Klimek-Piotrowska et al., 2016; Li et al., 2011). Cadaveric studies examine vessels that have undergone formalin fixation or other preserving methods, during which vessel diameters may change and fail to represent the true dimensions of the vessel (Li et al., 2011: Saikia, Handigue, Phukan, Lynser, & Sarma, 2014), as blood is not actively flowing through them, as would be in an LPI study. Thus, cadaveric and LPI studies may give different results. Furthermore, cadaveric studies allow direct visualization of the vessels in situ (Qiu et al., 2015); such access is impossible in CTA or 3D-TOF-MRA studies. Despite this, the results of the present study show that no statistically significant difference exists between the results of the highest quality studies. Hence, for this review, it was considered appropriate to combine the two types of study for descriptive statistics, but the results should be interpreted with a degree of caution.

4.6 | Future directions and recommendations

The outcome of this review is that the prevalence of CoW variation, in general, is $68.22\% \pm 14.32$, (range 53.9%-82.54%) with confidence that it is likely to be considerably over 50%. The results show the most frequently reported prevalence of variation was in the range of 71-80% (n = 8), whilst 88.5% of studies analyzed reported the prevalence of a variant CoW as >51%. However, to produce a more accurate estimate for the prevalence of variations, and to improve understanding of the types of variation and their frequency, a comprehensive classification system needs to be established and adhered to in future studies.

It is, therefore, pertinent that a universally accessible database is created, collating all current, high-quality research. Such a database

should be created from an expert consensus, of anatomists who have extensive experience studying the area. The consensus should also involve clinicians, with regular, ongoing experience managing relevant conditions, such as stroke and aneurysms, to ensure the resulting classification is of clinical relevance. This database would include known variations of the CoW, their estimated prevalence, and a clear definition for each. This would also include an agreed definition for hypoplasia, preferably <1 mm, as this has been most widely used throughout the literature analyzed (Table 2). All future research could henceforth refer to this database to describe their results, unifying the reporting and comparison of CoW variations and prevalence. In doing so, the true prevalence of variation will likely be found.

Such a database could also be referred to by clinicians to whom the anatomy is relevant, to familiarize themselves with unusual anatomy, and to increase awareness of new variations and changes in patterns of prevalence.

It is also recommended that when teaching the anatomy of the CoW, in both undergraduate and postgraduate settings, several points should be emphasized. Firstly, it should be highlighted that the CoW commonly displays variability, with considerably over 50% of the population showing some form of variation. Additionally, the areas most commonly exhibiting variation, such as the PComA should be emphasized. Furthermore, the clinical application of these variations, such as their relevance to stroke patterns, embolus distribution, or aneurysm treatment approaches should be highlighted and considered in tandem with anatomical teaching. The depth of discussion of all of these areas should, of course, depend on the audience and their expected knowledge level.

4.7 | Limitations

It was not possible to determine an appropriate cut off value for the sample size of studies. Papers examining smaller sized samples (i.e., <200) may have statistically unreliable results, which may have impacted on the results of the meta-analysis. If more high-quality studies were available, a sample size cut-off may have been established.

The searching, review and appraisal of the studies considered in this review were carried out by a single investigator, raising the potential for observer bias. The critical appraisal grading scheme was assessed by two independent experts (a University Academic and a Consultant Neurosurgeon.)

5 | CONCLUSIONS

The CoW is a network of arteries surrounding the base of the brain, providing collateral circulation to prevent ischemic pathology. Variations from the originally described model of the CoW are common, with the present study estimating variant CoWs to be present in 68.22% \pm 14.32%. Variations are most commonly seen in the PComA, with unilateral and bilateral hypoplasia or aplasia present in 19.45% \pm 8.63% and 22.83 \pm 14.58% of the neurologically healthy population respectively.

To provide more accurate and precise estimates for the prevalence of variations, it is suggested that a universal classification system of known variations is created and used in all future studies of CoW anatomy. Within this classification system, an agreed definition of a hypoplastic vessel should be established; for instance, <1 mm. Understanding the prevalence of variations and how they can impact pathology may help lead to more effective prevention and treatment of such conditions.

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