

Utilisation of CO₂ as “Structure Modifier” of Inorganic Solids

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Utilisation of CO₂ as a chemical reagent is challenging, due to the molecule's inherent chemical stability. However, CO₂ reacts promptly at high temperature (~1000 °C) with alkaline-earth oxides to form carbonates and such reactions are used towards capture and re-utilisation. In this work, this concept is extended and CO₂ is utilised as a reagent to modify the crystal structure of mixed-metal inorganic solids. Modification of the crystal structure is a “tool” used by materials scientists to tailor the physical property of solids. CO₂ gas was reacted with several isostructural mixed-metal oxides Sr₂CuO₃, Sr_{1.8}Ba_{0.2}CuO₃ and Ba₂PdO₃. These oxides are carefully selected to show anion vacancies in their crystal structure, to act as host sites for CO₂ molecules, leading to the formation of carbonate anions, (CO₃)²⁻. The corresponding oxide carbonates were formed successfully and the favourable formation of SrCO₃ as secondary phase was minimised via an innovative, yet simple synthetic procedure involving alternating of CO₂ and air. We also derived a simple model to predict the kinetics of the reactions for the cuprates, using first-principles density functional theory and assimilating the reaction to a gas–surface process.

Introduction

Materials are at the core of our ever more high-technology society, with the impact of new materials discovery felt throughout on a daily basis. Inorganic materials in particular, have their role in many innovative applications and thus discovery of new inorganic materials has allowed access to new technologies. For example, inorganic materials with semiconducting properties started the computer revolution and now are investigated as photocatalytic materials for environmental applications, superconducting materials could be part of future energy saving plans and are currently key components in Magnetic Resonance Imaging (MRI) instrument and quantum computers. A wide range of imaginative synthetic routes has led not only to brand new chemical classes but also to the modification of structure and properties of known materials in order to target specific applications. In this work, we propose the use of CO₂ gas as a tool to modify the structure of selected materials. If such synthetic route is established among materials chemists, it will offer an additional approach to the synthesis of inorganic materials with the benefit of utilising a gas normally considered harmful to the environment. Increasing concerns have risen over the link between CO₂ emissions and rising global temperatures.^[1,2]

Interaction of inorganic solids with CO₂ gas is being considered in relation to CO₂ capture and utilisation.^[3] Zeolites and metal organic frameworks (MOFs) for example have porous structures which allow them to store quantities of CO₂ gas from emissions, mostly *via* physisorption.^[4–7] Alkaline earth metal oxides MO (M = Ca and Mg) have also been investigated for the capture CO₂ *via* the formation of metal carbonates MCO₃.^{[8],[9]} CO₂ reacts

readily with alkaline earth metal oxides to form carbonates, due to the strong affinity of the M–O bonds for CO₂.

In this work, we extend the use of CO₂ for the formation of binary carbonates to the use of CO₂ as reagent to modify the crystal structures of mixed-metal oxides. To obtain a proof-of concept for our method, we have chosen a class of materials, which contain alkaline earth metals and show vacancies in their crystal structures. These vacancies act as hosts for the CO₂, which then binds to one oxide within the structure to form a carbonate. This process leads to the formation of oxide-carbonates as well as a structural rearrangement, leading to different compounds (oxide-carbonates) with a different crystal structure, albeit related to that of the starting material.

Compounds with general formula A₂BO₃ (A = metal 1, B = metal 2) or AO(ABO₃)_n show anion vacancies. Their crystal structures relate to the n=1 series of Ruddlesden–Popper phases, A₂BO₄, containing 1 perovskite-type layer (ABO₃) interleaved by 1 NaCl-type layer (AO). The anion-deficiency in A₂BO₃ compounds when compared with the A₂BO₄ series, derives from the absence of the two equatorial oxide anions in the coordination sphere of transition metal B. In A₂BO₃ (A = Ca, Sr, Ba; B = Cu, Pd) the B cation is coordinated by the oxide anions in a square planar manner with each B–O square linked to another via one of its corners to form linear 1D chains (Figure 1). The anion vacancies, which are used as “host sites” for CO₂ molecules, are ordered along these chains. A₂BO₃ (A = Ca, Sr, Ba; B = Cu, Pd) compounds have been used as “hosts” for extra anions and, as a consequence, a structural rearrangement had taken place. Oxide insertion in Sr₂CuO₃ was carried out by Lobo *et al.* using high pressure O₂ gas and resulted in the formation of the Sr₂CuO_{3+x} series with superconducting properties.^{[10],[11]} The crystal structure changed from orthorhombic to tetragonal.

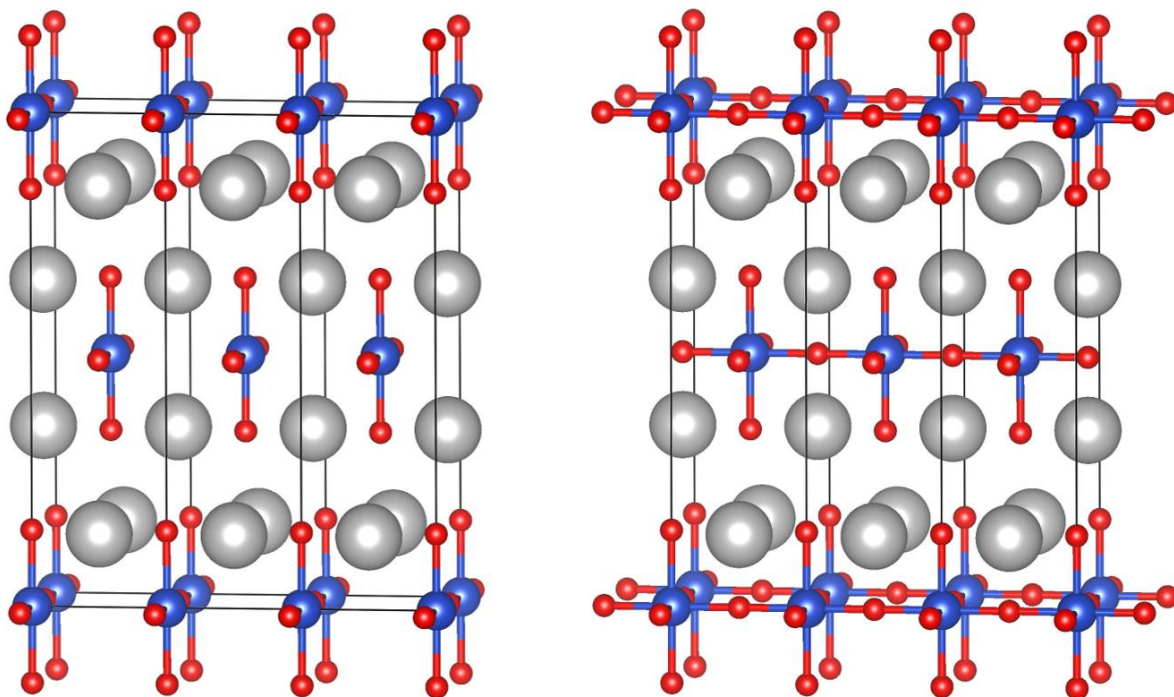


Figure 1: The crystal structure of A_2BO_4 left, and A_2BO_3 , right with $A = \text{Ca, Sr, Ba}$ and $B = \text{Cu, Pd}$. The silver spheres represent the cation A and the red spheres represent the anions O_2 . The blue squares are the B cation, blue spheres with the B - O coordination bonds showing either square planar or octahedral coordination.

Extensive research was carried out on the fluoride insertion/substitution in Sr_2CuO_3 and led to formation of the oxide-fluoride, $\text{Sr}_2\text{CuO}_2\text{F}_{2+\delta}$, ($0 \leq \delta \leq 0.35$).^[12,13] In the fluorination of Sr_2CuO_3 towards $\text{Sr}_2\text{CuO}_2\text{F}_{2+\delta}$, 1 oxide anion was replaced by 2 fluorides and extra fluoride anions were inserted into the interstitial sites within the crystal structure. The coordination of the copper cation changed from 4, in Sr_2CuO_3 , to 6, in $\text{Sr}_2\text{CuO}_2\text{F}_{2+\delta}$, due to the increased anion number. The crystal system also changed from body centred orthorhombic to primitive tetragonal and the extra fluoride anion, δ , caused a $2+/3+$ mixed oxidation state of the copper cation as charge compensation mechanism. The structure of $\text{Sr}_2\text{CuO}_2\text{F}_{2+\delta}$ is classified as an anion-deficient La_2CuO_4 -type (K_2NiF_4 -type) structure. In practice, the fluorination process “filled up” the anion vacancies. Within this series, the compound $\text{Sr}_2\text{CuO}_2\text{F}_{2.3}$ ($\delta \approx 0.3$) shows high T_c superconductivity ($T_c \sim 46 \text{ K}$).

Compounds of general formula $\text{Sr}_{2-x}\text{Ba}_x\text{CuO}_3$, derived from Sr_2CuO_3 via isovalent substitution of Sr^{2+} with Ba^{2+} were also fluorinated and led to the formation of oxide-fluorides adopting the “full” K_2NiF_4 -type structure.^[13–15]

Ba_2PdO_3 is isostructural to Sr_2CuO_3 and was reported to undergo fluorination to form the oxide-fluoride $\text{Ba}_2\text{PdO}_2\text{F}_2$.^[16,17] The coordination of Pd^{2+} remains square planar, but, instead of one-dimensional chains of Pd-O squares, there are two-dimensional planes of Pd-O squares in $\text{Ba}_2\text{PdO}_2\text{F}_2$. The structure of $\text{Ba}_2\text{PdO}_2\text{F}_2$ is classified as a Nd_2CuO_4 -type structure.

In this work we use these finding on anion insertion in A_2BO_3 ($A = \text{Ca, Sr, Ba}$; $B = \text{Cu, Pd}$) to obtain a proof-of-concept that CO_2 gas can be hosted within the vacancies of the crystal

structure and give oxide carbonates, as well as inducing a structural rearrangement related to those observed for the fluorination of these materials.

Specifically, here, we obtained $\text{Sr}_2\text{CuO}_2(\text{CO}_3)$, $\text{Sr}_{1.8}\text{Ba}_{0.2}\text{CuO}_2(\text{CO}_3)$, $\text{Sr}_{1.75}\text{Ca}_{0.25}\text{CuO}_2(\text{CO}_3)$ and $\text{Ba}_{11}\text{Pd}_{11}\text{O}_{20}(\text{CO}_3)_2$ via the insertion of CO_2 in the respective starting oxides Sr_2CuO_3 , $\text{Sr}_{1.8}\text{Ba}_{0.2}\text{CuO}_3$, $\text{Sr}_{1.5}\text{Ca}_{0.5}\text{CuO}_3$ and Ba_2PdO_3 .

Furthermore, we investigate the kinetic constants of the reactions between A_2CuO_3 ($\text{A} = \text{Ca}, \text{Sr}, \text{Ba}$) and CO_2 . We also formulate a simple computational model that relies on insights gained from the reaction of the corresponding metal oxides (AO) with CO_2 to form carbonates. Those have been previously investigated using theoretical methods for both surface^[18,19] and bulk calculations^[20,21].

Experimental

Preparation of $\text{Sr}_{2-x}\text{A}_x\text{CuO}_3$ ($\text{A} = \text{Ca}$ and Ba)

The preparation of Sr_2CuO_3 was carried out *via* a high temperature ceramic method using polycrystalline ACO_3 ($\text{A} = \text{Sr}, \text{Ba}$ and Ca) (98.5% BDH GPR), and CuO (96.0% BDH GPR).^[22] All reagents were stored in an oven at approximately 100 °C to prevent moisture contamination. The reagents were mixed in a stoichiometric ratio with acetone to produce a dispersed homogenous mixture. This mixture was then placed into an aluminium crucible that was inserted into a box furnace and heated to 1000 °C for 14 hours in static air. Intermediate regrinding and reheating cycles were performed until high purity products (> 99%) were achieved. $\text{Sr}_{1.5}\text{Ca}_{0.5}\text{CuO}_3$ was prepared via the same procedure as Sr_2CuO_3 except with the reagent mixture compressed into pellets before being heated. $\text{Sr}_{1.8}\text{Ba}_{0.2}\text{CuO}_3$ was prepared in the same way as $\text{Sr}_{1.5}\text{Ca}_{0.5}\text{CuO}_3$ except that it was heated under O_2 gas. These high-purity oxides were then reacted with CO_2 gas.

Preparation of Ba_2PdO_3

Ba_2PdO_3 was prepared *via* a two-step heating process. Firstly, PdO and BaCO_3 (99% Lancaster) were mixed in a stoichiometric ratio with acetone to produce a dispersed homogenous mixture. This mixture was firstly heated to 700 °C for 12 hours to allow PdO to react with BaO , as well as to prevent PdO reducing to Pd metal.^[23] Afterwards a second heating cycle at 1150 °C for 50 hours was carried out.

Reactions with CO_2

All the reactions between the solid compounds and CO_2 gas were carried out in a thermal gravimetric analysis (TGA) instrument, to monitor the reaction in-situ. Pre-weighted samples of A_2BO_3 ($\text{A} = \text{Sr}, \text{Ba}$ and $\text{B} = \text{Pd}, \text{Cu}$) were placed into an alumina crucible then inserted into the TGA furnace chamber. The samples were initially heated to 1000 °C under compressed air (O_2/N_2 mixture). The temperature was then maintained at 1000 °C for 2 minutes to reach equilibrium before the gas flow was changed to pure CO_2 . After a 15-minute isotherm at 1000

°C, the gas flow was switched back to compressed air for the samples to cool to room temperature.

The TGA instrument was a Mettler Toledo TGA/DSC 1 Star System and a GC100 gas controller, which showed the weight of the sample changing at different temperatures and gases. All gas flow rates were maintained at a value of 100 ml/min and the temperature ramp rate was at 100 °C/min. The overall change in weight from the reaction, was determined from the difference between the samples weight at 1000 °C under air, to the weight of the sample after the reaction with CO₂. The procedure used to calculate the (CO₃)²⁻ content in Sr₂CuO₂(CO₃) was based on the ratio of the starting mass to that of the residue mass. The accuracy of the TGA balance is given at ± 0.005 mg.

Powder X-Ray Diffraction

Powder X-Ray Diffraction (PXRD) was performed on a PANalytical Empyrean Series 2 Diffractometer operating CuK_{α1} ($\lambda = 1.54056 \text{ \AA}$) radiation. Samples were scanned using an automatic slit at a step size of 0.026° and a net time per step of 304.2 s at a power setting of 40 kV and 30 mA. A 2 θ range of 5-80° was used. For collection of data to be used for Rietveld refinements, the scan range was carried out from 5-120° with a 1/4° fixed slit at a step size of 0.026° and a net time per step of 1221.45s using a power setting of 45 kV and 40 mA. Subsequent analysis was performed either in HighScore Plus 1 using the PDF-2 2012 database of powder patterns.^[24] The GSAS suite of programs via the EXPGUI software was used for Rietveld refinements.^[25,26] The background was initially modelled using the Cosine Fourier series with twelve terms. The multi-term Simpson's rule integration of the pseudo-Voigt was used in order to model the peaks shapes within the pattern.^[27,28]

Theoretical approach to study the solid-gas reactions

The theoretical modelling of the interaction between CO₂ and the AO (A = Ca, Sr and Ba) surfaces was carried out using the ORCA suite of programs (version 3.0.3).^[29] The Perdew-Burke-Ernzerhof (PBE) exchange correlation functional was used with a resolution of identity approximation for the Coulomb interactions.^[30,31] The valence electrons were represented with a triple zeta valence polarised def2-TZVP basis set along with a compatible def2-TZVP/J auxiliary basis set.^[32,33] The TightOpt criteria implemented in ORCA was used to stop the geometry optimization at a total energy change of $1 < 10^{-6} \text{ Eh}$, respectively. Dispersion forces for each system were included using the Becke-Johnson damping D3BJ method.^[34,35] A surface model of the AO (A = Ba, Ca and Sr) oxides were prepared using the first top two layers of the reported crystal structures.^[36] Figure 2 shows a representation of the AO surface consisting of 18 atoms prepared from the original AO crystal structure.

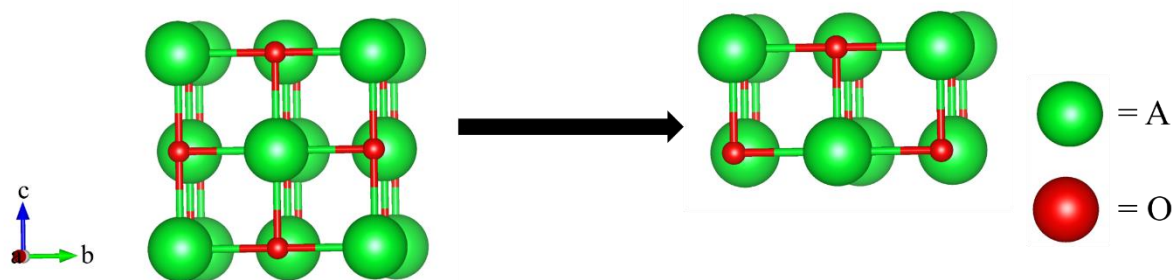


Figure 2: The crystal structure of an AO compound (A = Ca, Sr and Ba) is on the left, with the reduced cluster on the right.

All AO metal oxides considered have a NaCl type structure. To obtain the required binding energy values and optimised structures, a CO₂ molecule was placed over the metal oxide and allowed to optimise towards forming a carbonate. All calculations were performed on the high-performance computer (HPC), Viper, at the University of Hull.

Results and Discussion

Reaction between Sr₂CuO₃ and CO₂

In this work, Sr₂CuO₃ was chosen as a paradigm starting material for “hosting” CO₂ in the vacancies of its crystal structure to lead to Sr₂CuO₂(CO₃), in order to demonstrate that CO₂ can be used as a reagent to modify the composition and crystal structure of materials. In this case, the starting materials are oxides, which, via direct reaction with CO₂, give oxide carbonates. The crystal structure of the parent and the resulting compounds are closely related. Sr₂CuO₂(CO₃) was originally reported by Babu *et al.* as an intermediate during the formation of Sr₂CuO₃ from SrCO₃ and CuO.^[37] Later, Miyazaki *et al.* prepared a purer phase by reacting SrCO₃ and CuO with varying mixtures of O₂ and CO₂ gases at varying pressures.^[38]

We aimed at studying the feasibility of CO₂(g) as a reagent to prepare inorganic solids. Therefore, we chose a known starting oxide and a known product but altered the synthesis procedure in order to focus on a direct reaction between the starting oxide and CO₂(g). We carried out direct reactions of Sr₂CuO₃ with CO₂(g) under several different conditions to identify the route leading to the purest Sr₂CuO₂(CO₃). In the first sets of reactions the reaction temperature was varied between 500 and 1000 °C and the dwell time from 5 to 120 minutes. All the steps (heating, dwell and cooling) were carried out under CO₂ gas and the products were mixtures of SrCO₃, and Sr₂CuO₂(CO₃). The formation of SrCO₃ as secondary phase seemed to occur in all the reactions trialled at different temperatures. In particular, the formation of SrCO₃ seems to start at the beginning of the process, during the heating step.

To minimise the formation of the secondary phase, SrCO₃, the heating step was carried out under an air flow instead of CO₂. CO₂ gas was then introduced in the dwell step once the reaction temperature had been reached. In the cooling step, the gas was then switched back to air, again to minimise formation of SrCO₃. Thermo Gravimetric Analysis (TGA) was used to monitor the reaction of CO₂ with Sr₂CuO₃. The reaction was determined to occur when a weight increase appeared in the TGA graph (Figure 3). This weight increase shows uptake of CO₂ and starts at T = 1000 °C (Figure 3). After trialling several reaction times, the dwell step was

determined to be $T = 1000\text{ }^{\circ}\text{C}$ for 15 minutes. TGA shows that the sample has taken up 16% CO_2 by weight.

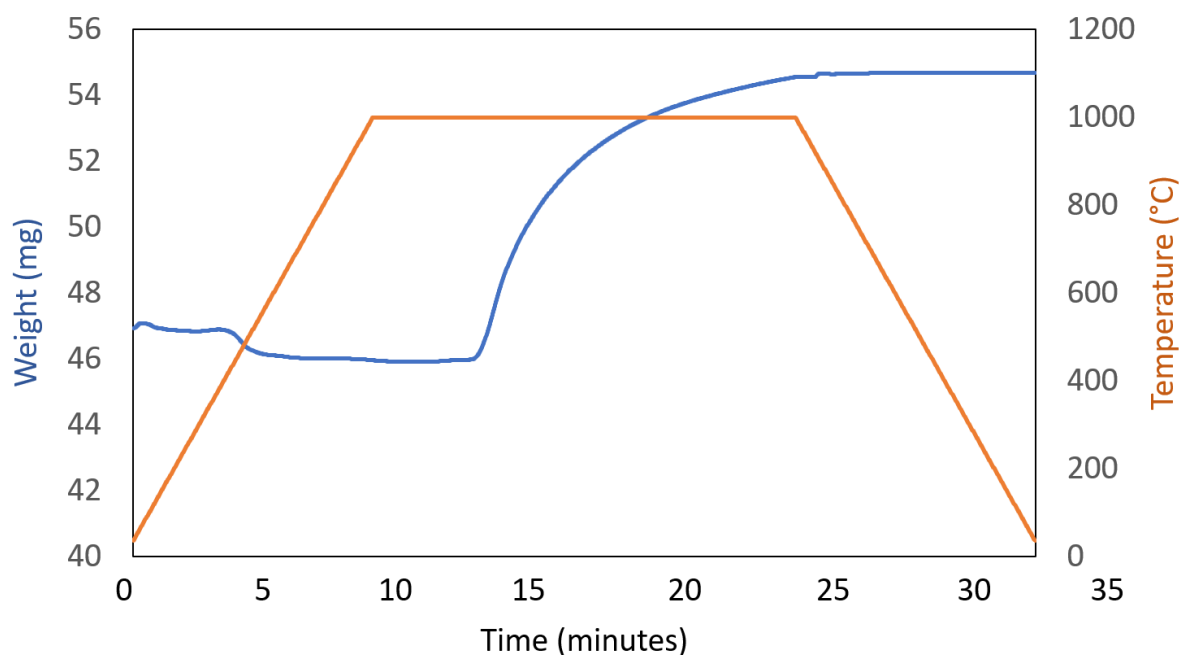


Figure 3: TGA curve showing an increase in the weight of the sample Sr_2CuO_3 as CO_2 is introduced at $1000\text{ }^{\circ}\text{C}$ forming $\text{Sr}_2\text{CuO}_2(\text{CO}_3)$.

PXRD patterns showed that $\text{Sr}_2\text{CuO}_2(\text{CO}_3)$ was the main phase with small amounts of SrCO_3 impurity. A two-phase refinement of PXRD data was carried out, using the structural model of $\text{Sr}_2\text{CuO}_2(\text{CO}_3)$ by Babu *et al.*^[37] ($P4/mmm$ $a = 3.9033(2)\text{ \AA}$; $c = 7.4925(4)\text{ \AA}$) and model by Antao *et al.* for SrCO_3 .^[39] The PXRD pattern resulting from Rietveld refinement is shown in Figure 4 a. The unit cell parameters, $a = 3.903(4)\text{ \AA}$; $c = 7.497(1)\text{ \AA}$, are in agreement with the literature, the R values are $R_p = 12.4\%$, $R_{wp} = 17.6\%$.^[37] The weight percentages of $\text{Sr}_2\text{CuO}_2(\text{CO}_3)$ and SrCO_3 are $85.5(\pm 0.1)\%$ $\text{Sr}_2\text{CuO}_2(\text{CO}_3)$ and $14.6 \pm 0.2\%$ SrCO_3 . Structural data are included in Supplemental Information (Table S1).

The presence of SrCO_3 clearly indicate a degree of decomposition of Sr_2CuO_3 during the reaction with CO_2 , however, we could not find sufficiently clear evidence of a copper-containing secondary phase. We can only infer that a small percentage of copper-containing secondary phase is present but could not be detected by PXRD, possibly because of reactivity with moisture resulting in broadening of the diffraction peaks.

A structural rearrangement accompanies the formation of $\text{Sr}_2\text{CuO}_2(\text{CO}_3)$. The CO_2 molecule form a carbonate anion via a bond with an oxide anion belonging to the SrCuO_3 structure. The carbonate anion is located in the crystal structure vacancies and this induces a structural rearrangement which the unit cell transitioning from the orthorhombic crystal system to the tetragonal one. The unit cell of $\text{Sr}_2\text{CuO}_2(\text{CO}_3)$ is shown in the insert of Figure 4 (top right).

The structural rearrangement occurring here is reminiscent of that identified for the fluorination of Sr_2CuO_3 to $\text{Sr}_2\text{CuO}_2\text{F}_{2+\delta}$.^[13]

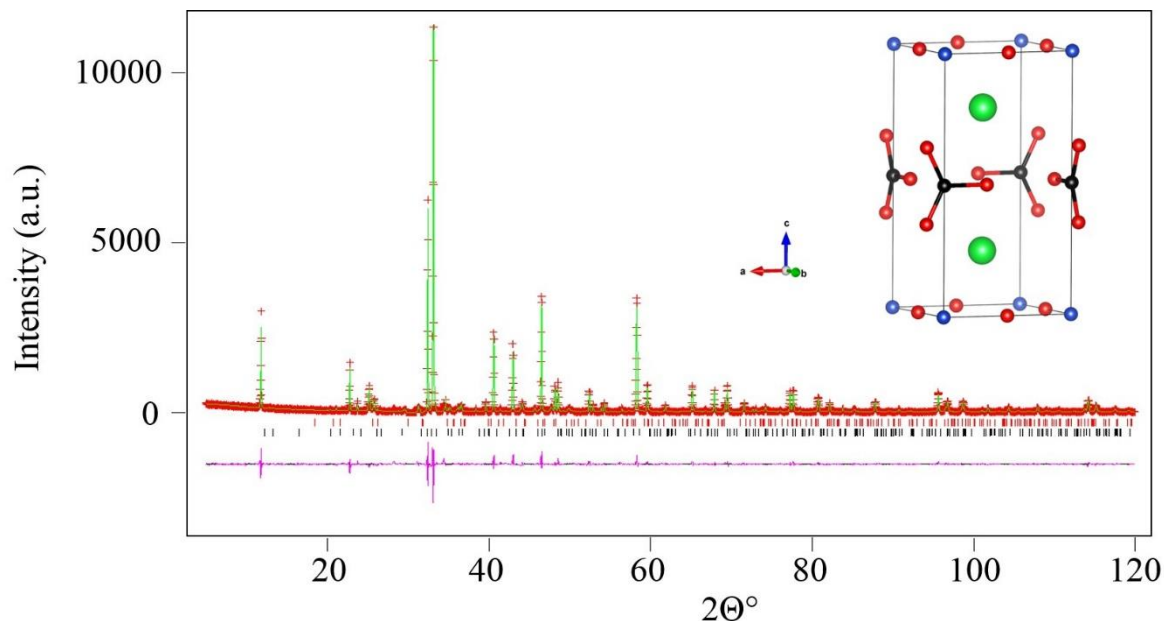


Figure 4: Rietveld refinement profile for $\text{Sr}_2\text{CuO}_2(\text{CO}_3)$, showing the observed (red crosses), calculated (green) and difference (purple) patterns. The reflections belonging to SrCO_3 are marked with (*) and the red ticks. Inset: Crystal structure of $\text{Sr}_2\text{CuO}_2(\text{CO}_3)$. The green spheres represent Sr^{2+} cations, the blue spheres Cu^{2+} cations and the red spheres O^{2-} anions.

To test a more general applicability for the use of CO_2 as “structure modifier”, we chose other mixed-metal compounds with stoichiometry and crystal structure related to Sr_2CuO_3 , i.e. Ca_2CuO_3 , $\text{Sr}_{1.8}\text{Ba}_{0.2}\text{CuO}_3$ and Ba_2PdO_3 .

Reactions of Ca_2CuO_3 , $\text{Sr}_{1.5}\text{Ca}_{0.5}\text{CuO}_3$ and $\text{Sr}_{1.8}\text{Ba}_{0.2}\text{CuO}_3$ with CO_2

Ca_2CuO_3 (*Immm*, $a = 12.25(2)$, $b = 3.789(8)$ and $c = 3.259(3)$ Å)^[40] was reacted with CO_2 in the same conditions as Sr_2CuO_3 , however no formation of oxide-carbonate was obtained. The reason for this lack of reactivity may be found in the difference in the size of the vacancies between Sr_2CuO_3 and Ca_2CuO_3 . In fact, the size of the anion vacancies in Sr_2CuO_3 is $3.50(2)$ Å (based on the distance between the Cu atoms in the b direction), whereas the size of the anion vacancies in Ca_2CuO_3 is approximately $3.25(1)$ Å. The kinetic diameter of CO_2 is 3.3 Å^[41] hence the anion vacancies in Ca_2CuO_3 may prove too small to host the CO_2 molecule. $\text{Ca}_2\text{CuO}_2(\text{CO}_3)$ was actually reported in the literature but its preparation required extreme conditions including a high pressure of 6 GPa, at 1300 °C and a AgO flux.^[42]

To explore this hypothesis, we modified the size of the anion vacancies in Sr_2CuO_3 via isovalent substitutions. Specifically, $\text{Sr}_{1.5}\text{Ca}_{0.5}\text{CuO}_3$ was selected as a prototype sample to show anion vacancies smaller than those in Sr_2CuO_3 and $\text{Sr}_{1.8}\text{Ba}_{0.2}\text{CuO}_3$ as a prototype sample to show anion vacancies larger than those in Sr_2CuO_3 .

$\text{Sr}_{1.5}\text{Ca}_{0.5}\text{CuO}_3$ was reacted 15, 60 and 90 minute at 1000 °C under CO_2 . The PXRD pattern for the 90-minute reaction showed that a $\text{Sr}_2\text{CuO}_2(\text{CO}_3)$ -type phase had formed, however other phases were present, specifically SrCO_3 and SrCaCuO_3 . A three-phase Rietveld refinement was carried out.^[43,44] In the refinements the model of $\text{Sr}_2\text{CuO}_2(\text{CO}_3)$ reported by Babu et al. was used for the calcium-copper oxide carbonate. The calcium content was initially set at $x = 0.5$ to reflect the stoichiometric ratio of the reagents.

For the refinement the background was modelled using the Cosine Fourier series with twelve terms. The multi-term Simpson's rule integration of the pseudo-Voigt was used in order to model the peaks shapes within for all phases.^[45,46] The parameters refined were: the cell parameters and the scale factors for all three-phases. The U_{iso} and the atomic coordinates for the strontium and calcium were constrained with each other when refined. The Lorentzian anisotropic strain broadening was also refined as well. The fractional occupancy between the strontium and calcium was also refined within the oxide carbonate phase. The refinement of the occupancies showed that the formula of the sample was actually $\text{Sr}_{1.75}\text{Ca}_{0.25}\text{CuO}_2(\text{CO}_3)$. This is possibly due to the formation of the secondary phase containing Sr, Ca and Cu for which the refinement of the strontium and calcium occupancies gave a 1:1 stoichiometric ratio hence the SrCaCuO_3 formula. The refinement is shown in Figure 5.

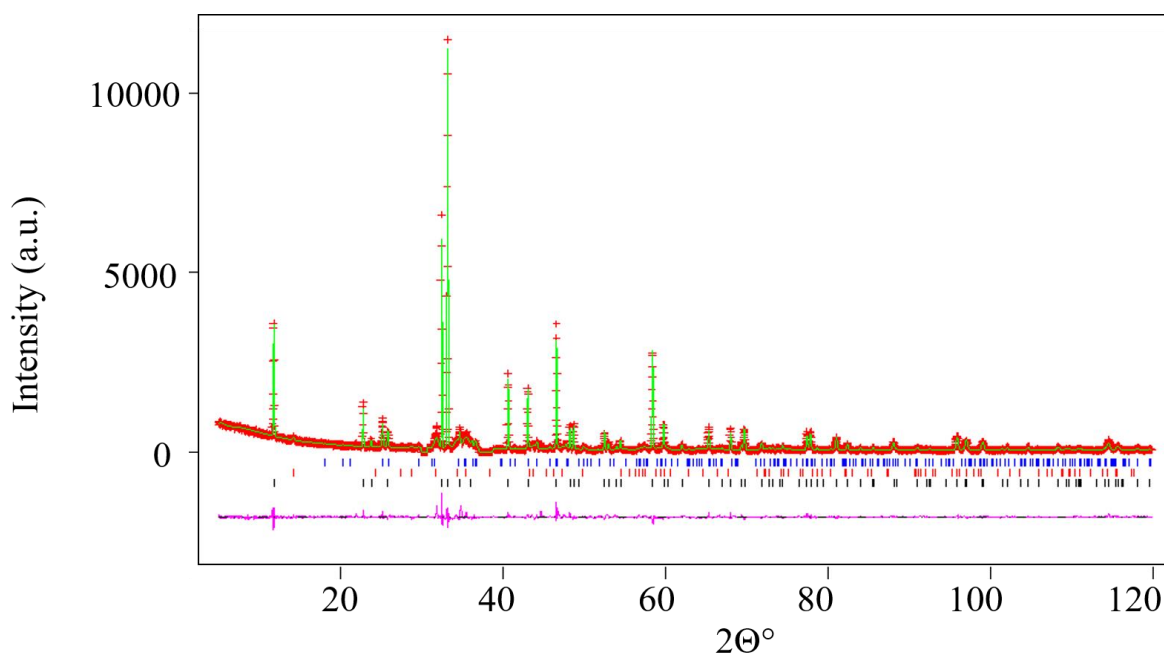


Figure 5: Rietveld refinement profile of $\text{Sr}_{1.75}\text{Ca}_{0.25}\text{CuO}_2(\text{CO}_3)$ obtained from a 90-minute reaction of $\text{Sr}_{1.5}\text{Ca}_{0.5}\text{CuO}_2(\text{CO}_3)$ under CO_2 . This shows the observed (red crosses), calculated (green) and difference (purple) patterns. The ticks represent $\text{Sr}_{1.75}\text{Ca}_{0.25}\text{CuO}_2(\text{CO}_3)$ (black), SrCaCuO_3 (red) and SrCO_3 (blue).

The R-values for this refinement were determined as $R_{\text{wp}} = 12.9\%$ and $R_p = 9.3$. The structural data of $\text{Sr}_{1.75}\text{Ca}_{0.25}\text{CuO}_2(\text{CO}_3)$ has also been presented in the Supplemental Information, Table S2. The size of the anion vacancies in $\text{Sr}_{1.75}\text{Ca}_{0.25}\text{CuO}_2(\text{CO}_3)$ is 3.44(3) Å (based on the distance between the Cu atoms in the b direction), hence larger than that in Ca_2CuO_3 is 3.25(1) Å.

$\text{Sr}_{1.8}\text{Ba}_{0.2}\text{CuO}_3$ shows a larger unit cell than $\text{Sr}_2\text{CuO}_2(\text{CO}_3)$, due to the substitution of 10% of the Sr^{2+} cations with the larger Ba^{2+} cations, hence larger vacancies in the crystal structure. $\text{Sr}_{1.8}\text{Ba}_{0.2}\text{CuO}_3$ was obtained as single phase via solid state reaction and Rietveld refinement of the occupancies of the Sr^{2+} and Ba^{2+} cations, confirmed that 10 % molar substitution of Ba^{2+} for Sr^{2+} has occurred (Figure 2 Supplemental Information). $\text{Sr}_{1.8}\text{Ba}_{0.2}\text{CuO}_2(\text{CO}_3)$ was prepared via the reaction of $\text{Sr}_{1.8}\text{Ba}_{0.2}\text{CuO}_3$ with CO_2 , following the same procedure devised for Sr_2CuO_3 . The PXRD pattern showed that the main phase is $\text{Sr}_{1.8}\text{Ba}_{0.2}\text{CuO}_2(\text{CO}_3)$ oxycarbonate, with SrCuO_2 and SrCO_3 as secondary phases. A three-phase Rietveld refinement was performed using the model by Babu *et al.* for $\text{Sr}_2\text{CuO}_2(\text{CO}_3)$, the one by Antao *et al.* for SrCO_3 , and the model by Lines *et al.* for SrCuO_2 is shown in figure 6. Rietveld refinement data are summarised in Table S3, in the Supplemental Information.^{39,41,42}

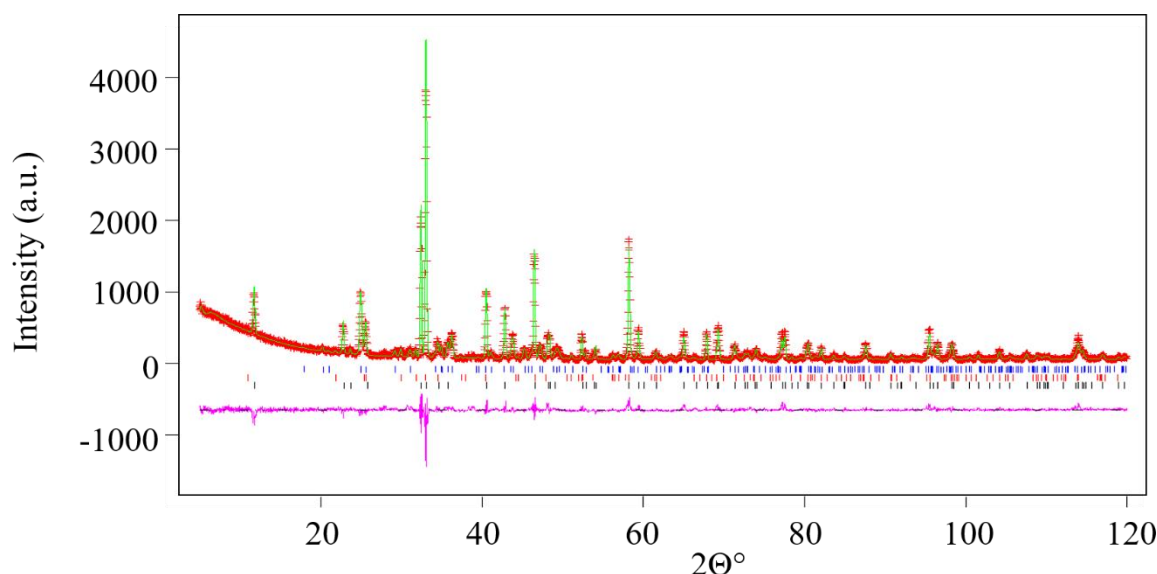


Figure 6: Rietveld refinement profile of $\text{Sr}_{1.8}\text{Ba}_{0.2}\text{CuO}_2(\text{CO}_3)$ showing the observed (red crosses), calculated (green) and difference (purple) patterns. The ticks represent $\text{Sr}_{1.8}\text{Ba}_{0.2}\text{CuO}_2(\text{CO}_3)$ (black), SrCuO_2 (red) and SrCO_3 (blue).

The lattice parameters were refined as $a = 3.90924(5) \text{ \AA}$, $c = 7.53570(2) \text{ \AA}$, $V = 115.162(3) \text{ \AA}^3$ and the R-values of $R_{\text{wp}} = 11.3 \%$ and $R_p = 8.4 \%$. The structural data of $\text{Sr}_{1.8}\text{Ba}_{0.2}\text{CuO}_2(\text{CO}_3)$ has also been presented in the Supplemental Information, Table S3. The size of the anion vacancies in $\text{Sr}_{1.8}\text{Ba}_{0.2}\text{CuO}_2(\text{CO}_3)$ is $3.53(2) \text{ \AA}$ (based on the distance between the Cu atoms in the b direction), hence larger than that in Sr_2CuO_3 is $(3.50(2) \text{ \AA})$.

Kinetics of formation for oxide-carbonates

Using the change in mass over time provided by the TGA curves (Figure 3), we can determine the order of reaction for the direct reaction between the starting oxides and CO_2 gas, as well as reaction rate, k . We performed this determination for the formation of $\text{Sr}_2\text{CuO}_2(\text{CO}_3)$, $\text{Sr}_{1.8}\text{Ba}_{0.2}\text{CuO}_2(\text{CO}_3)$ and $\text{Sr}_{1.5}\text{Ca}_{0.5}\text{CuO}_2(\text{CO}_3)$.

All three determinations follow the method outlined briefly here: we identified the data points on the TGA curve resulting from mass increase. In the case of $\text{Sr}_2\text{CuO}_2(\text{CO}_3)$, for example,

those were identified at 33.4466 mg (655 seconds) to 37.6611 mg (1355 seconds). Between these two points, the sample mass increased by 4.2145 mg as Sr_2CuO_3 reacted with CO_2 forming $\text{Sr}_2\text{CuO}_2(\text{CO}_3)$. This shows that there is an increase of 4.215 mg, entirely due to CO_2 insertion in 700 seconds. Using this relationship, we can infer the amount of Sr_2CuO_3 utilised at each second from the sample weight gain.

The order of reaction was determined to be 1st by fitting a line of best fit for the relationship between the concentration of Sr_2CuO_3 vs time (Figure 7 and Figures S1 and S2). The trendline of the graph can also then be used to determine a quantitative value for the rate constant k . Figure 7 shows three different graphs for concentration vs time, (1) moles of Sr_2CuO_3 vs time seconds, (2) $\ln(\text{moles})$ of Sr_2CuO_3 vs time seconds, and (3) $1/(\text{moles})$ of Sr_2CuO_3 vs time seconds, along with the respective kinetic models.

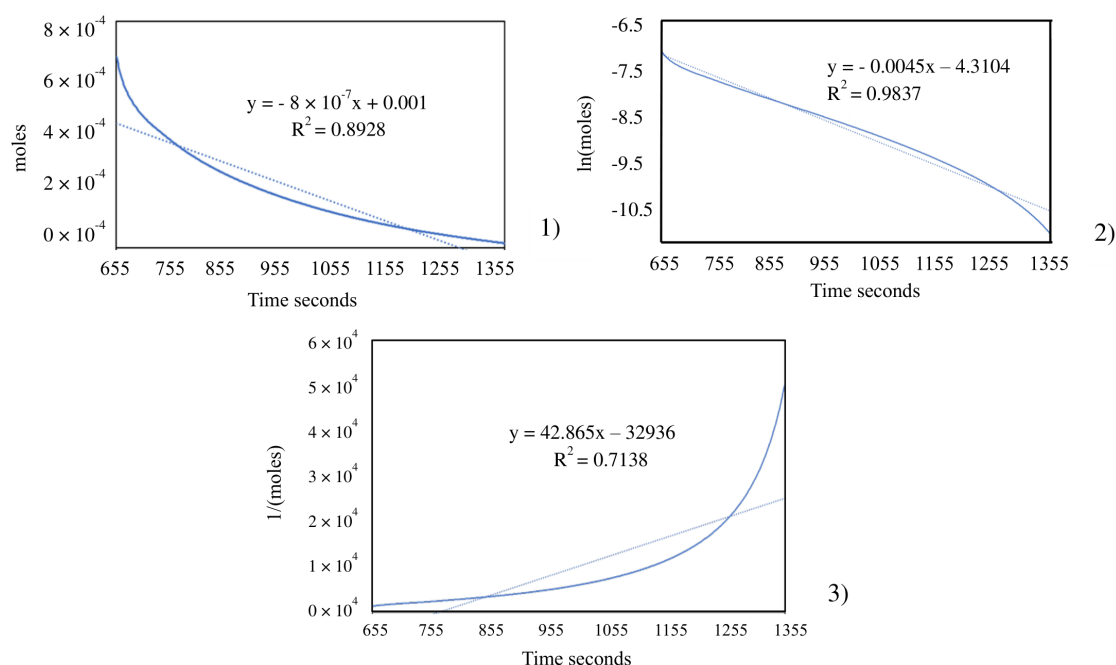


Figure 7: Three concentrations vs time graphs, (1) moles of Sr_2CuO_3 vs time seconds, (2) $\ln(\text{moles})$ of Sr_2CuO_3 vs time seconds, and (3) $1/(\text{moles})$ of Sr_2CuO_3 vs time second. Equations of trendlines and R^2 are given for each graph. The best fit ($R^2 = 0.9837$) is obtained for a first-order kinetics.

The apparent first-order kinetics constant for this reaction is determined from the slope of the fit to be $k = 0.0045 \text{ s}^{-1}$. A first-order kinetics model is consistent with a reaction where CO_2 is constantly replenished (this is the case, due to a constant stream of fresh CO_2 during the reaction) but where the oxide reaction sites are the limiting factors. Here we assume that the formation of the alkaline-earth/copper oxide-carbonate is the rate determining reaction. For all reactions we neglected the contribution from the formation of the alkaline-earth carbonates, as subtracting the weight of such carbonates would not change the slope.

The same procedure was followed for the formation reactions of $\text{Sr}_{1.8}\text{Ba}_{0.2}\text{CuO}_2(\text{CO}_3)$ and $\text{Sr}_{1.5}\text{Ca}_{0.5}\text{CuO}_2(\text{CO}_3)$ both reactions also followed first-order kinetics. Our results for the kinetic constants obtained are summarised in Table 1 below.

Oxide	Sr_2CuO_3	$\text{Sr}_{1.8}\text{Ba}_{0.2}\text{CuO}_3$	$\text{Sr}_{1.5}\text{Ca}_{0.5}\text{CuO}_3$
k/s^{-1}	0.0045	0.0048	0.0016

Table 1: determined values of the apparent first-order kinetic constants for the reactions of CO_2 with Sr_2CuO_3 , $\text{Sr}_{1.8}\text{Ba}_{0.2}\text{CuO}_3$ and $\text{Sr}_{1.5}\text{Ca}_{0.5}\text{CuO}_3$.

The reaction rates confirm that the substitution of calcium for strontium in Sr_2CuO_3 results in a lower reaction rate with CO_2 and slower reaction time, compared to the full strontium equivalent.

First-principles kinetic modelling of the reaction of CO_2 with $\text{A}_{2-x}\text{B}_x\text{CuO}_3$ (A, B = Ca, Sr, Ba)

In order to rationalise the kinetic constants measured experimentally (Table 1), we suggest that the CO_2 reaction proceeds through a surface-type mechanism and therefore should be well described by a model comprising a layer of alkaline-earth oxide and where the copper layer plays only a minor part. Indeed, a surface-like reaction occurs in A_2CuO_3 because “voids” are present in their crystal structure. At reaction temperature (approx. 1000°C), CO_2 gas will enter these voids and binds to the oxide anions to form the carbonate. This then means that an investigation of the reaction of CO_2 with an AO oxide surface should be a reasonable proxy for the formation of $\text{A}_{2-x}\text{B}_x\text{CuO}_2(\text{CO}_3)$.

There are already a number of studies that investigated the reaction of CO_2 with AO (A = Ca, Sr and Ba) oxides (Karlsen et al. and Schneider) ^[18,47]. Both of those studies use molecular functionals (PW91 or B3LYP), instead in our study we use PBE, which has traditionally been used for describing processes occurring at surfaces. While this choice might slightly disadvantage the description of molecular CO_2 , it has nevertheless been shown to give realistic surface binding energies.^[48] Furthermore, compounds showing perovskite-like structure have been shown to be prone to A enrichment on the surface compared to the bulk, with this segregation affecting reactivity with gas phases ^[49].

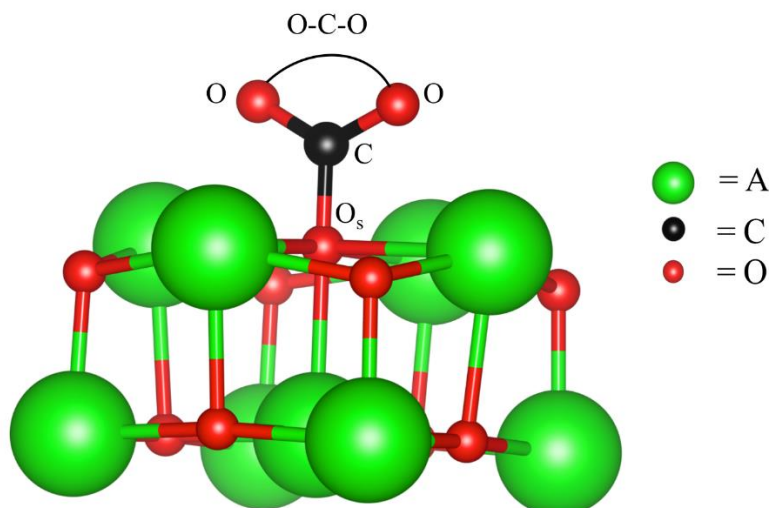


Figure 8: The optimised carbonate on the AO (A = Ca, Sr and Ba) cluster. The areas where the O-C-O ° angles and C-O_s bond lengths are measures are shown.

The optimised structure of CO₂ chemisorbed on a SrO “surface” (see “Theoretical approach to study the solid-gas reactions” in the experimental section for a full description of the surface model) is shown in Fig. 8. We note that this structure is in very good agreement with the previous studies of Schneider and Karlsen et al.^[18,47]. Our results for the bond lengths, O–C–O bond angle and adsorption energy for all three oxides (A= Sr, Ca and Ba) are summarised in Table 2, along with the results obtained with different functionals by Schneider and Karlsen et al.^[18,47]. The adsorption energy was determined as the difference between the optimised CO₂ and cluster energy separately to that of the surface-carbonate end-product.

Surface	Functional	O _s -C distance [Å]	C-O distance [Å]	O-C-O angle [°]	Adsorption energy [kJ mol ⁻¹]
SrO	PBE (This work)	1.392	1.267	127.0	-163
	PW91 (Schneider)	1.370	1.276	127.5	-188
	B3LYP (Karlsen)	1.460	1.240	132.0	-123
CaO	PBE (This work)	1.413	1.262	128.6	-124
	PW91 (Schneider)	1.384	1.270	129.1	-130
	B3LYP (Karlsen)	1.490	1.230	134.0	-87
BaO	PBE (This work)	1.374	1.272	125.6	-193
	PW91 (Schneider)	1.358	1.282	126.0	-226
	B3LYP (Karlsen)	1.440	1.240	130.4	-158

Table 2: Structural parameters of CO₂ adsorbed on three different metal oxides (SrO, CaO and BaO), along with the computed adsorption energy. Those values are also shown with the results of Schneider and Karlsen et al.^[18,47] for comparison.

We see that, for all oxides, the O_s-C distances computed with PBE are similar to those obtained with PW91, as expected since those two functionals are similar, and slightly shorter than the B3LYP results of Karlsen. This effectively puts our PBE values in between those of the two approaches. We see a similar trend for the C-O distances, where this time the B3LYP values are shorter and the PW91 values are longer, with our PBE results in between the two. Finally, the O-C-O angle for all cases is slightly smaller with PBE than with PW91 or B3LYP

Table 2 shows that the adsorption energies we computed using PBE again are in-between the PW91 results of Schneider and the B3LYP data of Karlsen et al.^[47] As expected, our GGA functional delivers results closer to the other GGA functional (PW91) rather than the hybrid B3LYP approach. Overall, our results are fully compatible with the published literature for both structural and energetic data.

Kinetic model

In order to gain some insights into the molecular mechanism of the reaction kinetics observed when varying the nature of the alkaline-earth metal (A), we propose the approach below. We assume reversible kinetics and therefore the kinetics of each reaction can be modelled by an Arrhenius-type equation:

$$k_x = A \exp\left(-\frac{E_x}{T}\right) \quad (1)$$

Where E_x is the adsorption energy of CO₂ on the oxide surface for A = x, A is the usual pre-exponential factor related to the probability of collision and T is the reaction temperature. To confirm the reversibility assumption or model, we reacted the oxycarbonates in air at the same conditions of time and temperature. The original oxides resulted from this reaction, thus confirming reversibility. This model was originally derived for surface adsorption kinetics, but it seems appropriate to use this here as the adsorption of CO₂ onto the reaction site is likely to be the rate-determining step.

Since the reactions all involve the same reactant (CO₂) and the reaction mechanism is the same (i.e. insertion into the solid), we assume that A is the same regardless of the nature of the alkaline-earth metal. This enables us to derive a simple relation between the kinetic constants of two reactions. By combining equation (1) for two different oxide surfaces in their logarithmic form, we obtain:

$$\ln k_1 = \ln A - \frac{E_1}{T} \text{ and } \ln k_2 = \ln A - \frac{E_2}{T}$$

thus:

$$\ln k_1 - \ln k_2 = \ln A - \frac{E_1}{T} - \left(\ln A - \frac{E_2}{T}\right)$$

leading to:

$$\ln k_1 - \ln k_2 = -\frac{E_1}{T} + \frac{E_2}{T} = \frac{E_2 - E_1}{T} = \frac{\Delta E}{T} \quad (2)$$

Where k_1 and k_2 are the kinetic constants for each reaction at temperature T and ΔE is the difference in adsorption energy of CO₂ onto the respective oxide surface models.

Using the results from Table 2, we can therefore determine a relation between the logarithms of the kinetic constants from first principles. However, as some of the oxides are actually mixed

oxides, we use their stoichiometric composition to weight their respective adsorption energy, $E_{A_xB_yO} = \frac{x}{x+y}E_{AO} + \frac{y}{x+y}E_{BO}$. Our results are summarised in table 3:

T = 1273/K	k /s⁻¹	ln(k)	Binary oxides $E_{AO}/\text{kJ mol}^{-1}$	Weighted energies $E_{A_xB_yO}/\text{kJ mol}^{-1}$
Sr₂CuO₃	0.0045	−5.4037	−163	
Sr_{1.8}Ba_{0.2}CuO₃	0.0048	−5.3391	−193	−166
Sr_{1.5}Ca_{0.5}CuO₃	0.0016	−6.4378	−124	−153

Table 3: Experimental rate constants and computed binary oxides adsorption energies, along with the weighted energies used for our kinetic model.

We use the computed weighted energies $E_{A_xB_yO}$ from table 3, to calculate the predicted Reactive adsorption energy difference (ΔE) with the kinetic model described earlier (see equation 2). The results obtained are shown in table 4, where we also compute the same values using the kinetic data measured during the reactions.

$\Delta E = (\ln k_1 - \ln k_2) \cdot T$	Reaction 2 (k_2)		
Reaction 1 (k_1)	Sr₂CuO₃ $\xrightarrow{\text{CO}_2}$ Sr₂CuO₂CO₃	Sr_{1.8}Ba_{0.2}CuO₃ $\xrightarrow{\text{CO}_2}$ Sr_{1.8}Ba_{0.2}CuO₂CO₃	Sr_{1.5}Ca_{0.5}CuO₃ $\xrightarrow{\text{CO}_2}$ Sr_{1.5}Ca_{0.5}CuO₂CO₃
Sr₂CuO₃ $\xrightarrow{\text{CO}_2}$ Sr₂CuO₂CO₃	0	−0.68 (−3.00)	+10.94 (+9.75)
Sr_{1.8}Ba_{0.2}CuO₃ $\xrightarrow{\text{CO}_2}$ Sr_{1.8}Ba_{0.2}CuO₂CO₃	+0.68 (+3.00)	0	+11.63 (+12.75)
Sr_{1.5}Ca_{0.5}CuO₃ $\xrightarrow{\text{CO}_2}$ Sr_{1.5}Ca_{0.5}CuO₂CO₃	−10.94 (−9.75)	−11.63 (−12.75)	0

Table 4: Reactive adsorption energy difference (ΔE) derived from experimental kinetics and our model values in brackets. All values are reported in kJ/mol for a temperature of $T = 1273$ K.

We observe that there is a strong qualitative agreement between our surface kinetics model and the experimental observations. In particular, both the sign *and* the magnitude of the energy difference are well predicted for all reactions. For example, we correctly predict that Sr_{1.8}Ba_{0.2}CuO₃ reacts faster than the pure strontium copper oxide, while Sr_{1.5}Ca_{0.5}CuO₃ reacts much slower than the other two compounds. This validates our initial assumption of a reaction that follows surface adsorption kinetics. Our model could be useful when predicting the kinetics of other insertion reactions in solids with vacancies in their crystal structure.

Reaction of Ba₂PdO₃ with CO₂

Ba_2PdO_3 is isostructural to Sr_2CuO_3 and shows one-dimensional Pd-O chains with Pd^{2+} coordinated in a square-planar fashion. Ba_2PdO_3 was therefore used to test the wider applicability of the direct reaction of CO_2 with compounds isostructural with Sr_2CuO_3 . Similarly to Sr_2CuO_3 , Ba_2PdO_3 was also reported to undergo fluorination to form the oxide-fluoride $\text{Ba}_2\text{PdO}_2\text{F}_2$.^[16,17]

Ba_2PdO_3 was reacted with CO_2 in identical conditions as Sr_2CuO_3 . This resulted in a three-phase sample with $\text{Ba}_{11}\text{Pd}_{11}\text{O}_{20}(\text{CO}_3)_2$ as the main phase, BaCO_3 and Pd metal. The Rietveld refinement of the sample is shown in Figure 9. The parameters derived from Rietveld refinement are listed in Table S4.

$\text{Ba}_{11}\text{Pd}_{11}\text{O}_{20}(\text{CO}_3)_2$ was reported by Crooks and Weller and has been labelled as “BaPdO₂”, due to the 1:1:2 ratio between the cations and anion. In $\text{Ba}_{11}\text{Pd}_{11}\text{O}_{20}(\text{CO}_3)_2$, Pd maintains its square planar coordination as in the starting oxide Ba_2PdO_3 . Hence, the insertion of CO_2 changes the crystal structure and the chemical composition, however, the strong stability of the Pd^{2+} cation in square-planar coordination prevents a structural rearrangement identical to the one occurring for Sr_2CuO_3 . Similarly, Pd^{2+} maintained its original square-planar coordination when undergoing fluorination from Ba_2PdO_3 to $\text{Ba}_2\text{PdO}_2\text{F}_2$.^[17]

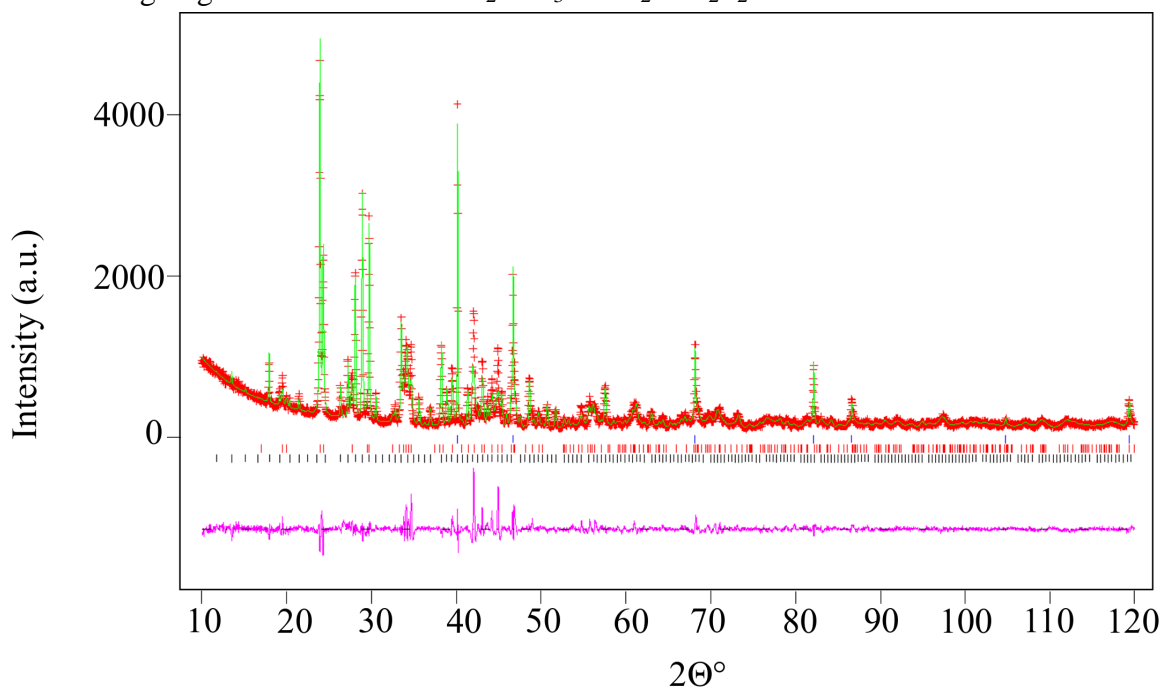


Figure 9 Rietveld refinement pattern of Ba_2PdO_3 after reacting with CO_2 , showing the observed (red crosses), calculated (green) and difference (purple) patterns. The ticks represent $\text{Ba}_{11}\text{Pd}_{11}\text{O}_{20}(\text{CO}_3)_2$ (black), BaCO_3 (red) and Pd metal (blue).

Rietveld refinements used the X-ray diffraction data for the models $\text{Ba}_{11}\text{Pd}_{11}\text{O}_{20}(\text{CO}_3)_2$ ^[50], BaCO_3 ^[51] and Pd metal^[52]. The refinement calculated $R_{\text{wp}} = 11.4$ and $\chi^2 = 3.981$ and showed in the terms of the weight fraction %, $\text{Ba}_{11}\text{Pd}_{11}\text{O}_{20}(\text{CO}_3)_2$ (50 %), BaCO_3 (42 %) and Pd metal (8 %). The structural data of $\text{Ba}_{11}\text{Pd}_{11}\text{O}_{20}(\text{CO}_3)_2$ has also been presented in the Supplemental Information, Table S4.

Conclusion

This work explores the utilisation of CO₂ as a reagent for the modification of the crystal structure of solids. Modifying the crystal structure of solids is a chemical tool to tailor their properties towards specific applications, and we demonstrate that structure tailoring via solid-gas reaction with CO₂ could be added to this toolbox. Selected mixed metal oxides were reacted with CO₂ and led to the formation of oxide-carbonates with modified crystal structures. The selected oxides were Sr₂CuO₃, Sr_{1.8}Ba_{0.2}CuO₃, Sr_{1.5}Ca_{0.5}CuO₃ and Ba₂PdO₃. They are all isostructural and showing anion-deficient K₂NiF₄ structure and were chosen because their crystal structure shows vacancies with potential to be host sites for CO₂. The actual chemical reactions were designed in a way that prevented as much as possible the formation of the favourable alkaline-earth carbonates as secondary phases. The oxide carbonates Sr₂CuO₂(CO₃), Sr_{1.8}Ba_{0.2}CuO₂(CO₃), Sr_{1.75}Ca_{0.25}CuO₂(CO₃) and Ba₁₁Pd₁₁O₂₂(CO₃)₂ were obtained and showed filled K₂NiF₄-type structure, indicating that CO₂ can be used as a reagent to modify the crystal structure of oxides, as well as prepare oxide carbonates.

We proposed a simple model for the kinetics of the reactions between the cuprates and CO₂ based on calculations of the adsorption energy of CO₂ on the surface of the binary alkaline earth metal oxides. We obtained near-quantitative agreement with the kinetics determined for the apparent reactions.

Some initial guidelines can be evinced for the application of CO₂ as crystal structure modifier to a wider range of materials as well as the preparation of novel oxide-carbonates. The CO₂ molecules insert into the vacancies within the crystal structure of the parent compounds and links with an oxide to give the carbonate anion. Hence, the starting materials should be oxides and their crystal structure must show voids to host the CO₂. Furthermore, we suggest that these vacancies need to be of appropriate size to host CO₂, the kinetic diameter of which is 3.3 Å.

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Keywords: carbon dioxide fixation; intercalation; main groups elements; perovskite phases; transition metals

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