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1	Performance investigation of solar tower system using cascade supercritical
2	carbon dioxide Brayton-steam Rankine cycle
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13	Abstract: A novel solar power tower system that integrates with the cascade supercritical carbon
14	dioxide Brayton-steam Rankine cycle is proposed to tackle the challenges of a simple supercritical
15	carbon dioxide system in solar power systems. It provides a large storage capacity and can react to
16	the fluctuation of solar radiation by adjusting the mass flow rate of molten salts in the receiver and
17	heat exchanger. The fundamental is illustrated and comprehensive mathematical models are built.
18	Energy and exergy analysis in the heat collection and power conversion processes is conducted. A
19	comparison between the novel system and simple supercritical carbon dioxide system is made at a
20	design plant output of 10 MW. Results indicated that: (1) the cascade system has a lower receiver
21	inlet temperature, wider temperature difference across the receiver, higher specific work of the
22	thermal energy storage system and lower mass flow rate of the working fluids. The solar-thermal
23	conversion efficiency of the receiver is improved significantly. The heat gain of the tower receiver of

the novel system is 53.4 MWh, which is about 7.1 MWh more than that of the simple system. The electricity production of the cascade system is improved by 9.5% at design point; (2) The novel system can generate constant electricity in a wide range of solar radiation and offer flexible control strategy for heat collection and storage. It is a promising option for central solar tower technology with a high efficiency, large storage capacity and short payback period.

Keywords: Supercritical carbon dioxide; Brayton cycle; Rankine cycle; solar tower; Cascade
system

Nomenclature			
a	Ambient	HTF	heat transfer fluid
А	Area, m ²	MS	molten salt
D	Diameter, m	sCO ₂	Supercritical carbon dioxide
F	view factor	SR	steam Rankine
Gr	Grashof number	STP	solar tower power
h	heat transfer coefficient $W/(m^2 \cdot K)$	TES	thermal energy storage
Н	Height,m	Subscripts	
k	thermal conductivity, $W/(m \cdot K)$	abs	absorbed
Ν	Number	с	convection
Nu	Nusselt number	conv	convection
Pr	Prandtl numbers	cond	conduction
Q	Energy flux, W/m or W/m ²	f	reference solar flux or fluid
Re	Reynolds number	fc	forced convection

Т	Temperature, $^{\circ}C$ or K	i	Inner
W	Work, W	in	inlet
α	Absorption	inf	real solar flux
ß	volumetric thermal expansion	m	mirror
þ	coefficient, 1/K	m	minor
3	Emissivity	nc	natural convection
η	Efficiency	0	outer
λ	thermal conductivity, $W/(m \cdot K)$	ou	outlet
Δx	Length, m	r	radiation
Abbreviation		sol	incident solar irradiation
CSP	Concentrated solar power		

31

32 1. Introduction

Concentrated solar power (CSP) is a dispatchable power generation technology that can employ 33 34 cheap materials for thermal energy storage(TES) in comparison with the photovoltaic system [1]. Nowadays, the CSP systems can be classified into four main technic routines, namely solar tower 35 power (STP) system, parabolic trough system, linear Fresnel system, dish system[2]. Among them, 36 the STP system is point focusing technology, which has a higher solar concentration ratio and is 37 easier to reach a higher heat collection temperature and higher efficiency[3]. However, it is not 38 economically competitive when compared with the traditional fossil-fired power plants at the current 39 stage[4]. Further investigations should be devoted to efficiency increment and cost reduction. To 40 achieve a higher photo-electric efficiency, the next generation CSP systems tend to operate at a 41

42 higher temperature [5].

With the increase of the operating temperature above 700°C, the chemical reaction between the 43 water-steam and solid materials in the boiler is obviously intensified. Thus the traditional steam 44 Rankine cycle cannot satisfy the improvement of the operating temperature[6]. The supercritical CO₂ 45 (sCO₂) Brayton cycle has been proposed to achieve a higher temperature. The advantages of the 46 supercritical CO₂ Brayton cycle can be summarized as follows: (a) CO₂ is an inert working fluid and 47 possesses a significantly weaker chemical corrosion with power cycle components compared with 48 water-steam, indicating that the inlet temperature of the gas turbine can be further improved[7]; (b) 49 the thermal conversion efficiency of the sCO₂ cycle is remarkably higher than a water-steam Rankine 50 cycle when the maximum operation temperature exceeds $450^{\circ}C[8]$; (c) the whole sCO₂ system 51 operates under the supercritical status with high pressure(>7.38MPa). Thus the sizes of the turbine 52 53 and heat exchangers are reduced significantly, leading to low thermal inertia of the power plants and flexible power output adjustment[9]. 54

Based on the benefits mentioned above, sCO₂ Brayton system is regarded as an alternative of the 55 traditional water/steam Rankine cycle. The various researches related to sCO₂ cycle are studied 56 experimentally and theoretically. The sCO₂ Brayton cycle was firstly proposed by Sulzer in the 57 950s[10], and the performance characteristic of the sCO₂ system was firstly analyzed by Feher[11]. 58 Dostal reported that the thermal efficiency could achieve 45.3% with a cost reduction in the power 59 system by 18% compared to the steam Rankine cycle at the inlet temperature of 550°C[12]. Several 60 sCO₂ layout configurations, including recompression[13] and intercooling[14], were also proposed to 61 improve power cycle efficiency. 62

63 To date, with the demand for the severe peak load regulation of the coal-fired power plants and fast

development of the CSP technologies, sCO₂ systems have attracted increasing attention by 64 researchers.. Xu et al. summarized the key issues and challenges of the sCO₂ used for coal-fired 65 power plants[15] and proposed solution strategies[16]. The CO₂ boiler pressure drop was decreased 66 to the water-steam boiler level and the cascade flue gas utilization system was proposed to improve 67 thermal conversion efficiency. The feasibility of the integrated sCO₂ with CSP systems was also 68 evaluated and analyzed. He et al. developed an integrated model for the integrated STP system 69 including the solar field, the molten salt (MS) solar receiver, the MS TES system, heat transfer fluid 70 (HTF) and the sCO₂ Brayton cycle[17]. The thermal performance of the CSP system using sCO₂ as 71 the HTF under non-uniform solar flux was studied and analyzed[18]. Thermodynamic analysis and 72 cycle layout optimization of the MS STP system integrated with a sCO₂ Brayton cycle were carried 73 out[19]. They pointed out that the maximum allowable MS temperature of 680°C was recommended 74 75 for the STP system combined with sCO₂ Brayton cycle under the present conditions and the intercooling cycle could generally offer the highest efficiency. Reyes-Belmonte presented a 76 single-stage sCO₂ cycle that integrated with recompression and a dense gas-particle suspension tower 77 receiver. The solar tower power systems using gas-particle suspension receiver was regarded as one 78 of the promising options to couple with the sCO₂ power cycle due to the high temperatures achieved 79 and the stability of the particle[20]. Saboora et.al. presented a detailed analysis of a combined power 80 block system using carbon dioxide integrated with a thermal energy storage system and solar field 81 82 [21]. Recently, the tower receiver that employed sCO_2 as heat transfer fluid (HTF) directly was investigated. In this case, the tower receiver was regarded as a primary heat exchanger in CSP 83 systems, thus directly applying the power cycle working fluid as the receiver HTF. The integration of 84 five different direct-heated sCO₂ Brayton cycles into a solar power tower system was studied by He 85

et.al. [22]. In addition, exergetic analysis of sCO₂ Brayton cycles integrated with direct CO₂ solar
central receivers was carried out to demonstrate the effect of operation temperature and the cycle
layout on the overall performance and exergy loss[23].

Desipte of the extensive investigation, there are some technical issues and challenges of combining the sCO₂ Brayton cycle with STP systems. Firstly, the single sCO₂ cycle cannot achieve optimal thermal conversion efficiency in such a wide temperature range of 200~700 °C. The sCO₂ cycle only can exhibit cycle efficiency superiority at a high temperature above 500 °C compared with steam Rankine cycle. In addition, the exhaust temperature of the gas turbine in the sCO₂ cycle is high. After being cooled in the regenerator, residual thermal energy is directly cooled by the cooler to the surroundings, causing a large amount of energy loss and significant efficiency decrease.

Furthermore, the regenerator outlet temperature (namely receiver inlet temperature) is high for a simple Brayton cycle, resulting in the high operating temperature of the solar receiver. Actually, the solar-thermal efficiency of the tower receiver is strongly dependent on the receiver temperature. The convection and radiation heat losses of the tower receiver significantly increase with the elevation of the receiver operating temperature.

Finally, at present there is no mature technology for higher temperature thermal storage, and the application of supercritical carbon dioxide in a tower power station is thereby restricted. The MS is regarded as an ideal thermal storage fluid, which has been employed in commercial CSP plants. However, the current MS cannot withstand temperature of above $600^{\circ}C$ [24], MS cannot meet the requirement of the higher temperature thermal storage of the sCO₂ systems. Meanwhile, the temperature difference across the solar receiver of the traditional system is also narrow, which causes great challenges for coupling with the sensible thermal energy storage (TES)[25]. Therefore, at the current stage, it is a crucial issue to build a novel sCO_2 cycle layout that can lead to a high efficiency, large specific work, and wide temperature difference across the receiver if the mature sensible TES is going to be adopted.

In this study, a novel solar tower power system integrating with supercritical carbon dioxide 111 Brayton-steam Rankine power cycle is proposed. The power block consists of a top sCO₂ Brayton 112 cycle and bottom steam Rankine cycle. The high temperature exhaust gas of the sCO₂ turbine is 113 introduced to the sCO₂/water heat exchanger for heating subcooling water and generating high 114 temperature and pressure steam, then driving the bottom steam Rankine cycle. The solar tower 115 receiver of the proposed system includes two HTF loops, namely the MS loop and sCO₂ loop, and 116 the lengths of the two loops can be adjusted. The cooled sCO_2 is directly heated by the solar receiver. 117 The MS is regarded as a sCO₂ preheating fluid and thermal storage medium. The current study firstly 118 119 develops a comprehensive numerical model that involves solar energy collecting subsystem and power cycle subsystem and the overall performance of the solar power systems is evaluated. The 120 cycle efficiency and parameters of the power cycle are analyzed and compared under different design 121 temperatures and pressure. Furthermore, the comparisons of the exergy loss and electricity output 122 between simple sCO₂ and sCO₂-SR systems at design point are carried out. 123

124 **2.** System description

The novel STP system in the present work mainly consists of a solar field, a central tower receiver, a two-tank MS thermal energy storage subsystem, and a cascade sCO_2 -RC cycle. The external central tower receiver consists of several solar panels as shown in **Figure** 1a and **Figure** 1b. The receiver is divided into two fluid sections for the STP system as shown in **Figure 1c**, namely the MS loop and sCO_2 loops. The MS and sCO_2 loops are arranged at different positions of the receiver. The loop lengths of the sCO₂ and MS loops are regarded as controllable to match the energy demand in
different operating conditions.





Figure 1 Physical structure of the central receiver's (a) 3D view (b) heat transfer fluid flow path of
the single fluid receiver (c) the top view of the dual fluid receiver

137 The operation strategy of the novel cascade STP system can be illustrated as follows

a. When the solar energy gain from the tower receiver can satisfy the full-load operation of the sCO₂ cascade cycle, the sCO₂ from the power block is heated to the desired temperature directly in the tower receiver. The high temperature and pressure sCO_2 is introduced into the turbine for electricity generation. Meanwhile, the energy of the high temperature exhaust gas of the top sCO_2 Brayton cycle is released to the bottom steam Rankine cycle by several sCO_2 /water heat exchangers. The sCO_2 and MS loop lengths and mass flow rate of MS are are adjusted according to the solar flux distribution of the receiver to keep full-load operation of the power block. The extra solar energy that exceeds the demand of the power block is collected by the MS loop and stored in the TES subsystem. The diagram of the this operation mode is shown in **Figure 2a**.

147 The energy gain from the receiver is less than the rated heat input to the cascade sCO₂-RC, but b. the system can still operate at full-load condition if sCO2, prior to its entrance to the receiver, is 148 preheated by molten salts in the heat exchanger. In this case, the sCO₂ is firstly preheated by 149 solar salt from the hot MS tank. Then, the preheated sCO₂ is introduced into the tower receiver to 150 absorb solar irradiation and elevate temperature. Finally, the high temperature and pressure sCO₂ 151 flows into the turbine and generates electricity. The energy of the high-temperature exhauste gas 152 of top sCO₂ Brayton cycle is used to drive the bottom steam Rankine cycle by several 153 sCO₂/water heat exchangers. The diagram of the this operation mode is shown in Figure 2b. 154

c. If the system cannot operate at full-load condition even CO2 is preheated by the molten salts,
then the cascade system is closed and the operation strategy of the system is converted to thermal
energy storage mode, meanwhile, the bottom steam Rankine cycle can operate by using MS as a
heat source or stop, depending on the grid load. The sCO₂ loop is closed and MS is heated by
tower receiver to 565°C and stored in TES subsystem. The diagram of this operation mode is
shown in Figure 2c.

d. At night or no sun periods, solar energy collecting subsystem, including solar field and tower
 receiver, is closed. The bottom steam Rankine cycle can keep running. The subcooled water is
 preheated, evaporated, superheated by hot MS from TES system.





(b)



- Figure 2 The diagram of the cacasde sCO₂-SR solar power system.(a) full-load operation with
- thermal storage; (b) full-load operation with molten salt preheating; (c) bottom cycle operation

172 **3. Mathematic model**

173 In this section, the comprehensive system numerical model, including a solar energy collecting 174 subsystem and power block subsystem, is developed to compare the performance of the STP plants 175 using simple sCO_2 and cascade sCO_2 -SR system.

176 **3.1 Solar energy collecting subsystem**

The numerical model of the solar energy collecting subsystem includes a solar field optical model and central tower receiver heat transfer model. The configuration parameters of the 10MW demonstrated STP plant in Dunhuang with 15h thermal energy storage capacity and an external central tower receiver is selected for modelling as example[26].

181 **3.1.1 Solar field optical model**

The detailed design parameters of the solar tower receiver and solar field of the Dunhuang STPplants are presented in Table 1 from the FluxSPT model[26].

184

Table 1 Detailed configuration parameters of the solar power tower systems

Parameters	Unit	Value
Tower height	m	121.4
Receiver height	m	10.5
Receiver diameter	m	7.3
Panels number	/	18
Coating absorption	/	0.94
Coating emittance	/	0.88

Tube outer diameter	mm	40
Tube wall thickness	mm	1.25(3.5)
Tube number per panel	/	31
Heliostats number	/	1525
Heliostats mirror reflectance	/	0.9

The model developed by Domingo Santana is used to obtain the solar flux distribution and concertation of the tower receiver[27]. The aiming factor is employed to simulate solar flux distribution of the receiver, which is a concept to demonstrate the aiming strategy of the solar tower systems. In this study, the value of the aim factor is set as 2. The solar field heliostat efficiencies and solar flux distribution of the receiver with incident solar irradiation of 900W/m² at Spring Equinox noon are presented as **Figure 3**.



191

192



Figure 3 Optical model of the solar field. (a) heliostat efficiencies at Spring Equinox noon (b) solar
flux distribution of the receiver

197 Then, the solar flux distribution under different solar irradiation conditions at the same time can be 198 calculated as follow:

199
$$Q_{inf}(i,j) = \frac{Q_f(i,j)Q_{sol}}{900}$$
 (1)

200 Where the *i* and *j* represents the different positions of the tower receiver ; the $Q_f(i, j)$ is the solar flux 201 distribution as shown in Figure 2 with the design incident irradiation of 900 W/m²; Q_{sol} is incident 202 solar radiation that differs from the reference point, W/m²; Thus the solar flux distribution of the 203 receiver at the different reference point can be obtained by **Equation 1**.

3.1.2 Central tower receiver heat transfer model

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194

The heat transfer model of the central tower receiver is composed of external thermal loss and internal HTF heat transfer. The diagram of the single receiver tube heat transfer is shown as **Figure 4**. The central receiver consists of a large number of single receiver tubes and refractory walls as shown in **Figure 2a**.



Figure 4 Heat transfer of the central tower receiver. (a) the diagram of the single receiver tube of the tower receiver; (b) external heat loss of the receiver; (c) internal heat transfer of the receiver tube of a control unit.

213 *3.1.2.1 External heat transfer of the receiver tube*

209

218

The external heat transfer process of the receiver includes radiation, convection heat loss, and solar energy absorption. The external heat transfer of the tower receiver is depicted in **Figure 4b**.

216 The solar energy absorbed by the receiver can be inferred from solar flux distribution and geometry

dimension of the receiver tube as **Equation** (2):

$$Q_{abs} = \alpha Q_{inf}(i, j) D\Delta x \tag{2}$$

219 Where the α is solar irradiation absorption of the solar selective coating; *D* is the outer diameter of 220 the single receiver tube, m; Δx is length of the receiver tube as shown in **Figure 4c**, m.

- 221 The temperature of the receiver tube is regarded as uniform in circumferential and axial directions in
- a control unit for radiation and convection heat loss calculation. Furthermore, the temperature of the
- 223 different receiver tubes in a panel is also regarded as uniform in the horizontal direction. Thus, the

temperature of the receiver tube varies only in the HTF flow direction. The radiation heat loss calculation of the receiver tube is simplified as two long parallel cylinders. The radiation loss of the receiver is the heat transfer between receiver tube and ambient and is expressed as follows[28]:

227
$$Q_{loss,r} = \frac{\sigma \left(T_{abs,o}^4 - T_0^4\right)}{\frac{1 - \varepsilon}{\varepsilon_{abs}A} + \frac{1}{AF}}$$
(3)

Where $T_{abs,o}$ is the outer surface temperature of the single receiver tube, K; T_0 is surrounding temperature, K; A is the surface area of the receiver tube, m²; ε_{abs} is the emissivity of the receiver tube; F is view factor between receiver tube and ambient which can be calculated using Crossed-String method by Modest[29].

The convection heat loss is calculated by Newton cooling formula as follow[28]:

233
$$Q_{loss,c} = h_c A \left(T_{abs,o} - T_a \right) \tag{4}$$

According to Siebers and Kraabel research[30], the convective heat transfer coefficient h_c of the central external receiver has taken into consideration of the combined action of the forced and natural convective of the air and calculated as follow:

237 $h_c = \left(h_{fc}^{3.2} + h_{nc}^{3.2}\right)^{\frac{1}{3.2}}$ (5)

238 Where natural convective coefficient h_{nc} can be expressed:

$$h_{nc} = \frac{\lambda_a N u_{nc}}{H}$$
(6)

$$Nu_{nc} = 0.049\pi Gr_{nc}^{1/3} \left(\frac{T_a}{T_{abs}}\right)^{0.14}$$
(7)

241
$$Gr_{nc} = \frac{g\beta(T_{abs} - T_a)H^3}{v_a^2}$$
(8)

242 And the forced convection coefficient h_{fc} is given as:

240

$$h_{fc} = \frac{\lambda_{a,b} N u_{fc}}{D_r}$$
(9)

244
$$Nu_{fc} = 0.0455 \operatorname{Re}_{fc}^{0.81}$$
 (10)

Where *H* and D_r is the height and diameter of the receiver, respectively. The volumetric thermal expansion coefficient β is equal to $1/T_a$ for the air and the kinematic viscosity of the air v_a is evaluated at the ambient temperature T_a . $\lambda_{a,b}$ is evaluated at the arithmetic average of the tube temperature and the ambient temperature while the thermal conductivity for the natural convection λ_a is evaluated just at the ambient temperature.

250 3.1.2.2 Internal heat transfer of the receiver tube

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In this work, the sCO₂ and MS are employed as HTF to deliver thermal energy to the power block.
The heat flux of the HTF heat transfer is expressed by Newton cooling formula[28]:

$$Q_{conv} = \pi h_f D_{abs,i} \left(T_{abs,i} - T_f \right) \tag{11}$$

$$h_f = N u_f \frac{k_f}{D_{abs,i}} \tag{12}$$

where Q_{conv} is the convection heat flux between absorber inner surface and HTF, W; h_f is the heat convection transfer coefficient, W/(m²·K); $D_{abs,i}$ is the inner diameter of the absorber tube, m; $T_{abs,i}$ and T_f are the temperatures of inner surface of the absorber tube and HTF, °C; and k_f is the thermal conductance of the HTF, W/(m·K). The sCO₂ and MS are regarded as single-phase fluid, thus the Nusselt number of the internal flow for transitional and turbulent flow can be calculated by Gnielinski formula[28]:

259
$$Nu_{f} = \frac{f_{abs,i} / 8 \left(\operatorname{Re}_{f} - 1000 \right) \operatorname{Pr}_{f}}{1 + 12.7 \sqrt{f_{abs,i} / 8} \left(\operatorname{Pr}_{f}^{2/3} - 1 \right)} \left(\frac{\operatorname{Pr}_{f}}{\operatorname{Pr}_{abs,i}} \right)^{0.11}$$
(13)

$$f_{abs,i} = \left(1.82\log_{10}\left(\mathrm{Re}_{f}\right) - 1.64\right)^{-2}$$
(14)

where $f_{abs,i}$ is the friction factor for the inner surface of the absorber tube; \Pr_{f} and $\Pr_{abs,i}$ are the Prandtl numbers of the HTF evaluated at the HTF temperature and absorber inner surface temperature. The thermophysical property of the sCO₂ is acquired by means of commercial software RefProp 9.1[31] and that of the MS is obtained by the empirical formula presented in reference[32]. The conduction heat transfer of the receiver tube wall can be obtained by the Fourier's law of hollow cylinder [28]:

$$Q_{cond} = \frac{2\pi\lambda \left(T_{abs,i} - T_{abs,o}\right)}{\ln \left(\frac{D_{abs,o}}{D_{abs,i}}\right)},\tag{15}$$

where λ is the thermal conductivity of the receiver tube wall, W/(m·K).

Based on above external and internal heat transfer of the receiver tube, the receiver tube is divided into a number of the control volume unit with an interval length of 0.1m along the HTF flow direction, thus the mass flow rate of the HTF is obtained with the given outlet temperature and solar irradiation by solving control unit energy balance equation:

272
$$m \left[c_{p,j} \left(T_{in,j} - T_{out,j} \right) + \frac{1}{2} \left(v_{in,j}^2 - v_{out,j}^2 \right) \right] + Q_{abs,j} - \Delta x \left(Q_{loss,r,j} + Q_{loss,c,j} \right) = 0$$
(16)

where Δx is the length of the control volume unit, m. The outlet temperature of the "*j*" control volume unit is set as inlet temperature of the "*j*+1" control volume unit. The iteration is performed similarly until a loop cycle of the receiver pipeline is finished. The calculation processes and flow chart of the numerical model for different operation strategies are described in **Appendix**.

277 3.2 Thermodynamics model of the power cycle



Figure 5 The diagram of the power cycle (a) simple Brayton cycle (b) cascade sCO₂-SR cycle using
MS preheating

Table 2 Input parameters of the power cycle[19]

Input parameters	Value
Maximum sCO ₂ cycle pressure, P_{max}	20~35 MPa
Minimum sCO ₂ cycle pressure, P_{\min}	7.36 MPa
sCO_2 Compressor inlet temperature, T_{cci}	32 °C

Turbine isentropic efficiency, η_t	0.93
Compressor isentropic efficiency, η_c	0.89
Steam condenser pressure, $P_{\rm sto}$	8 kPa

Table 3 Energy balance of the power cycle[33]

Component	Simple Bayton cycle	Cascade cycle
sCO ₂ -Compressor	$\eta_{\rm c} = (h_{\rm 5s} - h_4)/(h_5 - h_4)$	$\eta_{\rm c} = (h_{7\rm s} - h_6)/(h_7 - h_6)$
	$W_{\rm cc}=m_{\rm c}(h_5-h_4)$	$W_{\rm cc}=m_{\rm c}(h_7-h_6)$
Water pump	/	$W_{sc} = m_{\rm s}(h_{13} - h_{12})$
sCO ₂ -Turbine	$\eta_{t} = (h_1 - h_2)/(h_1 - h_{2s})$	$\eta_1 = (h_1 - h_2)/(h_1 - h_{2s})$
	$W_{\rm ct}=m_{\rm c}(h_1-h_2)$	$W_{\rm ct}=m_{\rm c}(h_1-h_2)$
Steam-Turbine	/	$\eta_t = (h_{10} - h_{11})/(h_{10} - h_{11s})$
	/	$W_{\rm st} = m_{\rm c}(h_{10}-h_{11})$
Regenerator	$h_2 - h_3 = h_6 - h_5$	$h_3 - h_4 = h_8 - h_7$
Preheater	$m_{\rm c}(h_4-h_5)=m_{\rm s}(h_{13}-h_{13})$	/
Biloer	$m_{\rm c}(h_2-h_3)=m_{\rm s}(h_{10}-h_{14})$	/
Heat source	$Q_c = m_c(h_1 - h_6)$	$Q_c = m_c(h_1 - h_8)$
Table 4 Everey analysis of the newer plant		

286

Table 4 Exergy analysis of the power plant

Component	Simple Bayton cycle	Cascade cycle
Solar field	$Ex_s = \eta_s NA_m Q_f$	$Ex_s = \eta_s NA_m Q_f$
	$\eta_s = 1 - \frac{4}{3} \frac{T_a}{T_{sun}} + \frac{1}{3} \left(\frac{T_a}{T_{sun}} \right)^4$	$\eta_s = 1 - \frac{4}{3} \frac{T_a}{T_{sun}} + \frac{1}{3} \left(\frac{T_a}{T_{sun}} \right)^4$

Receiver surface	$Ex_r = \eta_s A_r Q_{inf}$	$Ex_r = \eta_s A_r Q_{inf}$
	$\eta_{s} = 1 - \frac{4}{3} \frac{T_{a}}{T_{sun}} + \frac{1}{3} \left(\frac{T_{a}}{T_{sun}}\right)^{4}$	$\eta_s = 1 - \frac{4}{3} \frac{T_a}{T_{sun}} + \frac{1}{3} \left(\frac{T_a}{T_{sun}} \right)^4$
HTF	$\Delta E x_h = m_c \left[\left(h_6 - h_1 \right) - T_a \left(s_6 - s_1 \right) \right]$	$\Delta E x_h = m_c \left[\left(h_8 - h_1 \right) - T_a \left(s_8 - s_1 \right) \right]$
sCO ₂ -Turbine	$\Delta E x_{ct} = m_c \left[\left(h_1 - h_2 \right) - T_a \left(s_1 - s_2 \right) \right]$	$\Delta E x_{ct} = m_c \left[\left(h_1 - h_2 \right) - T_a \left(s_1 - s_2 \right) \right]$
sCO ₂ -Compressor	$\Delta E x_{cc} = m_c \left[\left(h_4 - h_5 \right) - T_a \left(s_4 - s_5 \right) \right]$	$\Delta E x_{cc} = m_c \left[\left(h_6 - h_7 \right) - T_a \left(s_6 - s_7 \right) \right]$
Regenerator		
High pressure	$\Delta E x_{cre,h} = m_c \left[\left(h_5 - h_6 \right) - T_a \left(s_5 - s_6 \right) \right]$	$\Delta E x_{cre,h} = m_c \left[\left(h_7 - h_8 \right) - T_a \left(s_7 - s_8 \right) \right]$
side		
Low pressure side	$\Delta Ex_{cre,l} = m_c \left[\left(h_2 - h_3 \right) - T_a \left(s_2 - s_3 \right) \right]$	$\Delta Ex_{cre,l} = m_c \left[\left(h_3 - h_4 \right) - T_a \left(s_3 - s_4 \right) \right]$
Pre-cooler	$\Delta E x_{cp} = m_c \left[\left(h_3 - h_4 \right) - T_a \left(s_3 - s_4 \right) \right]$	$\Delta Ex_{cp} = m_c \left[\left(h_5 - h_6 \right) - T_a \left(s_5 - s_6 \right) \right]$
Steam-Turbine	/	$\Delta E x_{st} = m_s \left[\left(h_{10} - h_{11} \right) - T_a \left(s_{10} - s_{11} \right) \right]$
Condenser	/	$\Delta E x_{sd} = m_s \left[\left(h_{11} - h_{12} \right) - T_a \left(s_{11} - s_{12} \right) \right]$
Bioler	/	Simialr with regenerator
Preheater	/	Simialr with regenerator

For a preliminary demonstration of the advantages of the hybrid systems, a simple Brayton cycle and 287 a cascade cycle based on simple Brayton and Rankine cycle are employed for performance 288 comparison. A simple Brayton cycle consists of a gas compressor, turbine, heat regenerator and 289 precooled exchanger as shown in Figure 5a. For the cascade cycle, the system configuration is 290 slightly more complex than that of the simple Brayton cycle as shown in Figure 5b. The valve is 291 employed to control sCO₂ preheating according to solar incident irradiation. The input parameters of 292 the two cycle systems are presented in Table 2[19]. For the heat exchanger, such as regenerator, 293 boiler, the minimum heat transfer difference are set as 10°C. The energy balance and exergy analysis 294

of the main component of the simple and cascade cycle are listed in **Table 3 and Table 4**. Based on

the parameters shown in **Table 3**, the cycle efficiency of the systems can be calculated as follows:

297 Simple Brayton cycle efficiency:

$$\eta = \frac{W_{ct} - W_{cc}}{Q_c} \tag{17}$$

299 Cascade cycle efficiency:

$$\eta = \frac{W_{ct} - W_{cc} + W_{st} - W_{st}}{Q_c}$$
(18)

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The exergy loss of the each components can be also calculated by the exergy and exergy difference results as presented in **Table 4**.

The sCO₂ mass flow rate of a power block can be obtained by following Equation(19) and Equation(20) :

306 Simple Brayton cycle :

$$m_{c} = \frac{P}{\left(h_{1} - h_{2}\right) - \left(h_{5} - h_{4}\right)}$$
(19)

308 Cascade cycle:

$$m_{c} = \frac{P}{(h_{1} - h_{2}) - (h_{7} - h_{6}) + x[(h_{10} - h_{11}) - (h_{13} - h_{12})]}$$
(20)

310
$$x = \frac{\left[\left(h_2 - h_3\right) + \left(h_4 - h_5\right)\right]\eta_T}{h_{10} - h_{13}}$$
(21)

Where *P* is net work output of the power block, W; h_1 , h_2 , h_4 , h_5 , h_6 , h_7 , h_{10} , h_{11} , h_{12} and h_{13} are the enthalpy of the fluid at different points; *x* is ratio of the steam mass flow to carbon dioxide mass flow; η_T is thermal efficiency of the heat transfer exchangers.

315 3.3 Model validation





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Figure 6 Validation of the power cycle

The simple Brayton cycle is also validated by the previous works with the inlet temperature from 318 500°C to 850°C as shown in Figure 6. The relative error between the current model and reference 319 results is between 0.01% and 1.5% for all operation temperatures. The parameters used for model 320 321 validation are listed in Table 2. The HTF heat transfer model and solar field optical model used in this study have been investigated and validated by previous work.[34] Based on the above results of 322 the comprehensive thermodynamic model of the power cycle and validated solar collecting 323 subsystem model, the current numerical model can be extended to overall performance analysis of 324 the solar tower power system integrated with sCO₂ Brayton cycle. 325

326 4. Results and discussion

The simulation process is implemented in a Matlab program based on the above model and parameters. The thermodynamics performance analysis and operation strategy adjustment of the

soalr power systems are elaborated in this section.

330 4.1 Thermodynamics analysis

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Figure 7 Regenerator outlet temperature variations with the turbine inlet temperature

The solar energy collecting temperature is crucial to solar-thermal conversion efficiency in solar 334 power systems. The regenerator outlet temperature (namely tower receiver inlet temperature) 335 variations with turbine inlet temperature and maximum operation pressure are presented in Figure 7. 336 337 The regenerator outlet temperature of the simple sCO₂ system increases with the turbine inlet temperature but decreases with pressure. The influences of turbine inlet temperature on the two solar 338 systems are different. For the simple sCO2 cycle system, a lower turbine inlet pressure and higher 339 340 inlet temperature lead to a higher exhaust temperature, resulting in a higher heat regeneration outlet temperature. While for the cascade system, given a constant power output of 10 MW, a higher 341 turbine inlet temperature is accompanied with a larger power put by the SR cycle. More energy is 342 released from the exhaust gas to the bottom SR cycle via the sCO₂/water heat exchanger, leading to a 343

344 lower heat regeneration outlet temperature.

Notably, the regenerator outlet temperature of the sCO₂-SR cycle is significantly lower than that of 345 the simple sCO₂ cycle, especially at high operating temperature. It indicates that the average solar 346 receiver temperature can be decreased appreciably and the solar-thermal conversion efficiency is also 347 improved. Furthermore, the lower inlet temperature also presents a wide temperature difference 348 across the solar receiver, improving the specific work of the TES system if there is a suitable thermal 349 fluid for thermal storage of the sCO₂ system with a lower HTF flow rate. The challenges of the 350 narrow temperature difference across the solar receiver and low specific work of the TES system of 351 the traditional sCO₂ system are overcome. 352



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Figure 8 Variation of the sCO₂ mass flow rate with the turbine inlet temperature

The mass flow rate is also a crucial parameter for systems operation. A lower mass flow rate of the working fluid leads to a lower pressure drop in receiver and heat exchanger and more moderate irreversible loss in the compressor and turbine. The variations of the sCO_2 mass flow rate of the 10MW systems with turbine inlet temperature are presented in **Figure 8**. The mass flow rate of the

working fluid decreases with the elevation of the turbine inlet temperature for all cases. The mass 359 flow rate of the cascade systems is lower than that of the simple systems at the same turbine inlet 360 temperature and pressure. It decreases from 46.9kg/s at 550°C to 20.1kg/s at 900°C with the inlet 361 pressure of 35MPa, while for the simple sCO₂ system, it drops from 60.2 kg/s to 46.7 kg/s. 362 Furthermore, the sCO₂ mass flow rate of the cascade system is not sensitive to turbine inlet pressure. 363 364 The difference of the flow rates at 25 and 35 MPa is less than 2.0 kg/s at a given temperature for cascade system. While the difference is more remarkable for the simple sCO₂ system, which is 365 approximately 10kg/s in the simulation temperature range. 366



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Figure 9 Cycle efficiency variations of the power block subsystems with the turbine inlet

temperature

The cycle efficiency variations with turbine inlet temperature from 550° C to 900° C and pressure from 25MPa to 35MPa are presented in **Figure 9**. The cycle efficiencies both for sCO₂ and sCO₂-SR cascade systems increase with turbine inlet temperature and pressure. The cycle efficiency is elevated from 41.4% to 53.4% when the inlet temperature increases from 550°C to 900°C at inlet

pressure of 25MPa and it is improved from 53.4% to 54.6% with the pressure from 25MPa to 35MPa 374 at 900°C for simple sCO₂ cycle. By comparing the results for sCO₂ and sCO₂-SR systems, it is 375 indicated that the cycle efficiency of the sCO₂-SR cascade cycle is firstly higher than that of the 376 simple sCO₂ system when the temperature is below 630°C. The sCO₂-SR system shows a poorer 377 performance at the temperature higher than 630°C in terms of power conversion. It can be explained 378 by the inferior thermodynamic performance of the steam Rankine cycle and lower thermal grade of 379 the sCO₂-SR system due to the lower average endothermic temperature of the receiver. Less exhaust 380 thermal energy and lower exhaust temperature of the sCO₂-SR system at operation temperature can 381 compensate for the higher irreversible losses of steam Rankine cycle and lower thermal grade of the 382 cycle fluid, then presenting higher comprehensive cycle efficiency. 383

To explore the contribution of the power cycle subsystem and solar energy collecting subsystem on 384 the overall performance of systems, the heat gains of the tower receiver for two system 385 configurations are presented in Figure 10 at noon on the spring equinox in Dunhuang with the 386 incident solar irradiation of 700W/m². The heat gain of two systems decreases with the increase of 387 the turbine inlet temperature. The heat gain of the sCO₂-SR system is significantly higher than that of 388 simple sCO₂ system at high temperature. It can be explained by the lower operation temperature of 389 the tower receiver as shown in Figure 7. The heat gains of the tower receiver for simple sCO₂ and 390 cascade sCO₂-SR systems are 46.3 MWh and 53.4 MWh at the receiver outlet temperature of 900 °C 391 392 and pressure of 35MPa, respectively. The influences of the operation pressure on heat gain of the two systems are different. A higher outlet pressure tends to lower heat gain for the cascade system, which 393 is caused by the lower average solar tower receiver operation temperature described in Figure 10. 394 The results indicate that the proposed cascade system is promising in improving thermal conversion 395

396 efficiency of solar tower power technology.





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Figure 10 Heat gain of the solar tower receiver

In order to further study the thermodynamic irreversibility of the system, the irreversible loss of the 399 400 solar power systems can be divided into six parts associated with the solar field, solar tower receiver, turbine, compressor, cooler, sCO₂ heat exchangers. The losses of the sCO₂ heat exchangers cover all 401 exergy destruction in exhaust gas heat exchangers, including water preheater, regenerator, and boiler 402 403 as shown in Figure 5. Based on the aforementioned model and analysis, the exergy loss for the energy conversion process is presented in Figure 11 at a sCO₂ turbine inlet temperature of 900°C. It 404 can be observed that the solar field optical loss and photo-thermal conversion of the tower receiver 405 are the two biggest exergy losses of the systems. The exergy losses of the solar field for two systems 406 are the same. The exergy loss of the receiver of the cascade system is slightly higher than that of the 407 simple sCO₂ cycle. For the power cycle subsystem, the exergy losses of the compressor, cooler, 408 regenerator of the proposed cascade sCO2-SR systems are lower than those of the simple sCO2, while 409 the reverse is true for the turbine, heat exchangers and additional bottom cycle are the opposite of 410

411 aforementioned results.

The phenomenon of the above exergy loss destruction will be explained one by one. The exergy loss 412 of the receiver is increased from 38 MWh to 38.7 MWh. The reason for this phenomenon is that the 413 higher conversion efficiency of the cascade system receiver cannot compensate for the lower exergy 414 of working fluid resulting from the lower average temperature of the HTF. The sCO₂ possesses more 415 superior thermodynamics performance compared to the steam under current operation temperature, 416 resulting in a higher turbine loss of the proposed system. As shown in Section 4.1, the lower mass 417 flow rate of the sCO₂ in sCO₂-SR system leads to lower exergy loss of the sCO₂ compressor. Moreover, 418 the state of work fluid of the bottom cycle is liquid during compression; the exergy loss of pump is 419 significantly lower than that of the compressor. Thus, the total compressor or pump exergy loss of 420 the sCO₂-SR system is lower than that of the simple sCO₂ system. For cooler exergy loss, the 421 422 pre-cooler inlet temperature is only 366.0K for the sCO₂-SR system, while the inlet temperature of the simple sCO₂ is 415K. Meanwhile, the condenser temperature of the Rankine cycle is only 309K, 423 thus the total exergy loss of the cooler (includes pre-cooler and condenser) of the sCO₂-SR system is 424 significantly lower than that of the simple sCO₂ system due to a lower exhaust gas temperature. The 425 sCO₂-SR system has a better temperature match and lower heat transfer temperature difference in the 426 regenerator and boiler, leading to a lower exergy loss in the sCO₂ exchanger. 427







Figure 11 Exergy loss of the solar tower power systems

430 *4.2 Performance analysis of the power plants*

The operation parameters of the solar power system, including operation temperature, pressure and
solar irradiation, are the critical parameters to overall performance of the power system. The
influences of the aforementioned parameters on system performance are illustrated in this subsection. *4.2.1 Operation temperature and pressure*

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442 To illustrate the overall performance of the simple sCO_2 and sCO_2 -SR cascade cycle, including the 443 solar energy collecting subsystem, the electricity productions at noon on the summer solstice in

Dunhuang with the incident irradiation of 700 W/m² are analyzed as shown in Figure 12. The results 444 show that the electricity productions have the bell curve with a maximum value at the turbine inlet 445 temperature of 700~750°C for simple sCO₂ systems and 750~800°C for cascade system. The 446 electricity production and optimal temperature of the solar power systems are affected by the thermal 447 efficiency of the receiver and power cycle efficiency simultaneously. Solar power system 448 performance at high temperature is strongly dependent on the exergy loss of solar energy collecting 449 subsystems, particularly in solar receiver due to significantly increased convection and radiation heat 450 losses. The proposed sCO₂-SR system possesses lower average receiver operation temperature, thus 451 the positive contribution of the solar thermal efficiency improvement of the receiver has overpassed 452 the negative effect of lower power cycle efficiency, leading to higher electricity production and 453 optimal temperature. The electricity productions of the simple sCO₂ system and sCO₂-SR cascade 454 455 system are 25.2 MWh and 27.6 MWh at the turbine inlet temperature of 900°C and pressure of 35MPa under design condition. The electricity production of the cascade system is improved by 456 9.5%. The electricity productions increase with the increase of the maximum operation pressure for 457 both the simple sCO₂ and sCO₂-SR cascade cycle, but the impact is more appreciable in a lower 458 pressure range. It indicates that the turbine inlet pressure possesses a stronger effect on overall 459 performance especially at low pressure conditions. 460

461 *4.2.2 Solar irradiation*

Solar radiation is constantly changing throughout the year. Thus, solar irradiation plays an important role in overall performance and optimum operating temperature. The ratio of electricity production to the maximum electricity production W/W_{max} from 560 °C to 900 °C is selected as evaluation parameters to demonstrate the performance of the system under different temperatures and solar

irradiation condition. The W/W_{max} of the two systems is presented in Figure 13 with the turbine inlet 466 pressure of 35MPa. The peak electricity production temperatures increase with the increase of solar 467 radiation both for two systems. The temperature of peak electricity production of the simple sCO₂ 468 system is 580°C, 680°C, 740°C, 800°C when the corresponding incident solar irradiation is 469 300 W/m², 500 W/m², 700 W/m², 900 W/m². While the peak electricity output occurs at 640 °C, 740 °C, 470 800°C, 820°C for the cascade system. The reason for this phenomenon is that the power cycle 471 efficiency improvement at high solar incident irradiation can exceed the heat loss attenuation of the 472 tower receiver at high temperature, leading to higher optimal operating temperature. Furthermore, 473 the cascade system presents higher optimal electricity production and slight electricity attenuation 474 when the operation temperature deviates from the optimal temperature, especially at low solar 475 irradiation conditions. The W/W_{max} of the simple sCO₂ cycle decreases from 1 at 580°C to 0.56 at 476 900°C with solar incident irradiation of 300W/m^2 , while it only decreases from 1 at 640 °C to 0.84 477 at 900°C for the cascade system. It is indicated that the cascade systems can exhibit more superior 478 performance at off-optimal operation temperatures compared to simple sCO₂ system. The electricity 479 production improvement of the cascade systems at optimal temperature is only 5.8% with solar 480 incident irradiation of 300W/m², while it is 59.0% at 900°C with solar incident irradiation of 481 300W/m² compared to those of the simple system. Thus, the cascade system can give a more 482 excellent overall performance under various reference solar irradiations. 483





490 **4.3 Operation strategy adjustment**

The thermal storage system is not considered in aforementioned analysis. Aiming to combine the 491 thermal energy storage subsystem with the sCO₂ solar power system, the MS solar collecting loop is 492 introduced in solar tower receiver and the operation strategy of the cascade solar power system is 493 also analyzed. In this section, the power output of the power block is set as constant. To explore the 494 flexibility of the cascade system, this study assumes that the system can operate at full load when the 495 solar radiation is 500W/m² at the design point using single sCO₂ as HTF (i.e. the flow rate of MS in 496 the receiver is 0). If the incident solar irradiation is over 500 W/m², the sCO₂ and MS loop lengths are 497 adjusted according to the solar flux distribution of the receiver. The extra solar energy that cannot be 498 absorbed by the sCO₂ loop is collected by MS loop and stored in TES subsystem. While, the solar 499 incident irradiation is below 500 W/m², the HTF of the receiver loop is sCO₂ and its flow rate is set as 500 501 constant value that is the same as the flow rate under full load operating condition. The solar incident irradiation is not enough to heat HTF to the desired outlet temperature at lower solar irradiation, thus 502 the stored MS is used to preheat sCO₂, then preheated sCO₂ is further heated in tower receiver to 503 desired temperature. Obviously, the outlet temperature of the preheater, namely sCO₂ receiver inlet 504 505 temperature, varies with solar incident irradiation. Once the required sCO2 receiver inlet temperature is higher than the temperature of the MS at low solar irradiation condition (called critical solar 506 irradiation), the systems cannot operate at full-load condition, the cascade system is closed and the 507 508 operation strategy of the system is shifted to thermal energy storage mode, meanwhile the bottom steam Rankine cycle can choose whether to work or stop according to grid load using MS as the heat 509 source. Thus the operation mode of the cascade system can be classified into four modes, namely (A) 510 thermal storage mode (B) full-load operation without thermal storage (C) full-load operation with 511

thermal storage and (D) bottom partial-load mode using MS as the heat source. The calculation flow
charts for different operation Modes are presented in Appendix .

To exhibit flexible adjustment of the cascade system, the critical parameters of the cascade systems, 514 including energy to TES system, sCO₂ inlet temperature, and electricity production, are analyzed 515 when solar irradiation varies from 200 W/m^2 to 900 W/m^2 with the receiver outlet temperature of 516 800°C and pressure of 35MPa, as shown in Figure 14. In order to simplify the analysis process of 517 the influence of the solar irradiation on system operation strategy, the variations of the solar position 518 and solar concentration distribution of the tower receiver are assumed as identical under different 519 incident solar irradiation. The power capacities of the bottom steam cycle using exhausted sCO₂ and 520 MS as the heat sources are regarded as the same. The powers of the cascade system and the bottom 521 steam cycle are 18.6 MW and 9.2 MW. When the solar irradiation is below 315W/m², the required 522 sCO₂ inlet temperature of the receiver is higher than the temperature of the MS, thus the system shifts 523 to Mode A; while solar irradiation is between 315 W/m^2 and $500W/m^2$, the system can operate at 524 Mode B using stored hot MS for preheating sCO₂ and the preheating temperature (required sCO₂ inlet 525 temperature of the receiver) decreases with the increase of the solar irradiation; when solar 526 irradiation is higher than 500W/m², the system operates at Mode C. The cascade presents stable 527 electricity output and the thermal energy to thermal storage system increases with the increase of the 528 solar irradiation. In conclusion, the cascade system can still work at partial-load using MS as the heat 529 source and keep considerable electricity outputs (about 50% power of the full-load operation) at low 530 solar irradiation (<315W/m²) or no sun periods. The mass flow rate of the MS is also shown in 531 Figure 15. Furthermore, the operation Mode B and C also can convert to Mode A according to 532 electricity grid load. In brief, the cascade system overcome the shortcoming of the simple sCO₂ 533

systems, the thermal energy storage subsystem is combined with a high temperature sCO_2 cycle and operation stability is improved by using thermal energy storage systems. Thus, the cascade system is a promising solar power system to achieve a higher efficiency with stable electricity output and cost-effective thermal energy storage.



538

539

Figure 14 Operation mode of the cascade system





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Figure 15 Mass flow rate in receiver and preheater

542 In Mode A, the HTF of the receiver is MS, the MS flow rate increases with the solar incident irradiation. While the HTF of the receiver in Mode B is sCO₂, the sCO₂ is firstly preheated in a 543 preheater by the MS. The MS flow rate in preheater decreases with solar irradiation. There is a more 544 complex HTF flow adjustment in Mode C. The two different HTFs, MS and sCO2, are adopted in 545 the receiver. To maintain the stable operation of the power block, the mass flow of the sCO₂ is 546 constant under fluctuant solar irradiation by adjusting the length of the sCO₂ solar receiver tube loop 547 and corresponding length of the MS loop is also changed, leading to higher MS flow rate at higher 548 solar irradiation in Mode C operation. Based on above analysis, it can be observed that the solar 549 receiver length is assumed variable for different HTF under off-design condition with a constant total 550 length of the receiver tube. In this study, the authors focus on the feasibility investigation and 551 performance superiority of the novel solar tower system using cascade cycle. The detailed design of 552

the solar tower receiver is not discussed. The development of a flexible receiver that can adjustcollecting length under different solar irradiation will be focused on in future work.

555 **5.** Conclusions

A novel solar power system integrating with supercritical carbon dioxide Brayton-steam Rankine power cycle is proposed to pave a path toward large scale utilization of the supercritical carbon dioxide solar power system. The comprehensive system model is developed to evaluate system performance. The energy and exergy analysis of systems with different configurations are performed. Based on the analysis results, the following conclusions are summarized:

1. The cascade systems have a the lower receiver inlet temperature, wider temperature difference across the receiver, higher specific work of the TES system and lower mass flow rate of the working fluid. The solar-thermal conversion efficiency of the receiver is improved significantly by cascade sCO₂-SR systems. The heat gain of the tower receiver of the cascade system is 53.4 MWh, which is about 7.1 MWh more than that of the simple system for a 10MW solar tower power plant at design point.

Solar field optical loss and photo-thermal conversion of the tower receiver are the two biggest
exergy losses of the systems. The cooler and supercritical carbon dioxide heat exchanger exergy
losses are decreased significantly by the cascade systems.

570 3. The electricity productions show that cascade system is a promising option for central solar tower 571 systems due to higher optimal operating temperature and efficiency compared to simple supercritical 572 carbon dioxide systems. The electricity productions of simple and cascade systems are 25.2 MWh 573 and 27.6 MWh at 900°C and 35MPa with solar irradiation of 700W/m². The electricity production of 574 the cascade system is improved by 9.5%. The cascade system also shows slighter performance attenuation at off-optimal operation condition.

4. The cascade solar tower system possesses a more flexible operation strategy. The MS is employed
as thermal storage medium for achieving continuous and stable operation at the fluctuating condition.
The thermal storage issue of the supercritical carbon dioxide systems in the solar thermal power
application is solved.

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584 Appendix

In this study, the performance of the power plants that possess three different boundary conditions 585 586 that correspond to different systems operation strategy should be investigated. Firstly, the mass flow calculation of the HTF is presented in Figure A1 at the given inlet temperature, outlet temperature 587 and solar receiver loop length. Secondly, the preheating temperature calculation of the sCO₂ in **Mode** 588 **B** operation are presented in Figure A2 at the given mass flow rate, loop length and outlet 589 temperature. Finally, the length of the sCO₂ loop is variable in **Mode C**, the length calculation of the 590 sCO₂ loop in Mode C operation is presented in Figure A3 at the given mass flow rate, inlet and 591 outlet temperature. Thus, the extra length of the receiver tube is set as MS loop and the flow rate of 592 the MS can be calculated as Figure A1. The calculation procedure of the above three different 593 boundary condition is explained one by one as follows: 594

595 A.1 Mass flow calculation of the HTF

596 (1) Initial fixed values, including solar flux distribution of the receiver, dimension parameter of the

597 receiver and absorber tube, are input;

- 598 (2) Initial values of the mass flow *m*, inlet temperature T_{in} , and outlet temperature T_{out} are input;
- 599 (3) Initial values of the outer surface of the absorber temperature $T_{\rm abs,o}$ are input;
- 600 (4) With T_{absi} , *m*, Q_{abs} , Q_{conv} , Q_{cond} , and Q_{loss} are calculated by Eqs. (4–8) and (20);
- 601 (5) With the calculated Q_{conv} , Q_{cond} , and Q_{loss} , the new value of the outer surface of receiver tube 602 is calculated;
- 603 (6) Go back to Step (4). The calculation is carried out with the same process until the absolute 604 temperature difference of $T_{abs,o}$ and T_{abs} is below 0.1°C;
- 605 (7) Go back to Step (3). The calculation is carried out with the same process until a whole loop L of 606 receiver is evaluated;
- 607 (8) Go back to Step (3). The new value of mass flow rate is calculated. Calculation is carried out with
- same process until the absolute difference of T_{outi} and T_{out} is below 0.1°C;
- 609 (9) The simulation results are output.



610

611

Figure A1 Flow chart of the mass flow rate calculation

- 612 A.2 sCO2 preheating temperature calculation
- 613 (1) Same as **Appendix A.1**
- 614 (2) Same as Appendix A.1
- 615 (3) Same as Appendix A.1
- 616 (4) Same as Appendix A.1
- 617 (5) Same as Appendix A.1
- 618 (6) Same as Appendix A.1
- 619 (7) Same as **Appendix A.1**
- 620 (8) Go back to Step (3). The new value of inlet temperature is calculated. Calculation is carried out
- 621 with same process until the absolute difference of T_{outi} and T_{out} is below 0.1°C;
- 622 (9) The simulation results are output.



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625

626 A.3 sCO2 loop length L calculation



627

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Figure A3 Flow chart of the sCO2 loop length calculation

- 629 (1) Same as Appendix A.1
- 630 (2) Same as Appendix A.1
- 631 (3) Same as Appendix A.1
- 632 (4) Same as Appendix A.1
- 633 (5) Same as Appendix A.1
- 634 (6) Same as Appendix A.1
- 635 (7) Go back to Step (3). The calculation is carried out with same process until the absolute difference
- 636 of T_{outi} and T_{out} is below 0.1°C;
- 637 (8) The simulation results are output.

638

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Declaration of interests

 \boxtimes The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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