Near-bed and surface flow division patterns in experimental river bifurcations

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Understanding channel bifurcation mechanics is of great im-Abstract. 3 portance for predicting and managing multichannel river dynamics and avul-4 sion in distributary river deltas. To date, research on river channel bifurca-5 tions has focused on factors determining the stability and evolution of bi-6 furcations. It has recently been shown that, theoretically, the non-linearity 7 of the relation between sediment transport and flow discharge causes one of 8 the two distributaries of a (slightly) asymmetrical bifurcation to grow and 9 the other to shrink. The positive feedback introduced by this effect results 10 in highly asymmetrical bifurcations. However, there is a lack of detailed in-11 sight into flow dynamics within river bifurcations and the consequent effect 12 on bedload flux through bifurcating channels and thus the impact on bifur-13 cation stability over time. 14

In this paper, three key parameters (discharge ratio, width-to-depth ra-15 tio and bed roughness) were varied in order to examine the secondary flow 16 field and its effect on flow partitioning, particularly near-bed and surface flow, 17 at an experimental bifurcation. Discharge ratio was controlled by varying down-18 stream water levels. Flow fields were quantified using both particle image ve-19 locimetry and ultrasonic Doppler velocity profiling. Results show that a bi-20 furcation induces secondary flow cells upstream of the bifurcation. In the case 21 of unequal discharge ratio, a strong increase in the secondary flow near the 22 bed causes a larger volume of near-bed flow to enter the dominant channel 23 compared to surface and depth-average flow. However, this effect diminished 24 with larger width-to-depth ratio and with increased bed roughness. 25

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The flow structure and division pattern will likely have a stabilizing effect on river channel bifurcations. The magnitude of this effect in relation to previously identified destabilizing effects is addressed by proposing an adjustment to a widely used empirical bed-load nodal-point partition equation. Our finding implies that river bifurcations can be stable under a wider range of conditions than previously thought.

1. Introduction

River deltas contain key nodes where fluid and sediment are partitioned into smaller 32 channels and braided multi-channel river systems continually divide and bifurcate flow 33 around mid-channel bars. The mechanisms governing the division of flow and sediment 34 at these channel bifurcations essentially control downstream water and sediment parti-35 tioning and, in many cases, also results in an upstream backwater control see *Slingerland* 36 and Smith, 2004; Kleinhans et al., 2013, for review]. The control of flow and sediment 37 partitioning means that bifurcation evolution and stability is intrinsically linked with 38 these mechanics over time [Kleinhans et al., 2008] and, thus, play a significant role in 39 the evolution of deltaic systems [Wang et al., 1995; Kleinhans et al., 2008; Edmonds and 40 Slingerland, 2008]. Bifurcations are also a key control of braided river system behavior 41 [Repetto et al., 2002; Bolla Pittaluga et al., 2003; Federici and Paola, 2003; Bertoldi and 42 Tubino, 2005, 2007; Miori et al., 2006; Parsons et al., 2007]. Understanding river channel 43 bifurcation behavior is hence of great importance for managing fluvio-deltaic and braided 44 river plains, notably in prediction and management of flood risks and understanding the 45 evolution of braided river systems and river delta environments in the face of environmen-46 tal change. 47

The inherent instability of bifurcations has traditionally been explored and explained using numerical models and linear stability analysis [see review in *Kleinhans et al.*, 2013]. A qualitative description of the stability analysis is as follows. Given a nearly symmetrical bifurcation with one slightly deeper and one slightly shallower bifurcate, the slightly deeper bifurcate has a slightly higher discharge and flow velocity. As sediment transport is

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known to depend nonlinearly on flow velocity, the sediment transport rate in the deeper 53 bifurcate is somewhat larger than in the shallower branch. However, in the absence of 54 topographic or curvature-induced steering, the sediment supply in the upstream channel 55 is partitioned between the downstream channels in proportion to the bifurcate widths 56 [Bolla Pittaluqa et al., 2003]. Consequently, the upstream sediment supply to the slightly 57 deeper bifurcate is smaller than the transport capacity, and this dominant channel incises. 58 Channel deepening leads to a positive feedback wherein more water is drawn into the 59 dominant bifurcate and more incision occurs, whilst the subordinate channel has reduced 60 discharge and sediment transport capacity. As a result, the bifurcation is unstable and 61 will become increasingly asymmetric [Wang et al., 1995; Bolla Pittaluga et al., 2003]. A 62 key point of such linear stability analyses is that is evaluates the initial stability. As a 63 consequence, in the above example the channel widths are constant and equal for both 64 bifurcate channels. In erodible channels, the morphology will adapt to such cases over 65 time. The study in this paper focusses on how the morphology might adapt. 66

Further research focused on the effect of bifurcation angle [Klaassen and Masselink, 67 1992], the influence of downstream water surface slope boundary conditions [Wang et al., 68 1995; Kleinhans et al., 2013; Thomas et al., 2011], the morphological characteristics of bi-69 furcations initiated by bar formation [Bertoldi and Tubino, 2005, 2007; Federici and Paola, 70 2003; Repetto et al., 2002, the stability of bifurcations with erodible banks [Miori et al., 71 2006] and their evolution [Edmonds and Slingerland, 2009; Kleinhans et al., 2008, 2011], 72 and the effect of bends upstream of bifurcations [Kleinhans et al., 2008]. A curved channel 73 upstream of the bifurcation causes helical flow, which strongly affects the sediment trans-74 port direction [Kleinhans et al., 2008] and thus controls sediment partitioning. All these 75

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effects point to the importance of secondary flow structures, which modify the sediment partitioning between the two bifurcates. This suggests that a perturbation of the detailed flow structure at a perfectly symmetrical bifurcation may also trigger the destabilization of the bifurcation. Moreover, if a perfectly symmetrical bifurcation is not perturbed at the bed but within the inherited flow field, the detailed flow structure determines the partitioning of bed load transport and the initial aggradation or erosion of the downstream channels.

The objective of this paper is to investigate the detailed flow structure in a perfectly 83 symmetrical bifurcation that is perturbed by a slight difference in discharge conveyance 84 in the two bifurcate channels. We focus particularly on the near-bed flow direction as this 85 drives the sediment transport at the onset of bifurcation destabilization. The methodol-86 ogy is to perform detailed measurements in a symmetrical bifurcating flume. Here the 87 discharge partitioning can be unbalanced by adjusting the downstream weirs in both bi-88 furcate channels, which has the consequence that flow at the bifurcation is preferentially 89 curved towards the channel with the highest discharge. Helical flow intensity is inversely 90 proportional to the bend radius relative to the channel width and depth, and inversely 91 proportional to the Nikuradse roughness length (bed roughness) relative to channel depth. 92 Therefore, we further vary bed roughness and width to depth ratio. To isolate the effect of 93 the bifurcating planform from changes in depth or gradient advantages, we also performed 94 control experiments where the water depths were kept equal in the upstream channel and 95 both downstream channels. 96

Previous work with a similar setup by *Thomas et al.* [2011] showed that secondary
 flow cells develop in the bifurcate channels which flow towards the inner bank at the

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surface. Their work mainly investigated the effect of the internal bifurcation angle on the partitioning of the flow, which had little to no influence, and the flow structure in the bifurcate channels as result from a range of discharge divisions. An interesting observation in those experiments is that near-bed flow seemed to be steered stronger into the bifurcate channel with the highest discharge. Here we study this effect of flow steering just upstream of the bifurcation in detail in order to explore implications for sediment partitioning and

¹⁰⁵ bifurcation stability. In addition to similar flow measurements as in *Thomas et al.* [2011], ¹⁰⁶ we utilize Particle Image Velocimetry to elucidate the flow structure very near the bed. ¹⁰⁷ Building on these data we study overall flow structure and near-bed flow steering for a ¹⁰⁸ wide range of variables known to be relevant to bifurcation stability, namely discharge ¹⁰⁹ division, width-to-depth ratio and bed roughness.

2. Methods and Materials

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2.1. Experimental Setup

We conducted a series of experiments to systematically investigate the flow structure 110 in relation to three key variables. First, we varied the width-to-depth ratio (WDR) of 111 the incoming channel by lowering flow discharge and reducing downstream weir height 112 to maintain uniform flow conditions at the system scale. As wider, shallower, channels 113 tend to have lower secondary flow intensities the experiment was targeted at examining 114 the importance of WDR on flow partitioning at bifurcations. Second, within the WDR 115 experiments we also varied downstream water levels in the bifurcate channels in order 116 to introduce a gradient advantage for one channel. This led to asymmetric discharge 117 partitioning and strengthened secondary flows, allowing us to examine the interaction of 118 secondary flow with WDR under asymmetric conditions. Third, we varied bed roughness 119

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¹²⁰ by running experiments initially with a smooth bed and subsequently with an immobile ¹²¹ gravel bed. This set of experiments was designed to capture the dampening influence of ¹²² increased roughness on secondary flows and how this interacted with WDR in governing ¹²³ the mechanics of partitioning.

The experiments were conducted in a transparent Perspex bifurcation scale model 124 (Fig. 1a,b), with a 1.6 m-long, 0.5 m-wide inlet channel upstream of a bifurcation which 125 splits the flow into two 0.25 m-wide, 1.6 m-long, distributaries [the same model as the 126 54° setup used by Thomas et al., 2011]. The entire setup was tilted at a slope of $1 \cdot 10^{-3}$. 127 Water was pumped from a reservoir into a header tank. This header tank was filled at 128 a controlled rate from below and contained a layer of rocks at the bottom to break any 129 flow structure present from the water flowing in. From the header tank, the water flowed 130 downstream through a series of flow straightening baffles into the upstream channel of 131 the flume. The inlet flow was tested and adjusted to ensure the best possible upstream 132 boundary conditions as will be demonstrated with measurements. 133

The water level and water surface slope were controlled by two weirs, one at the downstream end of each of the bifurcate channels. The water plunged over the control weirs from the bifurcate channels into a reservoir. The flow rate was adjusted until uniform flow conditions were achieved within the system. This was achieved by equalizing the water depths in the inlet channel and downstream distributaries just upstream and downstream of the bifurcation, respectively.

¹⁴⁰ A total of eight experiments were performed (Table 1), varying three parameters: width-¹⁴¹ to-depth ratio (WDR), discharge ratio (Qr) and bed roughness. Experiments were con-¹⁴² ducted with two different WDRs namely 6.3 and 14.3, the latter representing conditions

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found in natural systems such as the Cumberland Marshes, Canada [Edmonds and Slinger-143 land, 2008] and the Columbia River, Canada [Kleinhans et al., 2012]. For these ratios, 144 water depths of 80 and 35 mm were used, abbreviated as 80xxx and 35xxx herein. Both 145 equal (nnEQ) and unequal (nnNEQ) discharge divisions were examined; discharge ratios 146 of Qr=1 and about Qr=1.5 were used. Downstream weirs were used to control discharge 147 ratio and water depth in each bifurcate. For the equal discharge division runs, discharge 148 and weir heights were adjusted to acquire the required water depth and uniform flow 149 conditions. Experiments with unequal discharge division were always run with the same 150 discharge as their equal counterparts; in these runs uniform flow was acquired by varying 151 weir heights. The backwater adaptation length (*Ribberink and Van Der Sande* [1985]; 152 Parker [2004] also see Kleinhans et al. [2013] for importance in bifurcations, sometimes 153 named backwater length or backwater effect), estimated by $\lambda_{bw} = h/3S$ (h is water depth, 154 S channel slope), equals $27 \,\mathrm{m}$ for the low width-to-depth ratio, and $12 \,\mathrm{m}$ for the high 155 width-to-depth ratio experiments. These values are longer than the entire flume, justify-156 ing using downstream weirs to control the division of water at the bifurcation. Individual 157 runs were repeated to allow data collection with different techniques. 158

¹⁵⁹ All the experiments described above were conducted with a smooth bed as well as with a ¹⁶⁰ rough bed; experiments with a rough bed are indicated with the suffix _S for sediment. For ¹⁶¹ the experiments with a rough bed, a 15 mm-thick immobile layer of 3-8 mm ($D_{50} = 5$ mm) ¹⁶² white gravel was installed at the bed of the model. The same water depths and discharge ¹⁶³ ratios were used for the runs with sediment; water levels were measured relative to the ¹⁶⁴ top of the gravel bed to retain the same width-to-depth ratio. To ensure uniform flow, but ¹⁶⁵ to retain the same WDR, experiments 35EQ_S and 35NEQ_S and experiments 80EQ_S

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and 80NEQ_S were run at about 60% and 80% of the discharge of their smooth bed counterparts, respectively. This reduced discharge is caused by slower flow induced by the increased roughness.

2.2. Data Acquisition

¹⁶⁹ 2.2.1. Flow Velocity Vectors (UDVP)

A series of measurements were taken from a total of 4 cross-sections distributed through-170 out the model domain (Fig. 1c). 1D flow velocities were measured sequentially in the 171 streamwise Ux, cross-stream Uy and vertical Uz directions at each cross-section (Fig. 1c) 172 using an ultrasonic Doppler velocity profiling (UDVP) system [Takeda, 1991, 1995]. A 173 Met-Flow UVP-XW ultrasonic velocity profiler was used to record a multiplexed signal 174 from an array of 4 MHz ultrasonic transducers. The locations of the measurements were 175 chosen such that the individual signals could be combined into time-averaged 3D flow 176 velocity vectors for each cross-section. The positions of the transducers are described in 177 detail in the following paragraphs (also see Fig. 1d). 178

For the measurement of both Ux and Uy, 7 UDVP transducers were used. These 179 transducers were placed at a distance of 10 mm from each other. For the lower WDR 180 runs (runs 80xxx), all 7 transducers were used to measure flow velocities. For the higher 181 WDR runs (runs 35xxx) only 3 transducers were submerged due to the shallower water 182 depth. For the measurement of cross-stream velocities, the transducers were mounted on 183 the outside of the Perspex flume wall and sounded the flow using acoustic coupling gel to 184 prevent distortion of the acoustic signal through the flume walls. In the upstream section, 185 the cross-stream measurements were repeated from both sides. Streamwise velocities 186 were measured by inserting the stack of probes in the flow 100 mm downstream of the 187

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actual position of the cross-section in order to minimize the influence of the probe on the measured flow field. Measurements for Ux were taken at 16 locations per crosssection in the upstream channel (see Fig. 1d) and at 8 locations per cross-section in the bifurcate channels (effectively splitting the measurement location shown in Fig. 1d). For the measurement of Uz, 16 UDVP transducers were used in the upstream channel and 8 in the bifurcate channels. Transducers were mounted to be only slightly submerged. Locations corresponded with the location of Ux measurements.

The measured streamwise flow velocities Ux were in the range of 40 to 240 mm/s for 195 the low-WDR runs and 10 to 200 mm/s for the high-WDR runs. The majority of cross-196 stream flow velocities Uy were in the range of -10 to 10 mm/s for the low-WDR runs and 197 -5 to 5 mm/s for the high-WDR runs. Vertical flow velocities Uz were in the range of -4198 to 4 mm/s for the low-WDR runs and -1 to 1 mm/s for the high-WDR runs. These fell 199 well within the measurable range (Table 2), Ux and Uy were high compared to the flow 200 velocity resolution. Values for Uz come quite close to the minimum measurable value in 201 the high-WDR runs. 202

For every measurement location, a total of 512 samples were collected, this value was 203 determined using a method to estimate the optimal record length for turbulent flow, as 204 described by Buffin-Bélanger and Roy [2005]. By analysis of convergence of the measured 205 velocity to a mean value. Each transducer was set to record 1D velocities in a profile 206 at 64 distances from the probe. These profiles spanned different lengths for the different 207 measurement orientations and locations: 510 mm for cross-stream measurements in the 208 upstream channel, 256 mm for cross-stream measurements in the downstream channels, 209 200 mm for streamwise measurements and 98 mm for vertical measurements (see Table 2 210

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for full set of properties). Streamwise measurements were obtained at a distance of 100 211 mm upstream from the probe, which matched the locations of the cross-stream velocity 212 measurements, which is the actual location of the cross-section. This then allowed co-213 located time-averaged velocity vectors to be combined along each of the cross-sections. 214 For the cross-sections in the upstream channel, the cross-stream velocity was measured 215 from both sides of the channel subsequently. At every vector location in each section, the 216 two available values for the cross-stream component taken from either side were compared. 217 If the difference of the two values was within one standard deviation of all cross-stream 218 values, the mean of these values was used. Otherwise, the value with highest magnitude 219 was used. This procedure was followed because in the cross-stream data, vertical bands 220 with zero flow velocities were present in some of the data. It is likely that acoustic 221 reflections from the opposite flume boundary caused these bands. An occasional large 222 difference in the two values is likely to be the result of this effect. 223

224 2.2.2. Near-bed and Surface Flow Fields (Particle Image Velocimetry)

For all model runs Particle Image Velocimetry (PIV) [see Adrian, 1991, 2005] was used 225 to record 2D near-surface flow velocity vectors in the streamwise Ux and cross-stream 226 Uy directions. This was achieved through introduction of about 15,000 floating particles 227 $(\rho_s = 660 \,\mathrm{kg}\,\mathrm{m}^{-3}, d = 2.0 - 2.5 \,\mathrm{mm})$. Additionally, for runs with a smooth bed, near-bed 228 velocities were also measured using PIV using about 10,000 denser ($\rho_s = 1360 \,\mathrm{kg}\,\mathrm{m}^{-3}$, 229 $d = 2.5 \,\mathrm{mm}$) particles. In contrast to classic PIV techniques with neutrally buoyant 230 small particles and laser sheets, we applied PIV methods to slightly larger floating surface 231 particles and sinking particles at the channel bed (c.f. Jodeau et al. [2008]; Blanckaert et al. 232 [2013]). Note that the PIV data were collected in repeated runs and not simultaneously 233

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with the UDVP data. For both the near-surface and near-bed measurements PIV involved 234 uniformly feeding black particles into the inlet channel over a period of about 10 s. A 235 digital SLR camera with High Definition (HD) video capabilities (Canon EOS 550D) with 236 a low-distortion wide angle lens (Canon EF-S 10-22 mm @ 20 mm) was used to record the 237 movement of the particles during the run. The camera was mounted perpendicular to 238 the flume in the centre of the channel just upstream of the bifurcation head (Fig. 1c). 239 The camera was set to shoot HD video $(1080 \times 1920 \text{ at } 29.97 \text{ fps})$. Three 500 W halogen 240 lamps, shielded to prevent reflections at the water surface, illuminated the measurement 241 section. Single frames were extracted from 15-20 s of video from each run, resulting in 242 450-700 individual frames. For all runs, images of different water levels were used to 243 create image masks to remove areas outside the actual flow field. These masks represent 244 the with of the flume for the different water levels, and effectively correct for vertical 245 relief-displacement. As the water surface is near-flat, the camera was positioned level 246 and centered above the flume, and the used lens features minimal distortions, no further 247 lens corrections were applied to the image to maintain image sharpness. The main source 248 of optical distortion in these images is at the sides in the runs where we filmed bed-249 particles through the water. This distortion is minimal straight below the camera, which 250 is the area just before the bifurcation. A rectangular region centered on the inlet channel 251 with the bifurcation head as a fixed point was cropped out of the masked image. The 252 resulting image was converted to 8-bit grayscale, inverted and a pixel value threshold 253 was then applied to remove irregularities introduced by the bed and walls. Lighting 254 irregularities were minimal relative to the high contrast between the black particles and 255 white background. 256

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For every pair of consecutive images, flow velocities were calculated using the Mean 257 Quadratic Difference method. This method was chosen as it gives better results in record-258 ings with a high particle density [Gui and Merzkirch, 1996; Merzkirch and Gui, 2000]. 259 Velocity vectors were calculated in MATLAB using a bespoke toolbox [based upon Mori 260 and Chanq, 2003 using sampling windows of 32×32 pixels. This method uses a sub-pixel 261 estimate of particle location based on pixel values. The pixel size is about 0.5 mm which, 262 with a 30 fps frame rate, yields a theoretical minimum velocity resolution of $0.05 \,\mathrm{mm \, s^{-1}}$. 263 Vectors were spaced such that each dataset contains 32 vector per channel width, which 264 corresponds to a vector spacing of 32 pixels for the low WDR runs (80xxx) and 30 pixels 265 for the high WDR runs (35xxx, Table 1), resulting in overlap of 1 pixel at each side of the 266 sampling window in the high WDR runs. The magnitude of the vectors were corrected 267 for the different field of views for the different water heights. Filtering was applied to 268 the velocity time series at every vector location, resulting in all spurious vectors outside a 269 range of 2 standard deviations from the local mean being removed from the dataset. This 270 filtering resulted in the removal of about 10% of the vectors in the surface measurements 271 for the smooth-bed runs and about 35% of the rough-bed runs. For the near-bed mea-272 surements of the smooth-bed runs, about 5% of the vectors were filtered. The quality of 273 this method seems related to artifacts introduced by visible shadows as result from the 274 gravel in the setup. The mean values per time series were used in further analysis. Note 275 that no spatial filtering or any form of interpolation was performed on the data. 276

2.3. Data Analysis

217 2.3.1. Discharge and (Depth-) Averaged Velocities

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The measured UDVP data were used to calculate cross-sectional discharge and average flow velocity vectors. The average flow velocity was calculated for each measured crosssection *cs* and at each measured depth profile *y*. The cross-sectional discharge Q_{cs} (m³/s) was calculated by summing the products of stream-wise flow velocity measurements Ux(m/s) and their effective area *a* (m²):

$$Q_{cs} = \sum_{y=1}^{n_y} \sum_{z=1}^{n_z} \left(U x_{y,z} \cdot a_{y,z} \right)$$
(1)

²⁸³ Where *a* is calculated from the distances from the centers between measurement lo-²⁸⁴ cations or the flow boundaries at the outer edges. The cross-sectional averaged velocity ²⁸⁵ $U_{av,cs}$ (m/s) is the discharge through that cross-section (Q_{cs}) divided by cross-sectional ²⁸⁶ area $A = W \cdot H$ (m²).

$$U_{av,cs} = Q_{cs}/A \tag{2}$$

The discharge passing through the upstream sections CS01, CS02 and CS03, and the summed discharge of both downstream sections CS04L and CS04R were evaluated for continuity by calculating the root-mean-square (RMS) deviation from the mean discharge \bar{Q} of all four sections.

$$Q_{rms} = \sqrt{\frac{1}{n} \sum_{cs=1}^{n} \left(\bar{Q} - Q_{cs}\right)^2} \tag{3}$$

At each measured vertical profile y the discharge per unit width qx_y (m/s) was calculated in a similar way as the cross-sectional discharge:

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$$qx_y = \sum_{z=1}^{n_z} \left(Ux_{y,z} \cdot h_z \right) \tag{4}$$

where h_z is the effective height of each measurement. For the depth-averaged flow velocity vectors $Ux_{av,y}$, the discharge per unit width qx_y was divided by the flow depth H:

$$Ux_{av,y} = qx_y/H \tag{5}$$

Equations 4 to 5 were also applied to attain depth-averaged cross-stream flow velocities $Uy_{av,y}$ by substituting streamwise flow velocities Ux by cross-stream flow velocities Uy.

²⁹⁸ 2.3.2. Streamwise Circulation and Planar Vorticity

²⁹⁹ UDVP measurements were used to calculate the streamwise circulation at each cross ³⁰⁰ section. PIV data were used to calculate the planar vorticity field for both the surface as ³⁰¹ well the near-bed measurements.

³⁰² The streamwise circulation Γ of a flow is a measure of the amount of rotating secondary ³⁰³ flow field in a cross section. The circulation is calculated by taking the area integral of ³⁰⁴ the two-dimensional vorticity (ω , in the y-z plane) per cross section:

$$\Gamma = \int_{z} \int_{y} \omega \, dy dz \tag{6}$$

where $\Gamma(m^2 s^{-1})$ is the circulation and $\omega(rad \cdot s^{-1})$ is the vorticity which is defined as the curl of a vector field:

$$\omega = \nabla \times \vec{\mathbf{u}} \tag{7}$$

where $\vec{\mathbf{u}}$ is a 2D vector field of cross-stream and vertical flow velocities Uy and Uz from 307 UDVP measurements. 308

In order to compare the circulation for different cross sections, the circulation is com-309 puted using the absolute values of the vorticity ($\omega = |\omega|$ in Eq. 6). The vorticity is 310 normalized using the method of van Balen [2010, p.77]: 311

$$|\hat{\Gamma}| = |\omega| H / (A \cdot U_{av,cs}) \tag{8}$$

where $|\hat{\Gamma}|$ is the absolute normalized circulation and A is the cross-sectional area. 312

Details of the secondary flow structure are also shown by the planar vorticity (in the 313 x-y plane) using Eq. 7, but using cross-stream flow velocities (Uy) and downstream flow 314 velocities (Ux) for vector field $\vec{\mathbf{u}}$, taken from PIV measurements of the surface flow and 315 near-bed flow. 316

2.4. Data Quality

2.4.1. Development of turbulence 317

We analysed the UDVP data at CS01 to see whether a turbulent flow developed. Tur-318 bulent flow conditions result in a logarithmic velocity profile. We tested if such profile 319 existed in the measured flow velocities. At each vertical profile y we applied a logarithmic 320 regression to predict the stream-wise flow velocity \hat{Ux} from the height above the bed z: 321

$$\hat{U}x(\log(z)) = a_0 + a_1\log(z)$$
 (9)

We analysed these profiles visually and we indicate how good the data fits the model 322 with the coefficient of determination R^2 , which is calculated as: 323

$$R^{2} = 1 - \frac{\sum \left(Ux(z) - \hat{U}x(z)\right)^{2}}{\sum \left(Ux(z) - \overline{Ux}\right)^{2}}$$
(10)

where \overline{Ux} is the average flow velocity in the profile under consideration.

³²⁵ 2.4.2. Scaling assessment

We used the Froude number, Reynolds number and Weber number to evaluate the hydraulic behavior of our experiments. We evaluated these values from UDVP measurement in the upstream section of the experiment. The Froude number (Fr) determines if the flow is affected by downstream or only by upstream disturbances, respectively subcritical (Fr < 1) or supercritical (Fr > 1) flow. Subcritical flow conditions are desirable.

$$Fr = \frac{U}{\sqrt{gH}},\tag{11}$$

where, g the gravitational acceleration (9.81 m²/s). The Reynolds number (Re) indicates if the flow is turbulent (Re > 2000) or laminar (Re < 500), with a transition zone in between:

$$Re = \frac{UR}{\nu},\tag{12}$$

where R is the hydraulic radius (m), $R = (H \cdot W)/(2H + W)$, ν is the kinematic viscosity of water (m²/s), $\nu = 4 \cdot 10^{-5}/(20 + t)$, where t is the temperature (18°C for the current experiments). We aim for turbulent flow in our experiments.

The Weber number (We) shows the relation between inertia and surface tension forces [*Peakall and Warburton*, 1996]. Critical values for the Weber number are uncertain and vary from 10-100, so we aim for values above this range.

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$$We = \frac{U^2 \rho H}{\sigma},\tag{13}$$

where σ is the surface tension. We used an estimate of $\sigma = 6 \cdot 10^{-3} \text{ N/m}$ in our experiments as opposed to the value of $7 \cdot 10^{-2} \text{ N/m}$ for water because we used soap in the water to reduce the surface tension.

3. Results

3.1. General Flow Structure

The following key flow field properties were derived from UDVP data (Table 3): (1) all equal weir runs had equal (50/50) discharge division; (2) all unequal weir runs had a discharge division close to 40/60. The measured discharge was less uniform for the shallower runs with a rough bed (Q_{RMS} , Table 3), which is probably due to the higher levels of noise present in the UDVP measurements for these runs.

3.2. Effect of Flow Division on Flow Structure

In the low WDR smooth bed runs with equal discharge division (Run 80EQ), the high 348 velocity core was positioned in the center of the channel (Fig. 2). In the unequal discharge 349 division case (80NEQ), the flow velocity core was located to the right-hand side in the 350 two downstream cross-sections (Fig. 3), the side with the gradient advantage and largest 351 discharge. In both the equal and unequal cases (80EQ, 80NEQ), two opposed secondary 352 flow cells were present in the channel upstream of the bifurcation. These cells flowed 353 towards the center of the channel at bed level and towards the banks at the water surface 354 (Fig. 2a-b, 3a-b). However, in the unequal discharge division case, the cell at the side 355 of the channel with the highest discharge was smaller (Fig. 3a-b). In both cases, the 356

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division of flow becomes visible in CS02 and dominates the flow structure in CS3. In the latter, the rotational flow cells are almost absent (Fig. 2c, 3c). For a large portion of the width (about 80%) in the unequal discharge division case, the flow structure caused the near-bed velocities to be oriented towards the channel with the water surface gradient advantage (Fig. 3c Fig. 6b). Note that a flow direction towards the right channel does not mean that this flow indeed enters the right channel as we will discuss later.

In both bifurcate channels, most velocity vectors were consistently directed towards the inner bank while the near-bed vectors were directed towards the outer banks (Fig. 2d-e, 3d-e). This flow structure had an inverse direction of rotation compared to the flow cells upstream of the bifurcation.

The PIV vectors obtained for the near-surface and near-bed flow reveal a more detailed 367 flow field in the horizontal plane than the UDVP data (Figs. 7 and 8), especially in the area 368 just upstream of the bifurcation (the downstream-most UDVP section (CS03) is located 369 at x=431 mm in Fig. 7 and 8). In this zone, the flow divergence and steering into the 370 bifurcate channels becomes even stronger than at the locations observed with UDVP data 371 (Fig. 7). Moreover, near-bed flow accelerates closer to the bifurcation (Fig. 8b,d). Indeed, 372 just upstream of the bifurcation (x = 550 mm, Fig. 8) the near-bed velocity vectors were 373 almost perpendicular to the outer banks in both cases with unequal discharge division 374 (nnNEQ). 375

Flow division lines (Fig. 9) were derived from the near-surface (Fig. 7) and near-bed velocity vectors (Fig. 8). These lines indicate the spatial location of the division of incoming near-surface and near-bed fluid into the two bifurcate channels. Important observations from these divisions include: 1) in symmetrical bifurcations both the discharge

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ratio, Q_{right}/Q_{total} , and the near-bed division ratio, $q_{bed,right}/q_{bed,total}$, were about 50%; 2) in asymmetrical bifurcations $q_{bed,right}/q_{bed,total}$ (71%) was much greater than Q_{right}/Q_{total} (62%) (Table 3); and 3) the majority of this division of near-bed flow occurred within a distance of about one channel width upstream of the bifurcation (Fig. 9b).

3.3. Effect of Width-to-depth Ratio on Flow Structure

Similar flow features described above were also observed in the higher WDR runs 35EQ 384 and 35NEQ (see Fig. 4,5 and 6c-d), although some differences exist. There is no high 385 flow velocity core in the middle of the channel, but the highest flow velocities are spread 386 over a larger part of the channel (Fig. 4c). There are actually two locations with higher 387 velocities in the left and right part of the upstream channel, which can be related to the 388 highest velocity core in the bifurcate channels. Also in the unequal discharge case, the 389 stream-wise velocities develop toward one core of flow velocity on the side of the channel 390 with the largest discharge (Fig. 5c). The secondary flow structures upstream of the 391 bifurcation consists of two counter-rotating flow cells in the middle of the channel flowing 392 towards the banks near the bed (Fig. 4a). Additionally, a third and fourth flow cell 393 seems to be present near the banks which flow towards the banks near the water surface 394 (Fig. 4a). The secondary flow structure in the middle of the channel in opposite direction 395 as observed in the low-WDR runs. However, this flow structure has the same structure in 396 respect to the cores of highest flow velocity, which are two in the high-WDR case on either 397 side of the channel and just one in the middle in the low-WDR runs. These flow cells 398 were not observed in the unequal discharge division high-WDR run 35NEQ (Fig. 5). The 399 rotation of these cells is mostly inferred from the cross-stream flow as vertical flow is close 400 or even under the measurement limit. The splitting flow structure closer to the bifurcation 401

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⁴⁰² and flow cells in the bifurcate channels are comparable to the structure observed in the ⁴⁰³ low-WDR runs and suppress the flow cells closer toward the bifurcation (Fig. 4b-c).

There was no clear difference in the direction of near-bed and depth-averaged flow 404 (Fig. 6c-d). However, a divergence of surface water was observed in the zone just up-405 stream of the bifurcation (between x=400 mm and the bifurcation) in both the low-WDR 406 runs (80EQ, 80NEQ, Fig. 7a-b) and high-WDR runs (35EQ, 35NEQ, Fig. 7c-d), but this 407 diversion extended farther upstream and was significantly more pronounced in the low-408 WDR runs. Indeed, near-surface velocities are affected by the unequal discharge distribu-409 tion at a distance of about one channel width upstream of the bifurcation in the low-WDR 410 run (80NEQ, Fig. 9b) and about half a channel width in the high-WDR run (35NEQ, 411 Fig. 9b). Interestingly, the low-WDR has less impact upon near-bed cross-stream flow 412 velocities than on the near-surface flow. This effect is shown in terms of flow division 413 (Fig. 9, Table 3): in the high WDR run (35NEQ), a larger proportion of the near-surface 414 flow enters the bifurcate channel with a gradient advantage $(q_{surf,right}/q_{surf,total} = 62\%)$ 415 whereas in the low WDR run this is somewhat lower $(q_{surf,right}/q_{surf,total} = 56\%)$. The 416 same holds for near-bed flow, but with a smaller difference observed between the two 417 runs $(q_{bed,right}/q_{bed,total} = 71\%$ and $q_{bed,right}/q_{bed,total} = 68\%$ for runs 80NEQ and 35NEQ, 418 respectively). 419

3.4. Flow Circulation

⁴²⁰ Upstream of the bifurcation, there were two counter-rotating flow cells with upwelling ⁴²¹ flow in the middle of the channel in the low-WDR runs. These cells were symmetrical in the ⁴²² symmetrical bifurcation (Fig. 2a) and were unequal in size in the asymmetrical bifurcation ⁴²³ (Fig. 3b). In the high-WDR runs, two counter rotating flow cells with downward flow in

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the middle and two weaker flow cells with downward flow near the banks on either side 424 were observed in the symmetrical run (Fig. 4a), but this structure was not observed in the 425 unequal discharge run (Fig. 5a). In all cases these flow cells were suppressed by splitting 426 flow closer to the bifurcation. Downstream of the bifurcation, a single flow cell was present 427 in each bifurcate channel with flow towards the outer bank near the channel bed (Fig. 2d-428 e,3d-e,4d-e,5d-e). The magnitude of circulation consistently increased downstream of the 429 bifurcation in all runs (Fig. 10). Earlier results [Thomas et al., 2011] already show the 430 inversion of direction and increase in magnitude of flow rotation in the bifurcate channel. 431 This effect is attributed to super-elevation of the water surface at the bifurcation point. 432

The low WDR runs (80xx) had a higher relative circulation than the high WDR runs 433 (35xx) (Fig. 10). For unequal discharge division cases, the subordinate left channel (gra-434 dient disadvantage and thus lower discharge) had a 20-50% larger intensity of normalized 435 circulation than the dominant right channel (Fig. 10). In the equal discharge division 436 cases, there were differences in circulation between the bifurcate channel, however these 437 were small and not always stronger in the same channel (Fig. 10). Perhaps the most 438 notable difference was for 80NEQ, which is likely to have the strongest transverse flow 439 velocities because of the low WDR and smooth bed. 440

The planar vorticity of the flow field show the presence of rotating cells in the smooth bed runs (Fig. 11a-d). The general pattern corresponds with the flow structures observed in the UDVP data, with the presence of two counter-rotating flow cells in the low-WDR runs (Fig. 11a-b) and the presence of two additional cells in the high-WDR runs (Fig. 11cd). The main vorticity pattern in the low-WDR runs corresponds with a high flow velocity core in the middle of the channel and slow flow on the sides, which results in rightward

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vorticity on the right-hand side of the channel and towards the left on the left-hand side. 447 In the high-WDR runs, there is no concentrated velocity core in the middle of the channel, 448 the high velocity is more spread over a larger area. In this case, the planar vorticity pattern 449 shows the pattern of the the secondary flow structure, which are multiple cells of rotating 450 flow cells. In both cases, the planar vorticity pattern follows the streamline curvature. 451 The pattern of planar vorticity in the near-bed flow (Fig. 12) also shows a banded pattern. 452 However, there are more small-scale features. These patterns do not resemble the pattern 453 of flow cells observed in the surface data. Additionally, these patterns also show dividing 454 and splitting circulation bands. 455

Spatially averaged vorticity (Fig. 13) shows the average planar vorticity pattern in the 456 upstream reach. The large-scale vorticity pattern for the low-WDR runs is consistent 457 for both the equal and unequal discharge division and both smooth and rough bed runs 458 (Fig. 13a). This pattern is the result of a high-flow velocity core in the center of the 459 upstream channel which curves towards the outer banks and is consistent with the flow 460 structures observed in the cross-section. The vorticity pattern in the high-WDR runs 461 shows local vorticity patterns superimposed on a large-scale vorticity pattern (Fig. 13b). 462 This pattern is consistent with local flow structures, as also observed in cross-section data 463 (Fig. 4, 5). Vorticity of the near-bed flow show a local pattern without a large-scale 464 structure (Fig. 13c,d). 465

3.5. Effect of Bed Roughness on Flow Structure

In the runs with a rough bed (nnxxx_S), the deviations of the near-bed velocity from the depth-averaged velocity in the low-WDR rough bed experiments were similar as their smooth-bed counterparts (Fig. 6e,f, 80EQ_S, 80NEQ_S). Flow velocities were lower in the

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rough-bed cases. Additionally, the decrease in flow velocity towards the bed is stronger for
the rough bed cases. The general flow structures were similar to those in their smooth-bed
counterparts but were lesser in magnitude (Fig. 7e-h).

The high WDR, rough bed experiments (Fig. 6g,h, 35EQ_S, 35NEQ_S) showed sig-472 nificant levels of noise induced by acoustic interference between the rough bed and the 473 UDVP. In the rough bed runs, the upstream influence of the bifurcation extends for only 474 half the distance observed in their smooth bed counterparts. Near-surface flow is divided 475 more equally between the distributaries (Fig. 9, Table 3, $q_{bed,right}/q_{bed,total} = 55\%$ for run 476 80NEQ_S) and almost equal in the higher WDR run $(q_{bed,right}/q_{bed,total} = 51\%$ for run 477 35NEQ_S). Unfortunately, the near-bed flow field could not be quantified using PIV be-478 cause of entrapment of particles in the bed sediment. Compared to the smooth bed runs, 479 similar vorticity patterns are visible in the rough bed cases, although these are noisier 480 (Fig. 11e-h). The effect of bed roughness is dependent upon the WDR: in the low WDR 481 runs, both the smooth and rough beds show similar banding of comparable magnitude 482 (Fig. 13a) whereas in the high WDR runs the rough bed shows similar banding, but at 483 about a 2-4 times higher magnitude (Fig. 13b, pale colored lines). This comparison shows 484 that stronger flow structures emerged preferentially in channels with a larger width-to-485 depth ratio, but is reduced in channels with a larger ratio of roughness length to water 486 depth. 487

4. Discussion

4.1. Scaling Assessment and Robustness of Methods

In all experimental runs, the flow was subcritical with Froude numbers between 0.1 and 0.3 (Table 3). The Reynolds number was well above the threshold for turbulent flow

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(Re > 2000) in all low-WDR runs and in the smooth bed high-WDR runs. Re values for 490 the high-WDR runs with rough bed, equal discharge division (35EQ_S) are closer to, but 491 still above 2000. Run 35NEQ_S had a Reynold number slightly below 2000 (Table 3). 492 The same is shown by the flow velocity profiles at the most upstream cross-section: the 493 measured flow velocity profiles show a well-developed logarithmic profile in all low-WDR 494 runs (Fig 14a) and in the high-WDR, smooth bed runs (Fig 14b, closed symbols). The 495 high-WDR, rough bed runs show more scattered velocity profiles (Fig 14b,c open squares), 496 which is most probably due to noise in the measurements due to the high amount of 497 acoustic scattering on the rough bed and the limited water depth. Nevertheless the 498 Reynolds number is in the upper end of the transitional regime and the velocity profiles 499 show no indication of laminar flow so we believe these experiments to have had fully 500 turbulent flow. 501

⁵⁰² Deviations from the logarithmic profile are apparent close to the flume wall (Fig 14a, ⁵⁰³ profile 1). The deviation from a logarithmic profile is visible in all measurements and ⁵⁰⁴ most prominent in the smooth bed, low-WDR runs (Fig 14c, closed circles). This wall ⁵⁰⁵ friction effect is expected and is perhaps even more important in natural channels.

In small-scale experiments, surface tension might have an effect on the dominant acting processes. In our experiments, however, the relative importance of the fluid's inertia to the surface tension is very low as the Weber number is above the critical value of 100 for most runs and well above 10 for the high-WDR, rough bed cases. Note that the reported critical values are not consistent [*Peakall and Warburton*, 1996].

⁵¹¹ We compared the streamwise velocity from UDVP measurement closest to the water ⁵¹² surface to the surface PIV data at the same location (Fig. 15). Please note that these two

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things do not measure the same flow, but this provides a way to see whether there are issues with any of the data. Most measurements are close to being equal, with a tendency of the PIV data to be slightly higher. The main difference are the rough bed high-WDR runs. As stated above, we consider the UDVP data for these runs to be noisy.

4.2. Implication for Bifurcation Instability

Flow structure at bifurcations is determined by (1) flow forcing by streamline curvature, 517 angular divergence upstream and through a bifurcation and related zones of flow sepa-518 ration [e.g. Ramamurthy et al., 2007]; (2) the width-to-depth ratio and flow field inertial 519 and momentum forces [e.g. Bradbrook et al., 2001; Parsons et al., 2007]; (3) flow field 520 super-elevation and related pressure gradient terms [e.g. Shettar and Keshava Murthy, 521 1996; (4) backwater surface slopes; and (5) topographic forcing by the bed [e.g. McArdell 522 and Fach, 2001; Bolla Pittaluga et al., 2003; Kleinhans et al., 2008]. In this paper, two 523 independent flow measurement techniques have been used to quantify flow fields in a 524 morphologically symmetrical experimental bifurcation. Flow structures develop that can 525 significantly modify the near-bed flow direction at a distance of up to one channel width 526 upstream of the bifurcation head. The character of the flow was turbulent and highly 527 subcritical with strong backwater effects. Data obtained from control experiments with 528 equal discharge partitioning do not show asymmetric near-bed flow but do have some flow 529 structures that contain counter-rotating transverse-vertical cells upstream of the bifurca-530 tion in addition to a clear signal of the bifurcating flow closer to the bifurcation. In the 531 experiments with unequal discharge partitioning the near-bed transverse flow was directed 532 towards the bifurcate channel which had the gradient advantage and largest discharge. 533 About 80% of the near-bed flow entered the larger channel. Furthermore, as expected, the 534

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transverse flow component is larger for channels with larger water depth relative to chan-535 nel width and relative to the characteristic length of bed roughness. This flow structure 536 upstream of the bifurcation is caused by flow curvature towards the bifurcate channels at 537 the bifurcation. Such upstream influence is also observed in curved channels and may be 538 the result of the actual flow curvature itself [Jamieson et al., 2010], or the result of back-539 water effects [Blanckaert et al., 2013]. Downstream of the bifurcation, the flow structure 540 shows a pattern that is consistent with plunging water resulting from super-elevation at 541 the bifurcation point, as shown by *Thomas et al.* [2011]. 542

In classical analyses of the stability of a perfectly symmetrical bifurcation, a perturba-543 tion to the bed level or water depth is introduced either in one of the distributaries or 544 just upstream of the bifurcation [Wang et al., 1995; Bolla Pittaluga et al., 2003; Kleinhans 545 et al., 2008. Such a perturbation may grow or dampen depending on the channel width-546 to-depth ratio and sediment mobility. A growing perturbation may eventually lead to the 547 closure of one of the bifurcate channels, i.e. the bifurcation is unstable. In the present pa-548 per, we document laboratory flume experiments in which we perturbed the bifurcation by 549 changing the energy gradient in the bifurcate channels. Theoretically, this should always 550 lead to the enlargement of the channel receiving the most discharge when the bifurcation 551 is otherwise symmetrical. However, our experimental findings suggest that the destabi-552 lization of a morphologically perfectly symmetrical bifurcation has a pronounced influence 553 on the near-bed flow over a distance of about one channel width upstream of the bifur-554 cation, which may influence the bifurcation stability. This length scale is in agreement 555 with the length scales and model concepts of Bolla Pittaluga et al. [2003] and Kleinhans 556 et al. [2008]. However, in these models, the upstream length of bifurcation influence is 557

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assumed to be the result of an upstream extension of topographic forcing by the bed 558 [e.g. McArdell and Faeh, 2001; Bolla Pittaluga et al., 2003; Kleinhans et al., 2008], which 559 was absent in our experiments. In our case, the dividing line between near-bed flow that 560 enters the dominant channel and near-bed flow that enters the subordinate channel is 561 strongly curved (Fig. 9). Thus, the fraction of upstream channel width that contributes 562 water to the dominant bifurcate channel is much larger than expected on the basis of the 563 relative discharges of the bifurcate channels. This novel result is not included within the 564 depth-averaged model concepts used in both Bolla Pittaluga et al. [2003] and Kleinhans 565 et al. [2008]. The implication is that linear stability analyses of perturbed bifurcations 566 based on depth-averaging requires modification for the flow structure induced by discharge 567 asymmetry, which is the result of a perturbation in one of the downstream channels... 568

The observed near-bed flow structure upstream of perturbed bifurcations has an unexpected ramification for the breakdown of symmetry of river bifurcations. In our experiments, near-bed flow is directed towards the dominant bifurcate. Such flow structure may cause an increase of sediment supply into this dominant channel. For example, for experiments where the dominant bifurcate received about 60% of the total discharge, about 70% of the near-bed flow was going into this bifurcate (Fig. 9). We expect a similar effect on bedload partitioning in bifurcations.

Morphologically, we suggest that the impact of this accentuated asymmetry in near-bed flow partitioning could be a negative feedback on the destabilized bifurcation: the dominant bifurcate channel could receive so much more sediment that it aggrades, reducing its conveyance and thus forcing the bifurcation towards symmetry. In other words, the net effect opposes the initial degradation of the dominant bifurcate channel, particularly

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in the case of narrow and deep rivers with stronger transverse flow. Curvature in the 581 flow just upstream of the bifurcation will initially lead to sedimentation in the dominant 582 channel because of flow convergence, but also sedimentation upstream of the subordinate 583 channel distributary because of flow divergence. As a result, the dominant channel may 584 aggrade initially, even if it eventually enlarges [e.g. Bertoldi and Tubino, 2007; Bolla Pit-585 taluqa et al., 2003; Edmonds and Slingerland, 2008; Federici and Paola, 2003; Kleinhans 586 et al., 2008; Miori et al., 2006]. The flow structure observed in our experiments may thus 587 cause stabilization of a symmetrical but perturbed bifurcation. This negative feedback 588 has not been described before. 589

The question is: how important is this negative feedback in natural bifurcations? It 590 could be argued that the sediment transport capacity of the dominant bifurcate channel 591 would increase nonlinearly with discharge. However, the analyses of Wang et al. [1995] 592 and Bolla Pittaluga et al. [2003] demonstrate that the ratio of sediment transport in 593 the two bifurcates $Q_{s,right}/Q_{s,left} = (Q_{right}/Q_{left})^k$, where k is unity in the absence of a 594 transverse bed slope and planimetric perturbation. In principle, k is to be determined em-595 pirically, but three-dimensional flow and sediment transport modeling has demonstrated 596 that k is approximately unity for much of the lifetimes of bifurcations formed in mobile 597 beds [Kleinhans et al., 2008]. Here, k = 1 means that sediment is partitioned over the 598 downstream channels proportionally to their widths. This work was based on modeling 599 idealized but asymmetrical bifurcations with an initially flat bed [*Kleinhans et al.*, 2008]. 600 There were indeed fluctuations in discharge partitioning after the start of all model runs, 601 particularly in runs where the bifurcate channels were nearly balanced by, on the one 602 hand, a gradient advantage for one channel, but on the other hand an advantage for the 603

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⁶⁰⁴ other channel caused by an upstream bend with helical flow upstream of the bifurcation ⁶⁰⁵ that favors the subordinate channel. The models show that initially sediment always ⁶⁰⁶ deposited in one of the channels such that k is offset as the dominant bifurcate channel ⁶⁰⁷ initially receives relatively more sediment despite the presence of a bend [*Kleinhans et al.*, ⁶⁰⁸ 2008, their Fig. 9]. This can be expressed empirically as:

$$Q_{s,right}/Q_{s,left} = a \left(Q_{right}/Q_{left}\right)^k \tag{14}$$

where a < 1. In the numerical modeling the ultimate bifurcation condition was asymmetrical in the manner expected from gradient or upstream bend advantage, but the evolution towards this state was delayed by the negative feedback of flow structure.

In short, previous numerical modeling work supports our hypothesis that bifurcations 612 with subcritical flow perturbed by asymmetrical downstream discharge conveyance have 613 a flow structure that may result in elevated sediment transport into the dominant chan-614 nel, providing a negative feedback on the onset of bifurcation destabilization. Given that 615 the transverse bed slope upstream of the bifurcation only overcomes the initial flow and 616 sediment attraction of the advantaged channel in a later stage, we hypothesize the follow-617 ing. The balance is subtle and the transverse bed slope readily develops, so the condition 618 where balancing potentially occurs is when the transverse bed slope development is limited 619 whilst the imbalance between channel width and flow discharge is large. In other words, 620 balancing flow attraction and sediment attraction is most likely to occur where there is 621 a large gradient or bend advantage for one channel, leading to higher discharge, whilst 622 the other channel is equally wide or wider but has a lower discharge. Other important 623 factors are the roughness of the channel and the width-to-depth ratio of the channel, as 624

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these suppress the transverse flow and therefore the sediment attraction of the dominant channel.

The hitherto unidentified effect could lead to unexpected sedimentation in engineered 627 bifurcations, for example in small streams with newly created side channels. Altered sedi-628 mentation patterns will be especially present in cases of low roughness. Furthermore, the 629 flow structure and the inherited mixing of flow propagating into the downstream branches 630 may be relevant for the aquatic chemistry of small bifurcating streams as commonly found 631 in lowland areas, because it modifies the supply of dissolved oxygen, nutrients and organic 632 matter. In addition, the reported effects of bifurcation perturbation on near-bed flow af-633 fect the biologically important benthic boundary layer. 634

5. Conclusions

The effect of flow structure on the stability of geometrically symmetrical bifurcations was studied in fixed-bed experiments under a range of conditions, including both a smooth and rough bed case, over two width-to-depth ratios and either symmetrical or asymmetrical flow division forced by downstream water surface gradient.

⁶³⁹ Upstream of the bifurcation, counter-rotating flow structures emerged. In high width-to-⁶⁴⁰ depth ratio channels, the number of flow cells increased. These flow cells were equal in size ⁶⁴¹ for bifurcations with equal discharge division, but asymmetrical for the bifurcation with ⁶⁴² unequal discharge division. These flow cells diminished in strength with higher width-to-⁶⁴³ depth ratio and bed roughness. Closer to the bifurcation, flow splitting suppressed these ⁶⁴⁴ flow structures.

The experiments demonstrate that, under unequal discharge division, the flow is strongly curved towards the channel with the highest discharge over a length of about

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one channel width. The near-bed flow curvature was considerably larger than the surface flow curvature, with the strongest curvature just upstream of the bifurcation. These
effects diminish with increasing width-to-depth ratio and increasing bed roughness.

These results imply that a disproportionately large amount of sediment can be transported into the downstream channel with the largest discharge. This could provide a negative feedback on bifurcation destabilization because the enhanced sediment input would reduce the expected erosion rate in that channel. This modifies the usual hypotheses that sediment division in a symmetrical bifurcation is proportional to channel width. This mechanism would act as a stabilizing effect on perturbed river bifurcations, which is not been taken into account in current theory.

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 $_{669}$ 30%, GMK: 20, 10, 0, 5%, RET: 20, 0, 0, 5. The authors thank three anonymous reviewers

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Figure 1. (a) Photograph of the model set-up, (b) schematic illustration of the model set-up,
(c) bifurcation model detail with locations of UDVP measurements cross-sections and PIV area.
(d) Illustration of the locations and directions of UDVP transducers in the upstream part of the bifurcation at low WDR. In the bifurcate channels 8 measurements per channel width were used.
In the high WDR runs, 3 vertical measurement locations were used.

Figure 2. 3D velocity components (UDVP data) for run 80EQ, at cross-sections a) CS01, b) CS02, c) CS03, d) CS04L and e) CS04R. Color contours show stream-wise velocity (Ux), black arrows show cross-stream (Uy) and vertical (Uz) velocity components. White arrows indicate the bulk flow structure, dashed line shows the approximate location of flow division (Uy = 0). Axis orientation is such that the 'flow goes into the paper' / looking downstream. Vertical axis and vertical flow velocities are 2 times exaggerated in respect to cross-stream axis and flow velocity.

Figure 3. 3D velocity components (UDVP data) for run 80NEQ, see Fig. 2 for caption.

Figure 4. 3D velocity components (UDVP data) for run 35EQ, see Fig. 2 for caption.

Figure 5. 3D velocity components (UDVP data) for run 35NEQ, see Fig. 2 for caption.

Figure 6. Depth-averaged (DA, light-green) and near-bed (NB, dark-red) flow velocity vectors (UDVP data) at all measured cross sections. Axis labels were removed where they are the same as the adjacent graphs. Secondary flow structures caused the direction of the near-bed flow to deviate from the depth-averaged flow. This effect was more pronounced in the low WDR, asymmetrical runs (80NEQ / 80NEQ_S). The high WDR, rough bed runs are noisy due to acoustic resonance in the flume.

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Figure 7. Near-surface velocity vectors (PIV data, arrows). Cross-stream flow velocities are emphasized with colored contours, which indicate the magnitude of cross-stream flow Uy relative the upstream channel. Red contours indicate flow to the right, blue /dashed contours indicate flow to the left, first contour = 5 mm s^{-1} , contour interval = 10 mm s^{-1} . For clarity, only every third vector in the downstream direction is shown.

Figure 8. Near-bed velocity vectors (PIV data, arrows), see Fig. 7 for caption.

Figure 9. Division of flow at the bifurcation derived from PIV flow fields. a) equal discharge division runs (read legend as xx=EQ), and b) unequal discharge division runs (read legend as xx=NEQ). Solid black lines show the boundaries of the bifurcation model. Solid lines denote the division between surface water entering the left and right channels for the smooth bed runs, dashed lines show the surface water division for the rough bed runs. Dotted lines denote the division of incoming near-bed flow between the left and right channels.

Figure 10. Absolute normalized circulation derived from UDVP data for all a) smooth bed runs and b) rough bed runs plotted against downstream coordinate y. For the most downstream location, the lines spit for the left and right bifurcate channel. Blue lines represent the low-WDR runs, green the high-WDR runs. Dark colors represent equal discharge division runs, pale colors the unequal discharge division runs.

Figure 11. Surface flow vorticity derived from PIV data. Blue indicates counter-clockwise circulation and red indicates clockwise circulation. White lines are streamlines derived from PIV data.

Figure 12. Near-bed flow vorticity derived from PIV data. Blue indicates counter-clockwise circulation and red indicates clockwise circulation. White lines are streamlines derived from PIV data.

Figure 13. Average vorticity in the upper straight part of the bifurcation (0 < x < 320 mm)plotted against normalized channel width (0=left bank, 1=right bank) for surface flow (a,b) and near-bed flow (c,d). a and c show the low-WDR runs, b and d the high-WDR runs.

Figure 14. Measured streamwise velocity profiles (symbols) and logarithmic fit (lines) at CS01 at probe location 1 (next to wall), 4 and 8 (near-center) for all low WDR runs (a) and high WDR runs (b). Probe 4 and 8 are plotted with offset. Open symbols show the experiments with rough bed, pale colors are the unequal discharge division runs. c) The coefficient of determination (R^2) for the logarithmic fit of flow velocities for all probes in CS01, shown against normalized distance to the wall. Where the flume wall is at 0 and the center of the channel at 0.5. Symbols are plotted with slight offset for clarity.

Figure 15. Measured near-surface streamwise velocity from UDVP data plotted against surface streamwise velocity from PIV data.

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Run abbr.	WDR (-)	h (m)	Qr (-)	bed
80EQ	6.3	0.080	1	smooth
80NEQ	6.3	0.080	1.5	smooth
$35\mathrm{EQ}$	14.3	0.035	1	smooth
35 NEQ	14.3	0.035	1.5	smooth
$80 EQ_S$	6.3	0.080	1	rough
80NEQ_S	6.3	0.080	1.5	rough
$35 EQ_S$	14.3	0.035	1	rough
$35 NEQ_S$	14.3	0.035	1.5	rough

Table 1.Experimental runs.^a

^a Showing the width-to-depth ratio (WDR), the corresponding water depth (h) in the entire flume measured from the top of the bed, the desired discharge ratio $(Qr = Q_{right}/Q_{left})$ and the type of bed (no sediment / smooth or with gravel / rough). Upstream flume width is 0.5 m.

 Table 2.
 UDVP settings and parameters.^a

	х	y up	y down	Z
Sample bins	64	64	64	64
First sample distance (mm)	4.995	4.995	4.995	4.995
Sample length (mm)	194.4	496.5	247.6	99.7
Sample distance (mm)	2.96	7.68	3.79	1.48
Sample width (mm)	2.96	2.96	2.96	2.96
Sampling period (ms)	8	8	8	16
Intra-sample delay (ms)	15	15	15	15
Number of probes in cycle	7	7	7	8
Sampling frequency (Hz)	6.21	6.21	6.21	4.03
Maxium depth, Lmax (mm)	228.29	912.79	912.79	983.46
Min U (mm/s)	0.00	-74.99	-74.99	-69.60
Max U (mm/s)	299.84	74.99	74.99	69.60
Velocity resolution $\Delta U(mm/s)$	1.17	0.59	0.59	0.54

^a for streamwise (x), cross-stream in upstream channel (y up), cross-stream downstream

channels (y down) and vertical (z) velocities.

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		Run							
Property	Location	$80\mathrm{EQ}$	80NEQ	$35\mathrm{EQ}$	35NEQ	$80\mathrm{EQ}~\mathrm{S}$	80NEQ_S	$35 EQ_S$	35NEQ_S
WDR		low	low	high	high	low	low	high	high
Symmetry		symm	asymm	symm	asymm	symm	asymm	symm	asymm
Bed		smooth	smooth	smooth	smooth	rough	rough	rough	rough
<i>H</i> (m)	CS01-04	0.080	0.080	0.035	0.035	0.080	0.080	0.035	0.035
$Ux_{av} (m s^{-1})$	CS01-03	0.18	0.18	0.16	0.15	0.14	0.15	0.09	0.06
	CS04L	0.18	0.14	0.16	0.10	0.14	0.12	0.07	0.04
	$\rm CS04R$	0.18	0.23	0.16	0.18	0.15	0.17	0.06	0.06
Fr (-)	CS01-03	0.20	0.20	0.28	0.26	0.16	0.17	0.15	0.10
Re (-)	CS01-03	10298	10358	4720	4396	8320	8605	2524	1765
We (-)	CS01-03	426.6	431.5	152.8	132.5	278.5	297.9	43.9	21.6
$Q \ (\mathrm{m^3 s^{-1}} \ 10^{-3})$	CS01	7.28	7.22	2.85	2.69	5.71	6.02	1.65	1.16
	CS02	7.14	7.16	2.83	2.62	5.74	6.00	1.41	1.10
	CS03	7.03	7.21	2.81	2.60	5.90	5.91	1.49	0.92
	CS04L+R	7.08	7.25	2.78	2.49	5.80	5.87	1.17	0.91
	CS04L	3.56	2.71	1.37	0.88	2.85	2.40	0.61	0.36
	$\rm CS04R$	3.52	4.54	1.41	1.61	2.95	3.47	0.55	0.55
$Q_{rms} \ (\mathrm{m^3 s^{-1}} \ 10^{-3})$	CS01-04	0.09	0.03	0.03	0.07	0.07	0.06	0.17	0.11
$Q_{rms}(\%)$	CS01-04	1.33	0.46	0.89	2.72	1.24	1.08	12.16	10.73
$Qr \; (Q_{right}/Q_{left})$	CS04	0.99	1.67	1.03	1.83	1.03	1.45	0.90	1.51
Q_{right}/Q_{total}	$\rm CS04R$	0.50	0.63	0.51	0.65	0.51	0.59	0.47	0.60
$q_{surf,right}/q_{surf,total}$	PIT surface	0.51	0.62	0.50	0.56	0.49	0.55	0.50	0.51
$q_{bed,right}/q_{bed,total}$	PIT bed	0.52	0.71	0.50	0.68	-	-	-	-
$ \hat{\Gamma} $ (-)	CS01	15.4	12.8	5.5	0.9	8.5	9.0	2.1	4.0
	CS02	14.6	10.8	1.2	1.0	6.0	8.1	1.3	4.3
	CS03	12.7	10.3	0.9	1.5	6.8	10.0	2.9	4.5
	CS04L	18.0	29.9	9.9	7.1	24.4	31.5	8.4	8.5
	CS04R	13.1	16.3	8.2	4.0	27.6	23.9	5.4	10.2

Table 3. Flow properties for all runs	Table 3.	Flow	properties	for	all	runs.
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^a Derived from UDVP and PIV data. Flow division from PIV data were derived from the data in Fig. 9 and represent the location of division line in this Figure at y/W = 1. DRAFT January 14, 2014, 11:49am