Search for gravitational wave signals from known pulsars in LIGO-Virgo O3 data using the 5n-vector ensemble method

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The 5*n*-vector ensemble method is a multiple test for the targeted search of continuous gravitational waves from an ensemble of known pulsars. This method can improve the detection probability combining the results from individually undetectable pulsars if few signals are near the detection threshold. In this paper, we apply the 5*n*-vector ensemble method to the O3 data set from the LIGO and Virgo detectors considering an ensemble of 201 known pulsars. We find no evidence for a signal from the ensemble and set a 95% credible upper limit on the mean ellipticity assuming a common exponential distribution for the pulsars' ellipticities. Using two independent hierarchical Bayesian procedures, we find upper limits of 1.2×10^{-9} and 2.5×10^{-9} on the mean ellipticity for the 201 analyzed pulsars.

I. INTRODUCTION

Continuous gravitational waves (CWs) signals are promising targets for the LIGO [1] and Virgo [2] detectors defined by persistence and near-monochromaticity over long time scales. Among the most plausible sources of this type of signal there are spinning neutron stars with a non-axisymmetric mass distribution [3] due to deformations from shear strains in the crust, or from magnetic stresses [4].

The signal strain amplitude depends on the ellipticity, the physical parameter that quantifies the mass distribution asymmetry with respect to the rotation axis [5]. Different neutron star equations of state can allow different sizes of deformations, i.e. of ellipticities, to be sustained in the star. The detection of a CW signal could allow us to make physical inference about the equation of state, and/or about the internal magnetic field strength [6].

According to the knowledge of the source parameters (sky position, rotation parameters), different strategies can be adopted to search for a CW signal [7]. The simplest, but also the most sensitive strategy, is the *targeted* search [8]: using information about the spin evolution, astrometry, and binary orbit gained from continued pulsar monitoring, it is possible to infer with high accuracy the sky position and the rotation parameters including the source spin frequency and the spin-down. Indeed, most pulsars are observed to steadily spin-down due to the emission of electromagnetic waves (and, possibly, also CWs). From the pulsar spin-down, it is possible to set a theoretical upper limit to the strain amplitude, the socalled spin-down limit, assuming that all of the rotation energy lost by the pulsar is converted to gravitational wave (GW) energy [9].

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At the source reference frame, the CW signal is almost monochromatic with frequency proportional to the rotation frequency of the source, through a factor which depends on the considered emission model [4]. At the detector, the CW signal has a frequency and phase modulation mainly due to the Doppler effect for the relative motion between the source and the Earth.

De-modulation techniques are useful for removing the phase modulation caused by the spin-down/Doppler shift and hence to precisely unwind the apparent phase evolution of the source. Once these corrections have been applied, a CW signal would become monochromatic except for the sidereal modulation due to the antenna patterns. This modulation depends on the detector position and orientation on the Earth and it is used by the 5n-vector method to define a detection statistic as well as to estimate the signal parameters [10, 11].

So far, no evidence for a CW signal has been found in LIGO and Virgo data. The last targeted search from the LIGO-Virgo-Kagra (LVK) Collaboration [9], using the data from the observing run O3 and analyzing 236 known pulsars, set 95% credible upper limits on the amplitude and the ellipticity of each pulsar.

To improve the detection probability for the targeted search of CWs, different strategies can be used considering an ensemble of individually undetectable pulsars as in [12–14]. In this paper, we use the 5n-vector ensemble method, described in [15]. This method defines an ensemble statistic, T(k), as the partial sum of the statistics of single pulsar, ranked for increasing p-values.

The ensemble procedure is a rank truncation method that selects the top ranking sources according to the significance of the corresponding individual test. Using the statistics T(k), we define a *p*-value as a function of *k*, that is a *p*-value for the overall hypothesis of the presence of CWs from the ensemble.

In case of no detection, we can set 95% credible upper limit on the global parameter Λ (defined in [15]) that describes the ensemble, and on the mean ellipticity that returns information about the population properties using two independent hierarchical procedures.

The paper is organized as follows. In Sec. II, we review the 5n-vector ensemble method and describe the procedures to set upper limits in case of no detection from the ensemble. In Sec. III, we describe the data set used for the analysis while in Sec. IV, we show the results of the targeted search for single pulsar using the 5n-vector method with the first application to pulsars in binary system. In Sec. V, we report the results of the ensemble procedure on three different sets. Since there is no evidence of a signal from the ensemble, we set the upper limits, that are compared with the results of previous similar searches. Conclusions are presented in Sec. VI.

II. THE 5N-VECTOR ENSEMBLE METHOD

The 5n-vector ensemble method [15] is a multiple test that combines the effects of individually undetectable pulsars using the results of the single pulsar analysis through the 5n-vector method.

The 5*n*-vector method [11] is a frequentist pipeline used in the LVK Collaboration for CW searches. It is based on the splitting at the detector of the expected GW frequency f_{gw} in five components due to the sidereal modulation of the Earth. The expected signal h(t)can be written using the polarization ellipse [10]:

$$h(t) = H_0(H_+A_+(t) + H_\times A_\times(t))e^{i\Phi(t)}$$
(1)

where $H_{+/\times}$ are the polarization functions for the plus and cross components:

$$H_{+} = \frac{\cos(2\psi) - j\eta\sin(2\psi)}{\sqrt{1+\eta^{2}}}$$
(2)

$$H_{\times} = \frac{\sin(2\psi) + j\eta\cos(2\psi)}{\sqrt{1+\eta^2}} \,. \tag{3}$$

 η and ψ are the polarization parameters [10], $A_{+/\times}$ are linked to the antenna patterns while $\Phi(t)$ is the GW phase. The parameter η is defined as:

$$\eta = -\frac{2\cos(\iota)}{1 + \cos^2(\iota)} \tag{4}$$

where ι is the angle between the star rotation axis and the line of sight. The amplitude H_0 is linked to the classic amplitude h_0 , defined for example in [9], by:

$$H_0 = h_0 \sqrt{\frac{1 + 6\cos^2(\iota) + \cos^4(\iota)}{4}}.$$
 (5)

The phase $\Phi(t)$ in Eq. 1 shows a time dependence due to different phenomena that modulate in time the received signal frequency. Heterodine corrections [16] are applied to account for the pulsar spin-down and Doppler effect due to the Earth motion. The residual modulation is in the functions $A_{+/\times}$, i.e. in the detector response, that depend on the 5 frequencies $f_{\rm gw}, f_{\rm gw} \pm \Omega_{\oplus}, f_{\rm gw} \pm 2\Omega_{\oplus}$ where Ω_{\oplus} is the Earth's sidereal angular frequency.

The data 5-vector **X** and the signal template 5-vectors $\mathbf{A}^{+/\times}$ are defined as the Fourier transforms of the data and of the template functions $A_{+/\times}$ at the 5 frequencies where the signal power is split. The data/template 5vectors from each of the *n* considered detectors are then combined as described in Appendix A for a multidetector analysis.

The 5*n*-vector defines two matched filters between the data \mathbf{X} and the signal templates $\mathbf{A}^{+/\times}$ vectors, used in order to maximize the signal-to-noise ratio:

$$\hat{H}_{+} = \frac{\mathbf{X} \cdot \mathbf{A}^{+}}{|\mathbf{A}^{+}|^{2}} \quad \text{and} \quad \hat{H}_{\times} = \frac{\mathbf{X} \cdot \mathbf{A}^{\times}}{|\mathbf{A}^{\times}|^{2}} \quad (6)$$

The two matched filters are estimators [10] of the signal plus and cross amplitudes. They are used to construct the detection statistic S:

$$S = \frac{|\mathbf{A}^{+}|^{4}}{\sum_{j=1}^{n} \sigma_{j}^{2} T_{j} |\mathbf{A}_{j}^{+}|^{2}} |\hat{H}_{+}|^{2} + \frac{|\mathbf{A}^{\times}|^{4}}{\sum_{k=1}^{n} \sigma_{k}^{2} T_{k} |\mathbf{A}_{k}^{\times}|^{2}} |\hat{H}_{\times}|^{2} .$$
(7)

where σ_j^2 and T_j are the variance of the data distribution in a frequency band around f_{gw} (usually few tenths of Hz wide) and the observation time[17] in the j^{th} detector, respectively. In the case of Gaussian noise, the distribution of the statistic S in Eq. (7) is a Gamma distribution $\Gamma(x; 2, 1)$.

Fixing the number N of analyzed pulsars, the 5n-vector ensemble method ranks these pulsars according to the *p*-values P_i (with i = 1, ..., N),

$$P_i = P(S_i \ge \overline{S}_i | \text{noise}) \tag{8}$$

computed from the S_i noise distribution and the measured value \overline{S}_i for the i^{th} pulsar. Then, the ensemble statistic T(k) is defined as the partial sum of the first k largest order statistics (statistics with the k smallest p-values):

$$T(k) = \sum_{j=N-k+1}^{N} S_{(j)} .$$
(9)

From the statistics T(k), we can compute the *p*-value of ensemble P(k) as a function of k:

$$P(k) = P(T(k) \ge \overline{T}(k) | \text{noise}) \tag{10}$$

with

$$\overline{T}(k) = \sum_{j=N-k+1}^{N} \overline{S}_{(j)}, \qquad (11)$$

and $\overline{S}_{(j)}$ is the j^{th} largest measured value for the detection statistic for a certain pulsar in the ensemble. For example, for an ensemble of N pulsars with $P_j \leq P_i \forall i$ and $P_k \geq P_i \forall i$, the smallest and the largest order statistics values are $\overline{S}_{(1)} \equiv \overline{S}_k$ and $\overline{S}_{(N)} \equiv \overline{S}_j$, respectively.

We note that the p-value refers only to the null hypothesis and does not make reference to or allow conclusions about any other hypotheses, such as the alternative hypothesis. A small p-value (for example, below the 1%) can be used to recognize interesting ensemble of pulsars as starting point for the detection.

The noise and the signal distribution of the statistics T(k) can be inferred using a Monte Carlo procedure starting from the N experimental noise and signal distributions for the statistics of single pulsar, as described in [15].

The T(N) statistic coincides with the simple sum of the statistics S_i ; in case of Gaussian noise, T(N) follows a $\Gamma(x; 2N, 1)$ distribution. The T(N) signal distribution can be also expressed in closed-form and it is proportional to a non-central χ^2 distribution with 4N degrees of freedom and non-centrality parameter Λ [15]:

$$\Lambda = \sum_{i=1}^{N} H_{0,i}^2 f_i(\eta_i, \psi_i)$$
 (12)

where the coefficient f_i is:

$$f_{i}(\psi_{i},\eta_{i}) = 2\left(\frac{|\mathbf{A}_{i}^{+}|^{4}|H_{+,i}|^{2}}{\sum_{j=1}^{n}\sigma_{j}^{2}T_{j}|\mathbf{A}_{j,i}^{+}|^{2}} + \frac{|\mathbf{A}_{i}^{\times}|^{4}|H_{\times,i}|^{2}}{\sum_{k=1}^{n}\sigma_{k}^{2}T_{k}|\mathbf{A}_{k,i}^{\times}|^{2}}\right).$$
(13)

Even though we have defined a p-value of ensemble as a function of k, the statistical inference concerns the entire set of considered pulsars. The claim of a rank truncation method is the same of the Fisher's combination method where all the individual tests are combined together: i.e. there are some signals among all the N tests, regardless that a certain k < N led to a rejection.

A. Upper limit procedures

For the single pulsar analysis, we can set the 95% credible upper limits on the amplitude assuming uninformative uniform priors on ψ (with $-\pi/2 \leq \psi \leq \pi/2$) and $\cos(\iota)$ (with $-1 \leq \cos(\iota) \leq 1$) that defines η (see Eq. 4). Knowing the distance and assuming a fiducial moment of inertia, we set the 95% credible upper limits on the ellipticity.

The upper limit for the ensemble procedure must be set on population parameters since using a multiple test, we can not infer statistical information about the single pulsar parameters.

Considering the statistic T(N), i.e. the entire set of considered pulsars, two different approaches can be used.

First, we can constrain the parameter Λ , defined in Eq. (12), that fixes the T(N) distribution considering a mixed Bayesian-frequentist approach as in the case of single pulsar [18].

For the Bayes' theorem, the posterior on Λ is:

$$P(\Lambda | \overline{T}(N)) \propto L(\overline{T}(N) | \Lambda) \Pi(\Lambda)$$
(14)

where $\overline{T}(N)$ is the measured value of the ensemble statistic, $\Pi(\Lambda)$ is the prior while $L(\overline{T}(N)|\Lambda)$ is the likelihood, that is estimated from the theoretical T(N) signal distribution evaluated at the value $\overline{T}(N)$ for different Λ values.

The upper limit $\Lambda^{95\%}$ on the parameter Λ is:

$$\Lambda^{95\%} : \int_0^{\Lambda^{95\%}} P(\Lambda | \overline{T}(N)) d\Lambda = 0.95.$$
 (15)

 Λ is a global parameter for the ensemble and $\Lambda^{95\%}$ can be used to show the improvement in the method sensitivity analyzing future runs.

Secondly, assuming a common distribution for the ellipticities, we can use a hierarchical Bayesian framework to constrain the value of the hyperparameter that fixes the assumed common distribution. Indeed, hierarchical Bayesian inference allows to study population properties for the analyzed ensemble of pulsars [19].

Let us consider an ensemble of N pulsars and a common distribution fixed by the hyperparameter μ_{ϵ} for the set of ellipticities ϵ_i (with i = 1, ..., N).

We can constrain the value of the hyperparameter μ_{ϵ} considering the posterior probability density function inferred from a Bayesian procedure:

$$P(\mu_{\epsilon}|\overline{T}(N)) \propto L(\overline{T}(N)|\mu_{\epsilon})\Pi(\mu_{\epsilon})$$
(16)

where $\Pi(\mu_{\epsilon})$ is the prior distribution on the hyperparameter, while the likelihood $L(\overline{T}(N)|\mu_{\epsilon})$ can be defined as the value of the T(N) signal distribution evaluated at $\overline{T}(N)$, if the common distribution of the ellipticities is fixed by the hyperparameter μ_{ϵ} . The T(N) signal distribution and hence, the likelihood, is fixed by Λ in case of Gaussian noise. It follows that:

$$L(\overline{T}(N)|\mu_{\epsilon}) = \int L(\overline{T}(N)|\Lambda)\Pi(\Lambda|\mu_{\epsilon})d\Lambda.$$
(17)

From the definition in Eq. (12), deducing the analytical prior on Λ for an assumed distribution of the ellipticities with hyperparameter μ_{ϵ} is not straightforward. For a large ensemble, $N \gg 1$, $\Pi(\Lambda|\mu_{\epsilon})$ can be approximated with a Gaussian distribution according to the Central Limit Theorem. The mean and variance of the Gaussian distribution depend on the assumed distribution since it is the weighted sum of the mean and variance for the squared ϵ_i random variables.

The upper limit $\mu^{(\Lambda)}$ is:

$$\mu^{(\Lambda)} : \int_0^{\mu^{(\Lambda)}} P(\mu_\epsilon | \overline{T}(N)) d\mu_\epsilon = 0.95.$$
 (18)

Differently, we can also consider a classic hierarchical procedure combining the results of the single pulsar analysis as in [12]. In this case, the posterior probability density function on the hyperparameter μ_{ϵ} is:

$$P(\mu_{\epsilon}|\overline{S}_{1},..,\overline{S}_{N}) \propto \left(\prod_{i=1}^{N} \int L(\overline{S}_{i}|\epsilon_{i}) \Pi(\epsilon_{i}|\mu_{\epsilon}) d\epsilon_{i}\right) \Pi(\mu_{\epsilon}).$$
(19)

This posterior is independent of the ensemble procedure (i.e. of the statistic T(N)) and depends on the results of the single pulsar analysis through the likelihoods $L(\overline{S}_i|\epsilon_i)$. In addition, it does not depend on the Gaussian noise hypothesis and it can be used to constrain the hyperparameter μ_{ϵ} using the likelihood $L(\overline{S}_i|\epsilon_i)$ computed for the *i*th pulsar analysis.

The upper limit $\mu^{(S)}$ is

$$\mu^{(S)} : \int_{0}^{\mu^{(S)}} P(\mu_{\epsilon} | \overline{S}_{1}, .., \overline{S}_{N}) d\mu_{\epsilon} = 0.95.$$
 (20)

In this section, we describe the data set used for the analysis. It consists of the GW data set from the LIGO and Virgo detectors, and the electromagnetic data set from the different observatories used to determine the pulsar ephemerides.

A. Gravitational wave data

The O3 observing run started on 2019 April 1 (MJD: 58574.625) and ended on 2020 March 27 (MJD: 58935.708) for both the LIGO and Virgo detectors. O3 consisted of two parts, separated by a one month-long commissioning break. O3a ran from 2019 April 1, 15:00 UTC until 2019 October 1, 15:00 UTC. O3b ran from 2019 November 1, 15:00 UTC, to 2020 March 27, 17:00 UTC.

The duty cycles for this run were 76%, 71%, and 76% for LIGO Livingston (LLO), LIGO Hanford (LHO), and Virgo, respectively. The O3 data set is publicly available via the Gravitational Wave Open Science Center [20].

In this paper, we use the Band Sampled Data (BSD) framework [16] that consists of band-limited, downsampled time series of the detector calibrated data, called BSD files. This framework can be described as a database of sub-databases where the BSD file is a complex time series that covers 10 Hz and spans 1 month of the original data. Using the BSD libraries, it is possible to extract frequency sub-bands or time sub-periods in a flexible way, reducing the computational cost of the analysis.

B. Electromagnetic data

The set of analyzed pulsars is in Table II. We consider the ephemerides used in [9].

The observatories which have contributed to the data set [21] are: the Canadian Hydrogen Intensity Mapping Experiment (CHIME) [22], the Mount Pleasant Observatory 26-m telescope, the 42-ft telescope and Lovell telescope at Jodrell Bank, MeerKAT [23], the Nançay Decimetric Radio Telescope, the Neutron Star Interior Composition Explorer (NICER) and the Molonglo Observatory Synthesis Telescope (as part of the UTMOST pulsar timing program) [24, 25]. Pulsar timing solutions were determined from this data using TEMPO [26] or TEMPO2 [27–29] to fit the model parameters. The ephemerides have been created using pulse time-of-arrival observations that mainly overlapped with O3 observing period.

To estimate the theoretical spin-down limit or the upper limit for the fiducial ellipticity for a certain source, the pulsars' distances are needed [9]. For many pulsars, the distance can be found in the ATNF Pulsar Catalog [30]. These are distances mostly based on the observed dispersion measure and estimated using the Galactic electron density distribution model YMW16 [31] or

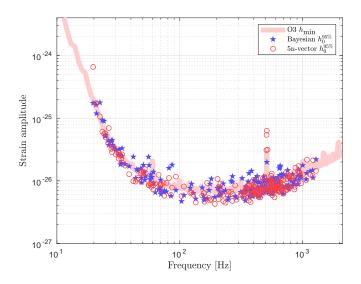


FIG. 1. Strain amplitude as a function of the GW frequency for O3 data of the LIGO and Virgo detectors. Blue stars are the upper limits inferred in [9] using the Bayesian method for the 223 pulsars in Table II while the red circles are the upper limits for the 5n-vector method. The continuous pink line is the minimum detectable amplitude for the O3 run considering a multidetector analysis.

the NE2001 model [32], although others are based on parallax measurements, or inferred from associations with other objects or flux measurements.

The distances used for each pulsar are given in Table II. The distances based on the dispersion measure are estimates with uncertainties that can amount up to a factor of two [31]. Nearby pulsars, for which parallax measurements are possible, have smaller distance uncertainties.

We select pulsars whose rotation frequency is greater than 10 Hz to match the sensitivity band of the GW detectors. This leads to primarily targeting millisecond pulsars and fast spinning young pulsars. In the analyzed set, there are 165 millisecond pulsars with expected CW frequencies above 100 Hz.

Pulsars can experience glitches during the observation time (as for the Crab pulsar during O3 [9]), i.e. sudden, impulsive increases in their spin [33]. The general procedure for glitching pulsars is to analyze each interglitch period independently and then to sum the resulting statistics [9]. In this analysis, we have not considered glitching pulsars; a dedicated study is needed to optimize the detection probability when glitching pulsars are present in the ensemble.

IV. SINGLE PULSAR ANALYSIS

In this section, we describe the results of the analysis of single pulsars using the 5n-vector method. Differently from the analysis in [9], we use the normalized single pulsar statistic S defined in Eq. (7) using the weighted multidetector extension described in Appendix A. For the first time using the 5n-vectors, we also consider pulsars in binary systems.

The results, reported in Table II, are obtained considering a single harmonic emission, i.e. the expected GW frequency is assumed exactly twice the rotation frequency of the source, and analyzing O3 data from the two LIGO and Virgo detectors.

For each pulsar, we consider a small frequency band (at least 0.2 Hz and at most 0.5 Hz wide) around the expected GW frequency. The frequency band extracted from the BSD files is chosen considering the spin-down of the source and in case of binary systems, considering also the Doppler effect due to the orbital motion.

Using the heterodyne correction [16], we remove the spin-down and the Doppler frequency modulation for the expected GW signal. The Doppler correction for pulsars in binary systems follows the model described in [34]. We do not take into account the uncertainty estimates in the binary parameters; the possible effects of these uncertainties on the heterodyne correction is described in the analysis in Appendix C.

The experimental noise distribution is inferred considering a range of off-source frequencies as described in [11]. The measured value of the statistics is compared with the noise distribution computing the p-value. Using the BSD framework, the computational cost of the analysis is reduced to a few CPU-minutes per source per detector.

In agreement with [9], there is no evidence of a CW signal from any pulsar in O3 data. We set 95% credible upper limit on the amplitude h_0 for each pulsar.

For the 5*n*-vector method since we are considering a different statistic, the results do not exactly coincide with the results in [9] but there is a very good agreement. For example, the upper limit on the amplitude for the pulsar J0711-6830 in [9] is 5.0×10^{-27} , while 4.8×10^{-27} in this work.

As shown in Fig. 1, the upper limits from the 5n-vector method (red circles) are in good agreement with the results of the Bayesian method (blue stars as in [9]). The differences in the results can be due to the data frameworks that are used in the two pipelines that entail different analyzed frequency bands for each pulsar and different pre-processing of the data.

V. ENSEMBLE ANALYSIS

In this section, we show the results of the 5n-vector ensemble method applied to O3 data. From the set of pulsars in Table II, we select 201 pulsars excluding 22 binary pulsars according to the selection criteria in Eq. C6 described in Appendix C based on the uncertainties of the binary parameters.

As described in [15], the improvement in the detection probability for the 5n-vector ensemble method depends on the number of analyzed pulsars N and on the power

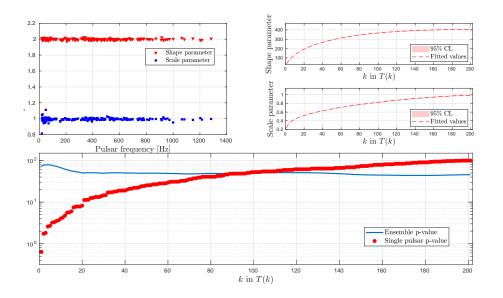


FIG. 2. Summary plot of the results for the ensemble over 201 pulsars considering O3 data of LLO, LHO and Virgo detectors. Top-left plot Fitted shape (red triangles) and scale parameters (blue squares) using a Gamma distribution to the experimental noise distribution for each pulsar as a function of the emission frequency of the pulsar. Top-right plots Fitted shape and scale parameters (dashed lines) with 95% confidence level (coloured area) for the T(k) noise distributions for each k inferred from the Monte Carlo procedure. Bottom plot p-value of ensemble (blue line) compared with the single pulsar p-values (red dots), ranked for increasing values.

of the combined individual tests. In a real search, we can not optimize N since we do not know the strength of the signals a priori.

We fixed three different ensembles from the set in Table II: the entire set for the three detectors, the set of millisecond pulsars ($f_{\rm gw} > 100 \,{\rm Hz}$) for the LIGO detectors and the high-value pulsars set for the LIGO detectors. High-value pulsars are the analyzed pulsars whose ratio between the experimental upper limit on the amplitude $h_0^{95\%}$ and the theoretical spin-down limit $h_{\rm sd}$ (the so-called spin-down ratio) is:

$$h_0^{95\%}/h_{\rm sd} \lesssim 1$$
. (21)

We chose the three ensembles according to physical observations. Indeed, millisecond pulsars are most likely to have undergone an accretion phase, which could alter the structure of their crust and magnetic field compared to non-recycled young pulsars [35], while high-value pulsars are promising targets that have surpassed their spindown limits.

The three ensembles correspond to fix N = 201 for the first set, N = 146 for the millisecond pulsars set and N = 20 for the high-value pulsars set.

After analyzing each pulsar singularly, we reconstruct the statistics T(k) and compute a *p*-value of ensemble as a function of k. The results are shown in the form of summary plot; the top-left plot shows the fitted shape and scale parameters of a Gamma distribution for the experimental noise distribution for the statistic S as a function of the GW frequency, the top-right plots show the fitted shape and scale parameters to the T(k) noise distributions as a function of k while the bottom-plot compares the ordered single pulsar p-values (red dots) with the ensemble p-values from the T(k) statistics (blue line).

Since there is no evidence of signal from the ensemble, we set 95% credible upper limit on the global parameter Λ and on the hyperparameter μ_{ϵ} , that is the mean value of the assumed exponential distribution for the ellipticities.

A. All pulsars, all detectors

The summary plot for the entire set of analyzed pulsars is shown in Fig. 2. For this analysis, we consider the two LIGO and Virgo detectors.

A criterion based on noise is used to select the detectors for the multi-detector analysis of single pulsar. Since the normalized statistic S, in the hypothesis of Gaussian noise, is distributed according to a $\Gamma(x; 2, 1)$, from the fitted parameters to the experimental noise S distribution (top-left plot in Fig. 2) we can easily check the Gaussianity in the selected frequency band for each pulsar. For the multi-detector analysis, we consider only the detectors that have fitted shape and scale parameters respectively in the range [1.6, 2.4] and [0.8, 1.2] (that is a maximum difference of 20% from the expected values for Gaussian noise). For each pulsar, this procedure allows to exclude the detectors with large noise disturbances in the analyzed frequency band. Indeed, experimental noise

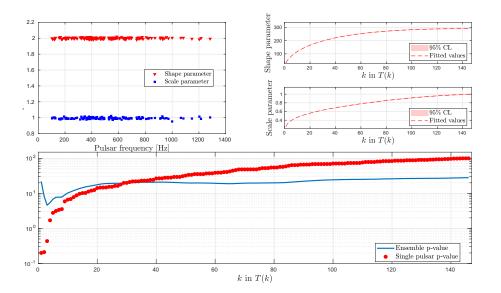


FIG. 3. Summary plot of the ensemble composed by the millisecond pulsars in Table II, considering O3 data and the two LIGO detectors. Top-left plot Fitted shape (red triangles) and scale parameters (blue squares) using a Gamma distribution to the experimental noise distribution for each pulsar as a function of the emission frequency for the considered pulsar. Top-right plots Fitted shape and scale parameters (dashed lines) with 95% confidence level (coloured area) for the T(k) noise distributions for each k inferred from the Monte Carlo procedure. Bottom plot p-value of ensemble (blue line) compared with the single pulsar p-value (red dots), ranked for increasing values.

S distributions that are very different from the $\Gamma(x; 2, 1)$ can influence the Monte Carlo procedure for the T(k) noise distributions.

From the bottom-plot of Fig. 2, there is no evidence of a signal form the ensemble. One pulsar has single pulsar p-value (red dot) below 1% as expected for a set of 201 pulsars. The p-value computed for the statistics T(k) are consistent with the noise hypothesis.

B. Millisecond pulsars, LIGO detectors

The summary plot for the millisecond pulsars is shown in Fig. 3. For this analysis, we consider only the two LIGO detectors with the same noise criteria introduced in the previous subsection, not considering the Virgo detector that has a higher noise level. As shown in Appendix A, a multidetector analysis does not necessarily entail a better sensitivity compared to the most sensitive detector's analysis.

As shown in the bottom plot in Fig. 3, there are **three** pulsars - J0824+0028, J1544+4937, J1551-0658 - below the 1% threshold. There is no evidence of a signal for any of these pulsars (as for the Bayesian results in [9]); the combination of the two LIGO detectors produces lower p-values with respect to the three detectors case.

For example considering the pulsar J0824+0028, the p-values for the single-detector single-pulsar analysis are 0.01, 0.04, 0.37 for LLO, LHO and Virgo respectively. The multidetector analysis considering all the three detectors entails a p-value of 0.01 while considering only

the two LIGO detectors, the p-value is 0.002.

The ensemble *p*-value has a minimum of almost 3% for k = 4 with no evidence of a signal from the ensemble. The strong decrease for the first values of k is due to the presence of the three pulsars with *p*-values below 1%.

C. High-value pulsars, LIGO detectors

There are 20 high-value pulsars in our dataset, that is there are 20 pulsars with spin-down ratio ≤ 1 (as in [9], excluding the glitching pulsars).

The summary plot for the high-value pulsars is shown in Fig. 4. For this analysis, we consider only the two LIGO detectors with the same noise criteria introduced in the previous subsection.

As shown by the the blue line in the bottom plot of Fig. 4, the *p*-value of the ensemble is fully consistent with the noise hypothesis.

D. Upper limits

For the upper limit computation, we consider the set of known pulsars analyzed in Fig. 2 and the O3 dataset for the LIGO and Virgo detectors.

Using the statistic T(N), that is the simple sum of the statistics for the pulsars in the analyzed ensemble, we set 95% credible upper limit on the parameter Λ defined in Eq 12. The prior on Λ is chosen uniform while the

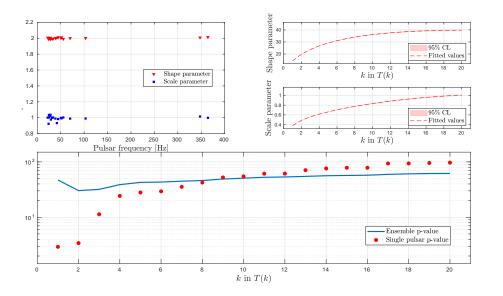


FIG. 4. Summary plot of the ensemble composed by the high-value pulsars with spin-down ratio ≤ 1 considering O3 data and the two LIGO detectors. Top-left plot Fitted shape (red triangles) and scale parameters (blue squares) using a Gamma distribution to the experimental noise distribution for each pulsar as a function of the frequency for the considered pulsar. Top-right plots Fitted shape and scale parameters (dashed lines) with 95% confidence level (coloured area) for the T(k) noise distributions for each k inferred from the Monte Carlo procedure. Bottom plot p-value of ensemble (blue line) compared with the single pulsar p-value (red dots), ranked for increasing values.

likelihood is the value of the T(N) signal distribution evaluated at the measured value $\overline{T}(N)$. The posterior $P(\Lambda|\overline{T}(N))$, shown in the left plot of Fig. 5, is compatible with zero as expected for the noise-only case. The 95% credible upper limit is:

$$\Lambda^{95\%} = 84.1.$$
 (22)

It is not possible to infer any information for the single pulsars from the upper limit $\Lambda^{95\%}$ since Λ is a global parameter for the ensemble. $\Lambda^{95\%}$ can be used to constrain different global parameters based on some assumptions for the single pulsar amplitudes. For example, by assuming that each pulsar in the ensemble emits a CW signal with the same amplitude \overline{h} , from the upper limit $\Lambda^{95\%}$ it follows that $\overline{h} = 1.9 \times 10^{-27}$.

For hierarchical procedures, following the analysis in [12] and the stochastic searches in [36, 37], we assume a common exponential distribution for the ellipticities with the hyperprior $\Pi(\mu_{\epsilon})$ that is log-uniform between 10^{-10} and 10^{-7} . The posteriors $P(\mu_{\epsilon}|\overline{T}(N))$ and $P(\mu_{\epsilon}|\overline{S}_1,..,\overline{S}_N)$ are shown in the right plot of Fig. 5.

The upper limit $\mu_{\epsilon}^{(\Lambda)}$ for the hierarchical procedure using the Λ parameter is

$$\mu_{\epsilon}^{(\Lambda)} = 2.5 \times 10^{-9} \,. \tag{23}$$

This upper limit procedure considers the theoretical signal distribution to evaluate the likelihood. The theoretical distribution can be used in the hypothesis of Gaussian noise in the analyzed frequency band for each pulsar. This can be checked looking at the fitted Gamma parameters for the T(N) statistic in the top-right plot of Fig. 2.

The upper limit $\mu_{\epsilon}^{(S)}$ for the hierarchical procedure using the single pulsar results is

$$\mu_{\epsilon}^{(S)} = 1.2 \times 10^{-9} \,. \tag{24}$$

The results and also the posteriors in Fig. 5 can be compared with Figure 8 in [12], where the authors analyzed 92 pulsars using data from the LIGO S6 science run showing the 90% upper limit on the mean of the assumed exponential distribution of 3.8×10^{-8} .

E. Discussion

As shown in Fig. 2-4 there is no evidence for a CW signal from the three different considered ensemble. In the following, we report some comments on the results found in this work.

(1) The upper limits set in this paper on the mean of the exponential distribution for the set of analyzed pulsars are more than one order of magnitude below the value in [12]. The combined O3 data for the LIGO and Virgo detectors are largely more sensitive than the LIGO S6 science run data and the analyzed ensemble is larger. A more reliable comparison between the two pipelines should consider the same ensemble, i.e. the same pulsars, and is outside the scope of this paper.

(2) The lowest limit on the ellipticity from the targeted search in [9] is 3.2×10^{-9} for J0636+5129 while from the

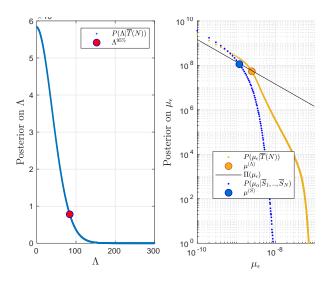


FIG. 5. Upper limits inferred from the ensemble procedure considering the set of 201 pulsars in Figure 2 and considering the O3 data for the LIGO and Virgo detectors. *Left plot:* posterior distribution for the global parameter Λ (defined in Eq. 12). The red point indicates the 95% credible upper limit for Λ . *Right plot:* posterior distribution for the two independent hierarchical procedures to set the upper limits on the mean μ_{ϵ} of the assumed exponential distribution. The continuous line is the log-uniform hyperprior on μ_{ϵ} . The blue and yellow points indicate the 95% credible upper limit for μ_{ϵ} .

all-sky search in [38] is 1.4×10^{-9} for a neutron star at 10 pc and 2047.5 Hz. The upper limits on the mean ellipticity set in this work are consistent with these values. We also note that these results approach the minimum limit on the ellipticity for millisecond pulsars of $\approx 10^{-9}$ supposed in [39].

(3) The upper limits in [36, 37] on average ellipticity for the neutron star population are $\mathcal{O}(10^{-8})$ from crosscorrelation-based searches of a stochastic gravitational wave background. These limits can not be directly compared with the limits in this work since we focused on known pulsars that represent only a small subset of the entire set of neutron stars in our Galaxy.

(4) The upper limits on the hyperparameter for the exponential distribution do not consider the uncertainties on the distance. The distance should be included as a variable assuming, for example following [12], a Gaussian prior with a mean given by each pulsar's best fit distance, and a standard deviation of 20% of that value with a hard cutoff at zero.

(5) The hierarchical procedures assume that all the analyzed pulsar ellipticities are drawn from a common distribution that can be too simplistic to describe the true ϵ distribution. For example, the population of young pulsars and old recycled millisecond pulsars have undergone different evolution and so have a different distribution. These populations should be treated independently, or a more complex distribution that allows separation of the two distributions should be used [12]. Therefore, a bimodal distribution, or two independent exponential distributions with different mean values, could be more appropriate and worth of study.

(6) Using the multidetector procedure, the results of single pulsar analysis in Fig. 1 are in agreement with [9]. However, it is still not clear when a multidetector analysis outperforms the most sensitive detector analysis. To choose which detectors should be used in the multidetector case, criteria based on the source sky position, on the detectors' sensitivities and observation times will be studied in the next future.

VI. CONCLUSION

In this paper, we have described the application of the 5n-vector ensemble method to O3 data for the LIGO and Virgo detectors considering a set of 201 known pulsars.

The single pulsar analysis can be seen as an hypothesis test where the null hypothesis of pure noise is tested against the alternative hypothesis of the presence of a CW signal in the data. To improve the detection probability, we apply the 5n-vector ensemble method, a multiple test that combines multi-detector single pulsar statistics defined through the 5n-vector method.

For the analysis of single pulsar, the single harmonic search (i.e. gravitational wave frequency exactly twice the rotation frequency of the source) on the 223 known pulsars shows good agreement with the Bayesian results in [9]. For the first time, the 5n-vector method is applied to binary systems for the targeted search and compared with the Bayesian results. The dual harmonic search (GW frequency at both once and twice the rotation frequency) is not implemented for the 5n-vector method. In Appendix C, we describe a preliminary analysis to quantify the effect of the binary parameters uncertainties on the detection sensitivity. We exclude from the ensemble analysis 22 binary pulsars whose combined uncertainties on t_p and ω do not respect the selection criteria in Eq. C6.

The ensemble statistics T(k) for the rank truncation method is defined as the partial sum of the k largest order statistics to control the look-elsewhere effect. Reconstructing the T(k) noise distributions for each k, using a Monte Carlo procedure, we compute the p-value of ensemble as a function of k, that is a p-value for the overall hypothesis of the presence of CWs from the ensemble.

In case of no detection, we propose different procedures to set upper limits using the ensemble procedure and the statistic T(N), i.e. the statistic for the entire ensemble. Using a mixed frequentist-Bayesian procedure, we can constrain the value of the global parameter Λ that fixes the T(N) signal distribution. Assuming a common exponential distribution for the ellipticities, we propose two independent hierarchical procedures to set upper limit on the mean μ_{ϵ} of the assumed distribution.

Section V shows the application of the ensemble procedure to the set of 223 pulsars in Table II considering O3 Three different ensembles are analyzed: the full set for the LIGO and Virgo detectors, the millisecond pulsar set for the two LIGO detectors and the high-value pulsars set for the two LIGO detectors. The results are shown in the summary plots in Fig. 2, Fig. 3 and Fig. 4.

There is no evidence of a CW signal from the ensemble; the *p*-values as a function of k are well above the assumed 1% threshold.

The upper limits procedures are applied to the entire set of pulsars considering the LIGO and Virgo detectors and O3 data. The posterior on the Λ parameter and on μ_{ϵ} are shown in Fig. 5. The upper limit set on Λ is $\Lambda^{95\%} = 84.1$ while the upper limit on μ_{ϵ} is 2.5×10^{-9} for the hierarchical procedure using the Λ parameter, and 1.2×10^{-9} for the hierarchical procedure using the single pulsar results. These results are more than one order of magnitude below the upper limit in [12], where the authors considered a classic hierarchical Bayesian procedure on an ensemble of 92 pulsars and data from the LIGO S6 science run.

The 5*n*-vector ensemble method improves the detection probability for the targeted search of CWs from known pulsars. Application of this procedure on the next observing runs will improve the possibility to detect a CW signal from known pulsars for the first time.

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Appendix A: Weighted multidetector extension

Considering *n* detectors, the classic 5n-vector definition, described in [40], combines together the 5-vectors \mathbf{X}_i from the i^{th} detector:

$$\mathbf{X} = \left[\mathbf{X}_1, ..., \mathbf{X}_n\right]. \tag{A1}$$

Since the detectors can have different sensitivities, the statistic based on the 5n-vector can reduce the signal to noise ratio compared to the statistic based only on the 5-vector of the most sensitive detector.

In this paper, we define the weighted data 5n-vector as:

$$\mathbf{X} = [c_1 \mathbf{X}_1, \dots, c_n \mathbf{X}_n] \tag{A2}$$

where the weights c_i are defined as:

$$c_j = \frac{\sqrt{n}}{\sqrt{\sum_{i=1}^n \left(\frac{T_i}{S_i}\right)}} \sqrt{\frac{T_j}{S_j}} = \sqrt{\mathcal{H}} \sqrt{\frac{T_j}{S_j}}.$$
 (A3)

 S_j and T_j are the variance of the data in a small frequency band around the expected GW frequency and the observation time in the j^{th} detector, respectively. \mathcal{H} is the harmonic mean of the time-weighted variances.

The matched filter is (similarly for \hat{H}_{\times}):

$$\hat{H}_{+} = \frac{\mathbf{X} \cdot \mathbf{A}^{+}}{|\mathbf{A}^{+}|^{2}} = \frac{\sum_{j=1}^{n} c_{j} \mathbf{X}_{j} (\mathbf{A}_{j}^{+})^{*}}{\sum_{k=1}^{n} \mathbf{A}_{k}^{+} (\mathbf{A}_{k}^{+})^{*}} = \frac{1}{|\mathbf{A}^{+}|^{2}} \left(c_{1} |\mathbf{A}_{1}^{+}|^{2} \hat{H}_{+,1} + \dots + c_{n} |\mathbf{A}_{n}^{+}|^{2} \hat{H}_{+,n} \right).$$
(A4)

In the hypothesis of Gaussian noise for the j^{th} detector with variance σ_j^2 , the two complex estimators $\hat{H}_{+/\times}$ have also Gaussian distributions,

$$\hat{H}_{+/\times} \sim Gauss\left(x; 0, \sigma_{+/\times}^2\right)$$
 (A5)

with

$$\sigma_{+/\times}^2 = \sum_{j=1}^n \frac{(c_j \sigma_j)^2 T_j |\mathbf{A}_j^{+/\times}|^2}{|\mathbf{A}^{+/\times}|^4} \,. \tag{A6}$$

Using the c_j , we re-define the noise variance in each detector:

$$(c_j \sigma_j)^2 \propto c_j^2 S_j = \frac{n T_j}{\sum\limits_{i=1}^n \left(\frac{T_i}{S_i}\right)}.$$
 (A7)

If the observation time was the same $(\forall j, T_j = t)$, this corresponds to "equalize" the noise in each detector. In this case, it follows that:

$$\sigma_{+/\times}^{2} = \sum_{j=1}^{n} \frac{(c_{j}\sigma_{j})^{2} T_{j} |\mathbf{A}_{j}^{+/\times}|^{2}}{|\mathbf{A}^{+/\times}|^{4}} = \sum_{j=1}^{n} \frac{n t |\mathbf{A}_{j}^{+/\times}|^{2}}{\sum_{i=1}^{n} \left(\frac{1}{\sigma_{i}^{2}}\right) |\mathbf{A}^{+/\times}|^{4}} = \frac{n t}{\sum_{i=1}^{n} \left(\frac{1}{\sigma_{i}^{2}}\right) |\mathbf{A}^{+/\times}|^{2}} = \frac{n t}{\sum_{i=1}^{n} \left(\frac{1}{\sigma_{i}^{2}}\right) \sum_{k=1}^{n} |\mathbf{A}_{k}^{+/\times}|^{2}}.$$
(A8)

Let us consider the toy case of *n* co-located detectors where $|\mathbf{A}_{k}^{+/\times}|^{2} = |\mathbf{A}_{1}^{+/\times}|^{2}, \forall k$; the variances are

$$\sigma_{+/\times}^2 = \frac{t}{\sum\limits_{i=1}^n \left(\frac{1}{\sigma_i^2}\right) |\mathbf{A}_1^{+/\times}|^2} \,. \tag{A9}$$

This corresponds to the case of one detector with observation time t and variance V^2 :

$$V^{2} = \frac{1}{\sum_{i=1}^{n} \left(\frac{1}{\sigma_{i}^{2}}\right)} = \frac{\mathcal{H}}{n}$$
(A10)

where \mathcal{H} is the harmonic mean of the variances. Since there is the condition:

$$\min\{\sigma_1^2, ..., \sigma_n^2\} \le \mathcal{H} \le n\min\{\sigma_1^2, ..., \sigma_n^2\}$$
(A11)

this means that:

$$\frac{\min\{\sigma_1^2, ..., \sigma_n^2\}}{n} \le \frac{\mathcal{H}}{n} \le \min\{\sigma_1^2, ..., \sigma_n^2\}.$$
(A12)

It follows that for n co-located detectors with the same observation time, we always have an improvement in the detection sensitivity using the coefficients c_i .

For example, let us consider the case of two co-located detectors n = 2 (equal to consider different datasets of the same detector), with $\sigma_2^2 = C \sigma_1^2$ and C > 1:

$$\sigma_{+/\times}^2 = \frac{C \,\sigma_1^2 t}{(C+1) \,|\mathbf{A}_1^{+/\times}|^2} \,. \tag{A13}$$

The minimum detectable signal is h_{min} :

$$h_{min} \propto \sqrt{\frac{C}{C+1} \frac{\sigma_1^2}{t}}$$
 (A14)

It is clear that in the general case (different detectors' locations and observation times), the multi-detector analysis not necessarily outperforms the most sensitive detectors.

It is important to briefly describe the signal distribution for $|\hat{H}_{+/\times}|^2$, see also [11]. If a CW signal is present into the analyzed data, the distributions of the two complex estimators $\hat{H}_{+/\times}$ are:

$$\hat{H}_{+/\times} \sim Gauss\left(x; H_0 e^{j\gamma} H_{+/\times} M_{+/\times}, \sigma_{+/\times}^2\right)$$
(A15)

where $H_{+/\times}$ are the polarization functions, H_0 is the amplitude, γ the phase and

$$M_{+/\times} = \sum_{j=1}^{n} \frac{c_j \, |\mathbf{A}_j^{+/\times}|^2}{|\mathbf{A}^{+/\times}|^2} \tag{A16}$$

is a known factor for the targeted search.

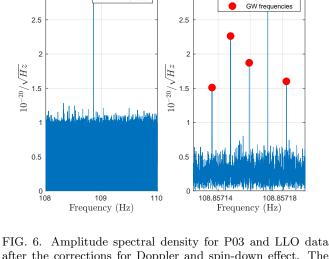
 $|\hat{H}_{+/\times}|^2$ have a non central- χ^2 distribution (apart from the factor $k_{+/\times}$):

$$|\hat{H}_{+/\times}|^2 \sim \frac{k_{+/\times}}{2} e^{-\frac{k_{+/\times}x + \lambda_{+/\times}}{2}} I_0(\sqrt{k_{+/\times}\lambda_{+/\times}x})$$
(A17)

where I_0 is the modified Bessel function of the first kind, and

$$k_{+/\times} = \frac{2}{\sigma_{+/\times}^2} \qquad \lambda_{+/\times} = k_{+/\times} |H_{+/\times}|^2 H_0^2 M_{+/\times} .$$
(A18)

With respect to the classic definition of the 5n-vector, the distributions do not change. There is just a redefinition of the variances for the detectors noise. This means that using the coefficients c_j , it is changed how $\lambda_{+/\times}$ depends on the detectors' sensitivity.



LLO data

LLO data

<<u>10</u>⁻³

3

FIG. 6. Amplitude spectral density for P03 and LLO data after the corrections for Doppler and spin-down effect. The right plot is the zoom around the GW frequency; the red dots show the expected 5 frequencies due to the Earth sidereal motion. Central peak frequency is the expected GW frequency.

Appendix B: Test of the binary correction

Hardware injections are simulated signals added to the detectors data physically displacing the detectors' test masses [41]. Differential displacement of the test masses mimics the detectors' response to a GW signal. Continuous hardware injections can be used to test CW analysis methods.

During the O3 run, 17 hardware injections that simulate different CW signals from spinning neutron stars were added in the two LIGO detectors. The list of injected pulsar parameters can be found in [42].

In this section, we consider two different hardware injections to test the 5*n*-vector pipeline. We report the results for the injected pulsar P03 (SNR(1 yr) \approx 30) that simulates an isolated spinning neutron stars with $f_{\rm gw} \simeq 108.8 \,{\rm Hz}$ and for P16 (SNR(1 yr) ≈ 68), a neutron star in binary system with $f_{\rm gw} \simeq 234.5 \,{\rm Hz}$. Figures 6

HI	Detector	ϵ_{H_0}	ϵ_η	ϵ_ψ
P03	LLO	0.93	0.54%	1.49%
	LHO	0.95	1.27%	0.39%
P16	LLO	0.91	0.66%	-
F 10	LHO	0.93	0.90%	-

TABLE I. Table of the parameters mismatch for the hardware injections (HI) P03 and P16 analyzing O3 data from the two LIGO detectors. ϵ_{H_0} is the ratio between the estimated and injected amplitude, while ϵ_{η} and ϵ_{ψ} are the normalized relative errors for the polarization parameters

and 7 show the amplitude spectral density for LLO detec-

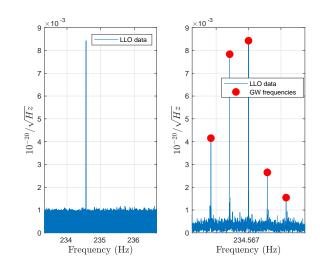


FIG. 7. Amplitude spectral density for P16 and LLO data after the corrections for Doppler and spin-down effect. The right plot is the zoom around the GW frequency; the red dots show the expected 5 frequencies due to the Earth sidereal motion. Central peak frequency is the expected GW frequency.

tor in the frequency band around the expected GW frequency for P03 and P16 after the Doppler and spin-down corrections using the BSD heterodyne method. The red dots are the theoretical expected 5 frequency peaks for the GW signal due to the sidereal modulation. The different "heights" of corresponding peaks in the two detectors depend on the antenna pattern, i.e. on the signal 5-vector templates $\mathbf{A}^{+/\times}$. It is important to note that the formalism used to construct the hardware injections' signal is independent from the 5-vector method.

In Table I, there are the results obtained for the two hardware injections considering the O3 datasets of the two LIGO detectors. The estimation of the intrinsic parameters (see [10]) is not influenced by the choice of the detection statistic since it depends only on the estimators $\hat{H}_{+/\times}$.

The small discrepancies (below 10%) in Table I for the amplitude fall within the uncertainties of the actuation system used for the injections. For P16, the ψ parameter is not well defined, since $\eta \approx 1$ and the signal is nearly circularly polarized.

Appendix C: Orbital parameters uncertainties

In this Appendix, we describe a preliminary analysis on the possible effects of the uncertainties on the heterodine de-modulation correction in the 5-vector context. We also describe the selection criteria used in this paper to include pulsars in binary systems for the ensemble procedure.

Indeed, large orbital parameters uncertainties could affect the sensitivity of targeted searches since large mismatches on the binary parameters could reduce the

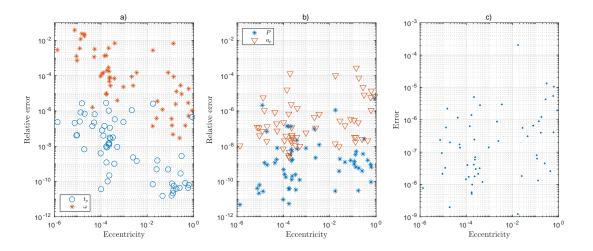


FIG. 8. Uncertainties for the orbital parameters provided by the T2 model. a) Relative errors on t_p and ω as a function of the eccentricity. b) Relative errors on P and a_p as a function of the eccentricity. c) $1-\sigma$ errors on the eccentricity as a function of the eccentricity values.

signal-to-noise ratio.

The heterodine correction is applied by multiplying the data by the exponential factor $e^{-i\Phi_{corr}(t)}$. The total signal phase correction $\Phi_{corr}(t)$ can be written as the sum of the spin-down and the Doppler contribution. The Doppler contribution is the sum of the terms due to the Earth motion and due to the pulsar orbital motion $\Phi_{bin}(t)$. For the linear phase model and the smalleccentricity limit, $e \ll 1$ (details in [34]):

$$\Phi_{bin}(t) \approx 2\pi f \left[-a_p \left(\sin \psi(t) + \frac{k}{2} \sin 2\psi(t) - \frac{\beta}{2} \cos 2\psi(t) \right) \right]$$
(C1)

where a_p is the semi-major axis whike k and β are the Laplace-Lagrange parameters:

$$k \equiv e \cos(\omega) \qquad \beta \equiv e \sin(\omega) \qquad (C2)$$

The mean orbital phase is

$$\psi(t) = \Omega(t - t_{asc}) \tag{C3}$$

measured from the time of ascending nodes t_{asc} . For small eccentricity and mean orbital angular velocity $\Omega = \frac{2\pi}{P}$ (*P* is the orbital period), t_{asc} is:

$$t_{asc} = t_p - \frac{\omega}{\Omega} \tag{C4}$$

 t_p and ω are the time and the argument of periapse, respectively. There are two main models for the orbital parameters [29]: the T2 model that returns the parameters (P, a_p, t_p, ω, e) and the ELL1 model that returns the parameters $(P, a_p, t_{asc}, k, \beta)$. Indeed in the low-eccentricity limit, the T2 model returns highly correlated values for t_p and ω , and the ELL1 model was developed for pulsars in such orbits.

In our preliminary analysis on the effects of the uncertainties, we focus on the T2 model since the ELL1 model provides better constrained parameters. For the ensemble of pulsars considered in our manuscript, almost 80 pulsars follows the T2 model. The parameters with the larger relative uncertainties are t_p and ω as shown in Figure 8 (particularly when the orbital eccentricity is below 0.01 as expected). These two parameters are also expected to be more relevant since they contribute directly to the orbital phase $\psi(t)$. We note that for 15 pulsars from the T2 model, we do not have an estimation of Δt_p while 11 pulsars are in circular orbits with $e = \omega = 0$. Using the P16, we have computed the coherence[43] for a wide range of the uncertainties Δt_p and $\Delta \omega$. The results show minima in the coherence corresponding to certain

$$\Delta \psi = \Omega \Delta t_p + \Delta \omega \tag{C5}$$

The values of $\Delta \psi$ corresponding to the minima can be analytically computed from the phase Φ_{bin} considering a mismatch Δt_p and $\Delta \omega$.

values of the combination:

We fix a threshold using the value of $\Delta \psi$ associated to the first minimum:

$$\Delta \psi \sim F \cdot \frac{3}{8fa_p} \tag{C6}$$

We can take the factor F = 5, which seems reasonable considering that the first minima are very sharp.

Considering the 223 pulsars analyzed in Table II, 80 pulsars have parameters form the T2 model; 22 pulsars (J0218+4232, J1017-7156, J1125-5825, J1312+0051, J1529-3828, J1545-4550, J1603-7202, J1614-2230, J1630+3734, J1708-3506, J1709+2313, J1737-0811, J1750-2536, J1751-2857, J1835-0114, J1840-0643, J1904+0412, J1946+3417, J1949+3106, J2019+2425, J2053+4650, J2129-5721) have a $\Delta \psi$ above the threshold in Eq. C6. We have excluded these pulsars from the ensemble analysis.

We stress that the uncertainties provided by the binary

model are 1σ Gaussian errors while in our relation, Δt_p and $\Delta \omega$ are considered as an absolute error.

The preliminary results described in this response consider only the t_p and ω parameters; it remains unclear how the uncertainties of the entire set of parameters combine together in the heterodyne correction. A precise and independent analysis is still required and falls beyond the scope of our manuscript.

TABLE II: Table of the parameters (name, GW frequency in Hz, distance in kpc, spin-down limit $h_{\rm sd}$) and the results inferred using the 5*n*-vector method (upper limit on the amplitude $h_0^{95\%}$, upper limit on the ellipticity $\epsilon^{95\%}$, *p*-value) for the 223 analyzed pulsars. Some pulsars don't have a value for $h_{\rm sd}$, and $\epsilon^{95\%}$ since the corresponding distance value (or the frequency derivative value) is not available in the ATNF Catalogue [30]. More details about the references for the ephemerides and distance estimation for the analyzed pulsars are in [9].

Pulsar name (J2000)	$f_{\rm gw}$ (Hz)	Distance (kpc)	$h_{ m sd}$	$h_0^{95\%}$	$\epsilon^{95\%}$	P-value
J0023+0923	655.7	1.1	$1.3 \cdot 10^{-27}$	$8.2 \cdot 10^{-27}$	$2.0 \cdot 10^{-8}$	0.68
J0030+0451	411.1	0.3	$3.6 \cdot 10^{-27}$	$6.5 \cdot 10^{-27}$	$1.2 \cdot 10^{-8}$	0.71
J0034 - 0534	1065.4	1.4	$8.9 \cdot 10^{-28}$	$1.0 \cdot 10^{-26}$	$1.2 \cdot 10^{-8}$	0.93
J0101 - 6422	777.3	1.0	$9.7 \cdot 10^{-28}$	$1.2 \cdot 10^{-26}$	$1.2 \cdot 10^{-8}$ $1.9 \cdot 10^{-8}$	0.11
J0102 + 4839	674.7	2.3	$6.8 \cdot 10^{-28}$	$7.3 \cdot 10^{-27}$	$3.5 \cdot 10^{-8}$	0.81
J0102 + 1000 J0117 + 5914	19.7	1.8	$1.1 \cdot 10^{-25}$	$6.6 \cdot 10^{-25}$	$2.8 \cdot 10^{-3}$	0.66
J0125 - 2327	544.2	0.9	$2.0 \cdot 10^{-27}$	$8.1 \cdot 10^{-27}$	$2.4 \cdot 10^{-8}$	0.48
J0154+1833	845.8	1.6	$3.4 \cdot 10^{-28}$	$1.1 \cdot 10^{-26}$	$2.5 \cdot 10^{-8}$	0.4
J0218 + 4232	860.9	3.1	$1.5 \cdot 10^{-27}$	$8.0 \cdot 10^{-27}$	$3.2 \cdot 10^{-8}$	1
J0340+4130	606.2	1.6	$7.2 \cdot 10^{-28}$	$9.1 \cdot 10^{-27}$	$3.7 \cdot 10^{-8}$	0.33
J0348 + 0432	51.1	2.1	$9.3 \cdot 10^{-28}$	$1.4 \cdot 10^{-26}$	$1.0 \cdot 10^{-5}$	0.2
J0406 + 3039	766.7	-	-	$8.0 \cdot 10^{-27}$	-	0.85
J0407 + 1607	77.8	1.3	$1.1\cdot 10^{-27}$	$9.3 \cdot 10^{-27}$	$1.9 \cdot 10^{-6}$	0.2
J0437 - 4715	347.4	0.2	$8.0 \cdot 10^{-27}$	$7.4 \cdot 10^{-27}$	$9.3 \cdot 10^{-9}$	0.24
J0453 + 1559	43.7	0.5	$3.1 \cdot 10^{-27}$	$9.7 \cdot 10^{-27}$	$2.5 \cdot 10^{-6}$	1
J0509 + 0856	493.1	0.8	$9.6 \cdot 10^{-28}$	$6.7 \cdot 10^{-27}$	$2.1 \cdot 10^{-8}$	0.83
J0509 + 3801	26.1	1.6	$5.3 \cdot 10^{-27}$	$4.0 \cdot 10^{-26}$	$8.7 \cdot 10^{-5}$	0.7
J0557 + 1550	782.4	1.8	$7.5 \cdot 10^{-28}$	$1.1 \cdot 10^{-26}$	$3.2 \cdot 10^{-8}$	0.33
J0557 - 2948	45.8	4.3	$2.4 \cdot 10^{-28}$	$1.1 \cdot 10^{-26}$	$2.1 \cdot 10^{-5}$	0.65
J0609 + 2130	35.9	0.6	$2.9 \cdot 10^{-27}$	$1.8 \cdot 10^{-26}$	$7.3 \cdot 10^{-6}$	0.73
J0610 - 2100	518.0	3.3	$1.3 \cdot 10^{-28}$	$3.2 \cdot 10^{-26}$	$3.6 \cdot 10^{-7}$	0.63
J0613-0200	653.2	0.6	$2.2 \cdot 10^{-27}$	$6.9 \cdot 10^{-27}$	$9.2 \cdot 10^{-9}$	0.96
J0614 - 3329	635.2	0.6	$3.0 \cdot 10^{-27}$	$8.2 \cdot 10^{-27}$	$1.2 \cdot 10^{-8}$	0.56
J0621 + 1002	69.3	0.4	$2.4 \cdot 10^{-27}$	$8.8 \cdot 10^{-27}$	$7.3 \cdot 10^{-7}$	0.34
J0636-3044	506.9	0.7	$2.6 \cdot 10^{-27}$	$3.1 \cdot 10^{-26}$	$8.1 \cdot 10^{-8}$	0.71
J0636 + 5129	697.1	0.2	$4.2 \cdot 10^{-27}$	$6.3 \cdot 10^{-27}$	$2.6 \cdot 10^{-9}$	1
J0645 + 5158	225.9	1.2	$3.7 \cdot 10^{-28}$	$4.7 \cdot 10^{-27}$	$1.1 \cdot 10^{-7}$	0.86
J0709 + 0458	58.1	1.2	$2.2 \cdot 10^{-27}$	$9.1 \cdot 10^{-27}$	$3.1 \cdot 10^{-6}$	0.78
J0711-6830	364.2	0.1	$1.2 \cdot 10^{-26}$	$4.8 \cdot 10^{-27}$	$3.8 \cdot 10^{-9}$	0.91
J0721 - 2038	128.7	2.7	$5.1 \cdot 10^{-28}$	$6.0 \cdot 10^{-27}$	$9.2 \cdot 10^{-7}$	0.59
J0732 + 2314	489.0	1.1	$8.5 \cdot 10^{-28}$	$6.8 \cdot 10^{-27}$	$3.1 \cdot 10^{-8}$	0.76
J0740 + 6620	693.1	1.1	$1.1 \cdot 10^{-27}$	$1.0 \cdot 10^{-26}$	$2.3 \cdot 10^{-8}$	0.21
J0751 + 1807	574.9	0.6	$1.9 \cdot 10^{-27}$	$8.4 \cdot 10^{-27}$	$1.4 \cdot 10^{-8}$	0.62
J0824 + 0028	202.8	1.7	$1.8 \cdot 10^{-27}$	$1.1 \cdot 10^{-26}$	$4.2 \cdot 10^{-7}$	0.01
J0835 - 4510	22.4	0.3	$3.4 \cdot 10^{-24}$	$1.1 \cdot 10^{-25}$	$5.6 \cdot 10^{-5}$	0.26
J0921 - 5202	206.6	0.4	$2.9 \cdot 10^{-27}$	$5.1 \cdot 10^{-27}$	$4.5 \cdot 10^{-8}$	0.73
J0931 - 1902	431.2	3.7	$1.8 \cdot 10^{-28}$	$5.9 \cdot 10^{-27}$	$1.1 \cdot 10^{-7}$	0.84
J0955 - 6150	1000.3	2.2	$9.9\cdot10^{-28}$	$1.3 \cdot 10^{-26}$	$2.6 \cdot 10^{-8}$	0.51
J1012 - 4235	644.9	0.4	$3.1 \cdot 10^{-27}$	$7.9 \cdot 10^{-27}$	$6.7\cdot 10^{-9}$	0.61
J1012 + 5307	380.5	0.7	$1.6 \cdot 10^{-27}$	$7.2 \cdot 10^{-27}$	$3.3 \cdot 10^{-8}$	0.3
J1017 - 7156	855.2	3.5	$2.5 \cdot 10^{-28}$	$7.3 \cdot 10^{-27}$	$3.3 \cdot 10^{-8}$	0.97
J1022 + 1001	121.6	0.6	$1.8 \cdot 10^{-27}$	$6.4 \cdot 10^{-27}$	$2.6 \cdot 10^{-7}$	0.56
J1024 - 0719	387.4	1.2	-	$6.1 \cdot 10^{-27}$	$4.6 \cdot 10^{-8}$	0.75
J1035 - 6720	696.4	1.5	$2.2 \cdot 10^{-27}$	$6.5 \cdot 10^{-27}$	$1.8 \cdot 10^{-8}$	0.96
J1036 - 8317	586.7	0.9	$2.6 \cdot 10^{-27}$	$6.6 \cdot 10^{-27}$	$1.7 \cdot 10^{-8}$	0.74
J1038 + 0032	69.3	6.0	$2.1 \cdot 10^{-28}$	$7.6 \cdot 10^{-27}$	$8.9 \cdot 10^{-6}$	0.59
J1045 - 4509	267.6	0.6	$2.1 \cdot 10^{-27}$	$4.8 \cdot 10^{-27}$	$3.7 \cdot 10^{-8}$	0.91
J1101 - 6101	31.8	7.0	$4.2 \cdot 10^{-26}$	$2.3 \cdot 10^{-26}$	$1.5 \cdot 10^{-4}$	0.62
J1101 - 6424	391.4	2.2	$2.2 \cdot 10^{-28}$	$6.1 \cdot 10^{-27}$	$8.1 \cdot 10^{-8}$	0.6
J1103-5403	589.5	1.7	$5.0 \cdot 10^{-28}$	$5.4 \cdot 10^{-27}$	$2.5\cdot 10^{-8}$	1

Pulsar name (J2000)	$f_{\rm gw}$ (Hz)	Distance (kpc)	$h_{ m sd}$	$h_0^{95\%}$	$\epsilon^{95\%}$	P-value
J1125 - 5825	644.7	1.7	$2.0 \cdot 10^{-27}$	$7.0 \cdot 10^{-27}$	$2.8 \cdot 10^{-8}$	0.78
J1125 - 6014	760.3	1.4	$7.1 \cdot 10^{-28}$	$7.7 \cdot 10^{-27}$	$1.8 \cdot 10^{-8}$	0.78
J1125 + 7819	476.0	0.9	-	$7.3 \cdot 10^{-27}$	$2.7 \cdot 10^{-8}$	0.48
J1142+0119	394.1	2.2	-	$1.0 \cdot 10^{-26}$	$1.3 \cdot 10^{-7}$	0.067
J1207 - 5050	413.0	1.3	$6.9 \cdot 10^{-28}$	$8.4 \cdot 10^{-27}$	$5.9 \cdot 10^{-8}$	0.17
J1216 - 6410	565.1	1.1	$5.0 \cdot 10^{-28}$	$5.9 \cdot 10^{-27}$	$1.9 \cdot 10^{-8}$	0.92
J1231-1411	542.9	0.4	$2.9 \cdot 10^{-27}$	$9.4 \cdot 10^{-27}$	$1.3 \cdot 10^{-8}$	0.29
J1300 + 1240	321.6	0.6	-	$6.1 \cdot 10^{-27}$	$3.4 \cdot 10^{-8}$	0.64
J1302 - 3258	530.4	1.4	$7.4 \cdot 10^{-28}$	$7.1 \cdot 10^{-27}$	$3.4 \cdot 10^{-8}$	0.67
J1302 - 6350	41.9	2.3	$7.7 \cdot 10^{-26}$	$9.9 \cdot 10^{-27}$	$1.2 \cdot 10^{-5}$	0.97
J1312 + 0051	473.0	1.5	$7.6 \cdot 10^{-28}$	$9.8 \cdot 10^{-27}$	$6.1 \cdot 10^{-8}$	0.21
J1327 - 0755	746.8	25.0	-	$7.9\cdot10^{-27}$	$3.3 \cdot 10^{-7}$	0.9
J1327+3423	48.2	-	-	$1.3 \cdot 10^{-26}$	-	0.5
J1337 - 6423	212.2	5.9	$1.9 \cdot 10^{-28}$	$7.5 \cdot 10^{-27}$	$9.3 \cdot 10^{-7}$	0.13
J1400 - 1431	648.5	0.3	$5.1 \cdot 10^{-28}$	$6.7 \cdot 10^{-27}$	$4.0 \cdot 10^{-9}$	0.98
J1411 + 2551	32.0	1.1	$8.5 \cdot 10^{-28}$	$2.8 \cdot 10^{-26}$	$2.9\cdot 10^{-5}$	0.3
J1412 + 7922	33.8	2.0	$9.5 \cdot 10^{-26}$	$2.0 \cdot 10^{-26}$	$3.3 \cdot 10^{-5}$	0.48
J1420 - 5625	58.6	1.3	$8.5 \cdot 10^{-28}$	$8.0 \cdot 10^{-27}$	$2.9 \cdot 10^{-6}$	0.88
J1421 - 4409	313.2	2.1	$3.8 \cdot 10^{-28}$	$5.9 \cdot 10^{-27}$	$1.2 \cdot 10^{-7}$	0.59
J1431 - 5740	486.6	3.5	$2.8 \cdot 10^{-28}$	$7.6 \cdot 10^{-27}$	$1.1 \cdot 10^{-7}$	0.44
J1435 - 6100	214.0	2.8	$4.6 \cdot 10^{-28}$	$9.1 \cdot 10^{-27}$	$5.3 \cdot 10^{-7}$	0.024
J1439 - 5501	69.8	0.7	$2.7 \cdot 10^{-27}$	$8.5 \cdot 10^{-27}$	$1.1 \cdot 10^{-6}$	0.21
J1446 - 4701	911.3	1.5	$1.1 \cdot 10^{-27}$	$9.6 \cdot 10^{-27}$	$1.6 \cdot 10^{-8}$	0.69
J1453 + 1902	345.3	1.3	$8.0 \cdot 10^{-28}$	$6.9 \cdot 10^{-27}$	$7.0 \cdot 10^{-8}$	0.44
J1455 - 3330	250.4	1.0	$1.3 \cdot 10^{-27}$	$6.7 \cdot 10^{-27}$	$1.0 \cdot 10^{-7}$	0.41
J1502 - 6752	74.8	7.7	$3.0 \cdot 10^{-28}$	$5.8 \cdot 10^{-27}$	$7.5 \cdot 10^{-6}$	0.84
J1513 - 2550	943.8	4.0	$6.5 \cdot 10^{-28}$	$1.4 \cdot 10^{-26}$	$5.7 \cdot 10^{-8}$	0.26
J1514-4946	557.2	0.9	$1.6 \cdot 10^{-27}$	$1.0 \cdot 10^{-26}$	$2.9 \cdot 10^{-8}$	0.19
J1518+0204A	360.1	8.0	$2.8 \cdot 10^{-28}$	$5.6 \cdot 10^{-27}$	$3.3 \cdot 10^{-7}$	1
J1518+4904	48.9	1.0	$6.3 \cdot 10^{-28}$	$9.7 \cdot 10^{-27}$	$3.7 \cdot 10^{-6}$	0.97
J1525-5545	176.1	3.1	$8.7 \cdot 10^{-28}$	$4.9 \cdot 10^{-27}$	$4.7 \cdot 10^{-7}$	0.81
J1528-3146	32.9	0.8	$2.1 \cdot 10^{-27}$	$2.5 \cdot 10^{-26}$	$1.7 \cdot 10^{-5}$	0.41
J1529-3828	235.7	4.3	$\begin{array}{c} 3.4 \cdot 10^{-28} \\ 6.0 \cdot 10^{-27} \end{array}$	$\frac{4.5 \cdot 10^{-27}}{1.3 \cdot 10^{-26}}$	$3.3 \cdot 10^{-7} \\ 4.8 \cdot 10^{-6}$	0.97
J1537+1155	52.8	1.1	$1.9 \cdot 10^{-27}$	$9.2 \cdot 10^{-27}$	$4.8 \cdot 10^{-8}$ $1.1 \cdot 10^{-8}$	0.17
J1543-5149	972.3 926.2	$1.1 \\ 3.0$	$1.9 \cdot 10$ $3.1 \cdot 10^{-28}$	$9.2 \cdot 10$ $1.7 \cdot 10^{-26}$	$1.1 \cdot 10^{-8}$ $5.7 \cdot 10^{-8}$	$0.85 \\ 0.019$
J1544 + 4937 J1545 - 4550	920.2 559.4	$\frac{3.0}{2.2}$	$3.1 \cdot 10$ $1.4 \cdot 10^{-27}$	$1.7 \cdot 10$ $9.5 \cdot 10^{-27}$	$5.7 \cdot 10^{-8}$ $6.3 \cdot 10^{-8}$	0.019 0.32
J1543 - 4550 J1547 - 5709			$3.9 \cdot 10^{-28}$	$5.5 \cdot 10^{-27}$ $7.8 \cdot 10^{-27}$	$9.2 \cdot 10^{-8}$	
J1547 - 5709 J1551 - 0658	$466.1 \\ 281.9$	2.7 1.3	$1.0 \cdot 10^{-27}$	$8.5 \cdot 10^{-27}$	$9.2 \cdot 10$ $1.3 \cdot 10^{-7}$	$0.32 \\ 0.15$
J1600 - 3053	555.9	3.0	$4.0 \cdot 10^{-28}$	$9.9 \cdot 10^{-27}$	$9.1 \cdot 10^{-8}$	$0.15 \\ 0.25$
J1603 - 7202	134.8	3.4	$2.5 \cdot 10^{-28}$	$4.5 \cdot 10^{-27}$	$8.0 \cdot 10^{-7}$	0.23
J1614 - 2230	634.8	0.7	$1.2 \cdot 10^{-27}$	$7.6 \cdot 10^{-27}$	$1.2 \cdot 10^{-8}$	0.76
J1618-3921	166.8	5.5	$3.1 \cdot 10^{-28}$	$9.3 \cdot 10^{-27}$	$1.2 \cdot 10^{-6}$ $1.7 \cdot 10^{-6}$	0.036
J1618 - 4624	337.2	3.0	$1.9 \cdot 10^{-28}$	$6.1 \cdot 10^{-27}$	$1.5 \cdot 10^{-7}$	0.56
J1622 - 6617	84.7	4.0	$2.9 \cdot 10^{-28}$	$6.0 \cdot 10^{-27}$	$3.2 \cdot 10^{-6}$	0.69
J1623-2631	180.6	1.8	$1.3 \cdot 10^{-27}$	$5.0 \cdot 10^{-27}$	$2.6 \cdot 10^{-7}$	0.92
J1628 - 3205	622.7	1.2	-	$7.1 \cdot 10^{-27}$	$2.1 \cdot 10^{-8}$	0.79
J1629 - 6902	333.3	1.0	$1.1\cdot 10^{-27}$	$6.0 \cdot 10^{-27}$	$4.9 \cdot 10^{-8}$	0.79
J1630 + 3734	602.8	1.2	$1.1 \cdot 10^{-27}$	$7.9 \cdot 10^{-27}$	$2.5 \cdot 10^{-8}$	0.53
J1640+2224	632.2	1.5	$3.4 \cdot 10^{-28}$	$1.1 \cdot 10^{-26}$	$3.9 \cdot 10^{-8}$	0.17
J1641+3627A	192.7	7.1	$3.2 \cdot 10^{-28}$	$4.3 \cdot 10^{-27}$	$7.7 \cdot 10^{-7}$	1
J1643-1224	432.7	1.2	$1.3 \cdot 10^{-27}$	$1.1 \cdot 10^{-26}$	$6.6 \cdot 10^{-8}$	0.045
J1652 - 4838	528.4	-	-	$9.7 \cdot 10^{-27}$	-	0.14
J1653 - 2054	484.4	2.6	$5.0 \cdot 10^{-28}$	$7.5 \cdot 10^{-27}$	$8.0\cdot10^{-8}$	0.6
J1658 - 5324	819.9	0.9	$1.9 \cdot 10^{-27}$	$1.1 \cdot 10^{-26}$	$1.4 \cdot 10^{-8}$	0.3
J1705 - 1903	806.4	2.4	$9.8 \cdot 10^{-28}$	$1.2 \cdot 10^{-26}$	$4.0 \cdot 10^{-8}$	0.33
J1708 - 3506	443.9	3.3	$3.4 \cdot 10^{-28}$	$6.2 \cdot 10^{-27}$	$9.9 \cdot 10^{-8}$	0.74
J1709 + 2313	431.9	2.2	$1.9\cdot10^{-28}$	$6.4 \cdot 10^{-27}$	$7.1\cdot 10^{-8}$	0.68

Dulcar name	f	Distance	h	$h_0^{95\%}$	$\epsilon^{95\%}$	D voluo
Pulsar name (J2000)	$f_{ m gw}$ (Hz)	$\begin{array}{c} { m Distance} \\ { m (kpc)} \end{array}$	$h_{ m sd}$	n_0	e	P-value
(32000)	(112)	(kpc)				
J1713+0747	437.6	1.0	$1.1 \cdot 10^{-27}$	$7.0 \cdot 10^{-27}$	$3.5 \cdot 10^{-8}$	0.59
J1719 - 1438	437.0 345.4	0.3	$2.6 \cdot 10^{-27}$	$8.0 \cdot 10^{-27}$	$2.1 \cdot 10^{-8}$	0.39 0.25
J1721 - 2457	540.4 572.0	1.4	2.0 10	$8.0 \cdot 10^{-27}$	$3.1 \cdot 10^{-8}$	0.29 0.59
J1727-2946	73.8	1.4	$1.3 \cdot 10^{-27}$	$9.3 \cdot 10^{-27}$	$3.0 \cdot 10^{-6}$	0.35
J1729 - 2340 J1729 - 2117	30.2	1.9	$1.3 \cdot 10^{-27}$ $1.3 \cdot 10^{-27}$	$2.6 \cdot 10^{-26}$	$2.7 \cdot 10^{-5}$	0.2
J1730 - 2304	246.2	0.5	$2.0 \cdot 10^{-27}$	$5.8 \cdot 10^{-27}$	$4.2 \cdot 10^{-8}$	0.64
J1732 - 5049	376.5	1.9	$6.2 \cdot 10^{-28}$	$4.6 \cdot 10^{-27}$	$5.8 \cdot 10^{-8}$	1
J1732 - 0043 J1737-0811	479.0	0.2	$5.4 \cdot 10^{-27}$	$8.4 \cdot 10^{-27}$	$7.3 \cdot 10^{-9}$	0.44
J1738+0333	341.9	1.5	$1.1 \cdot 10^{-27}$	$7.1 \cdot 10^{-27}$	$8.5 \cdot 10^{-8}$	0.44
J1741+1351	533.7	1.5	$2.1 \cdot 10^{-27}$	$6.4 \cdot 10^{-27}$	$2.3 \cdot 10^{-8}$	0.9
J1744 - 1134	490.9	0.4	$2.6 \cdot 10^{-27}$	$1.1 \cdot 10^{-26}$	$1.8 \cdot 10^{-8}$	0.087
J1745 - 0952	103.2	0.2	$7.5 \cdot 10^{-27}$	$5.7 \cdot 10^{-27}$	$1.2 \cdot 10^{-7}$	0.82
J1745 + 1017	754.1	1.2	$6.0 \cdot 10^{-28}$	$1.1 \cdot 10^{-26}$	$2.2 \cdot 10^{-8}$	0.38
J1747 - 4036	1215.4	7.2	$2.9 \cdot 10^{-28}$	$2.1 \cdot 10^{-26}$	$9.8 \cdot 10^{-8}$	0.036
J1748-2446A	173.0	6.9	$3.3 \cdot 10^{-28}$	$5.3 \cdot 10^{-27}$	$1.2 \cdot 10^{-6}$	0.76
J1748-3009	206.5	5.0	-	$8.0 \cdot 10^{-27}$	$9.0 \cdot 10^{-7}$	0.13
J1750 - 2536	57.6	3.2	$5.1 \cdot 10^{-28}$	$8.9 \cdot 10^{-27}$	$8.2 \cdot 10^{-6}$	0.74
J1751-2857	510.9	1.1	$1.2 \cdot 10^{-27}$	$6.3 \cdot 10^{-26}$	$2.5 \cdot 10^{-7}$	0.088
J1753-1914	31.8	2.9	$1.6 \cdot 10^{-27}$	$2.6 \cdot 10^{-26}$	$7.2 \cdot 10^{-5}$	0.56
J1753 - 2240	21.0	3.2	$8.0 \cdot 10^{-28}$	$1.7 \cdot 10^{-25}$	$1.2 \cdot 10^{-3}$	0.33
J1755 - 3716	156.4	8.2	$1.5 \cdot 10^{-28}$	$6.4 \cdot 10^{-27}$	$2.0 \cdot 10^{-6}$	0.41
J1756 - 2251	70.3	0.7	$6.6 \cdot 10^{-27}$	$8.8 \cdot 10^{-27}$	$1.2 \cdot 10^{-6}$	0.41
J1757 - 1854	93.0	19.6	$4.6 \cdot 10^{-28}$	$1.2 \cdot 10^{-26}$	$2.5 \cdot 10^{-5}$	0.018
J1757 - 5322	225.5	0.9	$1.5 \cdot 10^{-27}$	$6.0 \cdot 10^{-27}$	$1.0 \cdot 10^{-7}$	0.45
J1801 - 1417	551.7	1.1	$7.4 \cdot 10^{-28}$	$8.9 \cdot 10^{-27}$	$3.0 \cdot 10^{-8}$	0.41
J1801 - 3210	268.3	6.1	-	$6.2 \cdot 10^{-27}$	$5.0 \cdot 10^{-7}$	0.52
J1802 - 2124	158.1	0.8	$2.5 \cdot 10^{-27}$	$6.4 \cdot 10^{-27}$	$1.8 \cdot 10^{-7}$	0.49
J1804 - 0735	86.6	7.8	$2.9 \cdot 10^{-28}$	$7.8 \cdot 10^{-27}$	$7.7 \cdot 10^{-6}$	0.39
J1804 - 2717	214.1	0.8	$1.9\cdot 10^{-27}$	$6.1 \cdot 10^{-27}$	$1.0 \cdot 10^{-7}$	0.51
J1807 - 2459 A	653.7	3.0	$7.6 \cdot 10^{-28}$	$9.4 \cdot 10^{-27}$	$6.3 \cdot 10^{-8}$	0.41
J1809 - 1917	24.2	3.3	$1.4 \cdot 10^{-25}$	$5.6 \cdot 10^{-26}$	$3.0 \cdot 10^{-4}$	0.85
J1810 + 1744	1202.8	2.4	$5.5 \cdot 10^{-28}$	$1.2 \cdot 10^{-26}$	$1.8 \cdot 10^{-8}$	0.82
J1810 - 2005	60.9	3.5	$2.9 \cdot 10^{-28}$	$8.5 \cdot 10^{-27}$	$7.6 \cdot 10^{-6}$	0.69
J1811 - 2405	751.7	1.8	$9.9 \cdot 10^{-28}$	$7.2 \cdot 10^{-27}$	$2.2 \cdot 10^{-8}$	0.98
J1813 - 1749	44.7	6.2	$2.2\cdot10^{-25}$	$1.1 \cdot 10^{-26}$	$3.1 \cdot 10^{-5}$	0.89
J1813 - 2621	451.5	3.2	-	$5.4 \cdot 10^{-27}$	$8.0 \cdot 10^{-8}$	0.98
J1821 + 0155	59.2	1.7	$4.3 \cdot 10^{-28}$	$9.1 \cdot 10^{-27}$	$4.2 \cdot 10^{-6}$	0.92
J1823-3021A	367.6	7.9	$2.9 \cdot 10^{-28}$	$8.6 \cdot 10^{-27}$	$4.8 \cdot 10^{-7}$	0.15
J1824-2452A	654.8	5.5	$4.1 \cdot 10^{-28}$	$8.7 \cdot 10^{-27}$	$1.1 \cdot 10^{-7}$	0.55
J1825-0319	439.2	3.9	$2.6 \cdot 10^{-28}$	$5.5 \cdot 10^{-27}$	$1.0 \cdot 10^{-7}$	0.98
J1826-2415	425.9	2.7	$5.7 \cdot 10^{-28}$	$7.0 \cdot 10^{-27}$	$10.0 \cdot 10^{-8}$	0.53
J1828-1101	27.8	4.8	$7.7 \cdot 10^{-26}$	$3.2 \cdot 10^{-26}$	$1.9 \cdot 10^{-4}$	0.91
J1829+2456	48.8	0.9	$10.0 \cdot 10^{-28}$	$1.4 \cdot 10^{-26}$	$5.2 \cdot 10^{-6}$	0.57
J1832-0836	735.5	1.6	-	$1.4 \cdot 10^{-26}$	$3.8 \cdot 10^{-8}$	0.093
J1833-0827	23.4	4.5	$5.9 \cdot 10^{-26}$	$6.1 \cdot 10^{-26}$	$4.7 \cdot 10^{-4}$	0.91
J1835-0114	390.9	3.5 C.C	$\begin{array}{c} 2.7 \cdot 10^{-28} \\ 1.0 \cdot 10^{-25} \end{array}$	$6.4 \cdot 10^{-27}$ $3.4 \cdot 10^{-26}$	$1.4 \cdot 10^{-7}$	0.71
J1838-0655	28.4	6.6 5.0	$1.0 \cdot 10^{-28}$ $2.6 \cdot 10^{-28}$	$3.4 \cdot 10^{-20}$ $8.5 \cdot 10^{-27}$	$2.6 \cdot 10^{-4} \\ 1.3 \cdot 10^{-5}$	0.72
J1840 - 0643 J1841 + 0120	56.2	5.0	$2.6 \cdot 10^{-23}$ $3.2 \cdot 10^{-27}$	$8.5 \cdot 10^{-26}$ $1.2 \cdot 10^{-26}$	$1.3 \cdot 10^{-5}$ $1.1 \cdot 10^{-5}$	0.82
J1841+0130 J1843-1113	$67.2 \\ 1083.6$	$4.2 \\ 1.3$	$3.2 \cdot 10^{-27}$ $1.4 \cdot 10^{-27}$	$1.2 \cdot 10^{-26}$ $2.2 \cdot 10^{-26}$	$1.1 \cdot 10^{-8}$ $2.2 \cdot 10^{-8}$	$0.037 \\ 0.019$
J1843–1113 J1843–1448	1083.6 365.5	1.3 3.5	$1.4 \cdot 10$	$2.2 \cdot 10^{-23}$ $8.3 \cdot 10^{-27}$	$2.2 \cdot 10^{-7}$ $2.0 \cdot 10^{-7}$	0.019 0.23
			$-7.0 \cdot 10^{-26}$	$8.3 \cdot 10^{-26}$ $1.5 \cdot 10^{-26}$	$2.0 \cdot 10^{-5}$ $3.8 \cdot 10^{-5}$	
J1849-0001	51.9	7.0	$7.0 \cdot 10^{-28}$ $8.9 \cdot 10^{-28}$	$1.5 \cdot 10^{-20}$ $1.2 \cdot 10^{-26}$	$3.8 \cdot 10^{-8}$ $6.1 \cdot 10^{-8}$	0.08
J1853+1303 I1856+0245	488.8	$1.3 \\ 6.3$	$8.9 \cdot 10^{-25}$ $1.1 \cdot 10^{-25}$	$1.2 \cdot 10^{-20}$ $5.7 \cdot 10^{-26}$	$6.1 \cdot 10^{-6}$ $5.6 \cdot 10^{-4}$	$\begin{array}{c} 0.058 \\ 0.69 \end{array}$
J1856+0245 J1857+0943	$24.7 \\ 373.0$	6.3 1.2	$1.1 \cdot 10^{-27}$ $1.2 \cdot 10^{-27}$	$5.7 \cdot 10^{-23}$ $7.2 \cdot 10^{-27}$	$5.6 \cdot 10^{-8}$ $5.8 \cdot 10^{-8}$	$\begin{array}{c} 0.69 \\ 0.48 \end{array}$
J1857 + 0943 J1902 - 5105	373.0 1147.8		$1.2 \cdot 10^{-27}$ $1.1 \cdot 10^{-27}$	$1.3 \cdot 10^{-26}$	$5.8 \cdot 10^{-8}$ $1.5 \cdot 10^{-8}$	$\begin{array}{c} 0.48 \\ 0.59 \end{array}$
J1902 - 5105 J1903 + 0327	930.3	$\begin{array}{c} 1.6 \\ 6.1 \end{array}$	$1.1 \cdot 10^{-28}$ $3.9 \cdot 10^{-28}$	$1.3 \cdot 10^{-26}$ $1.4 \cdot 10^{-26}$	$1.5 \cdot 10^{-8}$ $9.3 \cdot 10^{-8}$	$\begin{array}{c} 0.59 \\ 0.24 \end{array}$
J1903+0327 J1903-7051	930.3 555.9	$0.1 \\ 0.9$	$3.9 \cdot 10^{-27}$ $1.3 \cdot 10^{-27}$	$1.4 \cdot 10^{-23}$ $6.7 \cdot 10^{-27}$	$9.3 \cdot 10^{-8}$ $1.9 \cdot 10^{-8}$	$\begin{array}{c} 0.24 \\ 0.77 \end{array}$
11909-1091	000.9	0.9	1.9.10	0.7.10	1.9.10	0.77

Pulsar name (J2000)	$f_{\rm gw}$ (Hz)	Distance (kpc)	$h_{ m sd}$	$h_0^{95\%}$	$\epsilon^{95\%}$	P-value
J1904+0412	28.1	4.6	$2.2 \cdot 10^{-28}$	$2.9 \cdot 10^{-26}$	$1.6 \cdot 10^{-4}$	0.98
J1905 + 0400	528.5	1.1	$8.0 \cdot 10^{-28}$	$7.3 \cdot 10^{-27}$	$2.6 \cdot 10^{-8}$	0.68
J1909-3744	678.6	1.1	$6.6 \cdot 10^{-28}$	$8.1 \cdot 10^{-27}$	$1.9 \cdot 10^{-8}$	0.64
J1910 + 1256	401.3	1.5	$7.2 \cdot 10^{-28}$	$8.1 \cdot 10^{-27}$	$7.2 \cdot 10^{-8}$	0.29
J1911-1114	551.6	1.1	$1.3 \cdot 10^{-27}$	$1.2 \cdot 10^{-26}$	$4.0 \cdot 10^{-8}$	0.067
J1911+1347	432.3	1.4	$1.1 \cdot 10^{-27}$	$7.1 \cdot 10^{-27}$	$4.9 \cdot 10^{-8}$	0.54
J1913+1011	55.7	4.6	$5.3 \cdot 10^{-26}$	$8.6 \cdot 10^{-27}$	$1.2 \cdot 10^{-5}$	0.82
J1914 + 0659	108.0	8.5	$1.2 \cdot 10^{-28}$	$8.1 \cdot 10^{-27}$	$5.6 \cdot 10^{-6}$	0.23
J1915 + 1606	33.9	5.2	$1.9 \cdot 10^{-27}$	$2.6 \cdot 10^{-26}$	$1.1 \cdot 10^{-4}$	0.21
J1918-0642	261.6	1.1	$1.3 \cdot 10^{-27}$	$6.7 \cdot 10^{-27}$	$1.0 \cdot 10^{-7}$	0.45
J1923 + 2515	528.0	1.2	$9.1 \cdot 10^{-28}$	$1.0 \cdot 10^{-26}$	$4.1 \cdot 10^{-8}$	0.15
J1925+1720	26.4	5.1	$5.9 \cdot 10^{-26}$	$7.0 \cdot 10^{-26}$	$4.8 \cdot 10^{-4}$	0.039
J1928+1746	29.1	4.3	$8.2 \cdot 10^{-26}$	$3.4 \cdot 10^{-26}$	$1.6 \cdot 10^{-4}$	0.54
J1933-6211	564.4	0.7	$1.1 \cdot 10^{-27}$	$6.9 \cdot 10^{-27}$	$1.3 \cdot 10^{-8}$	0.66
J1935 + 2025	25.0	4.6	$1.5 \cdot 10^{-25}$	$4.9 \cdot 10^{-26}$	$3.4 \cdot 10^{-4}$	0.66
J1939+2134	1283.9	4.8	$1.4 \cdot 10^{-27}$	$1.4 \cdot 10^{-26}$	$4.0 \cdot 10^{-8}$	0.59
J1943+2210	393.4	6.8	$1.6 \cdot 10^{-28}$	$6.4 \cdot 10^{-27}$	$2.6 \cdot 10^{-7}$	0.62
J1944 + 0907	385.7	1.2	$7.4 \cdot 10^{-28}$	$6.1 \cdot 10^{-27}$	$4.8 \cdot 10^{-8}$	0.75
J1946 + 3417	630.9	6.9	$6.5 \cdot 10^{-29}$	$9.3 \cdot 10^{-27}$	$1.5 \cdot 10^{-7}$	0.34
J1946-5403	737.8	1.1	$7.0 \cdot 10^{-28}$	$7.1 \cdot 10^{-27}$	$1.4 \cdot 10^{-8}$	0.89
J1949 + 3106	152.2	7.5	$2.9 \cdot 10^{-28}$	$5.8 \cdot 10^{-27}$	$1.8 \cdot 10^{-6}$	0.67
J1950+2414	464.6	7.3	$2.4 \cdot 10^{-28}$	$6.8 \cdot 10^{-27}$	$2.2 \cdot 10^{-7}$	0.67
J1952 + 3252	50.6	3.0	$1.0 \cdot 10^{-25}$	$1.3 \cdot 10^{-26}$	$1.4 \cdot 10^{-5}$	0.22
J1955+2527	410.4	8.2	$1.5 \cdot 10^{-28}$	$7.7 \cdot 10^{-27}$	$3.5 \cdot 10^{-7}$	0.36
J1955+2908	326.1	6.3	$2.9 \cdot 10^{-28}$	$6.6 \cdot 10^{-27}$	$3.7 \cdot 10^{-7}$	0.46
J2007+2722	81.6	7.1	$7.1 \cdot 10^{-28}$	$1.1 \cdot 10^{-26}$	$1.1 \cdot 10^{-5}$	0.037
J2010-1323	382.9	1.2	$5.3 \cdot 10^{-28}$	$8.4 \cdot 10^{-27}$	$6.3 \cdot 10^{-8}$	0.22
J2017 + 0603	690.6	1.4	$9.6 \cdot 10^{-28}$	$8.9 \cdot 10^{-27}$	$2.5 \cdot 10^{-8}$	0.6
J2019+2425	508.3	1.2	$4.4 \cdot 10^{-28}$	$5.4 \cdot 10^{-26}$	$2.3 \cdot 10^{-7}$	0.046
J2022+2534	755.9	-	_	$1.2 \cdot 10^{-26}$	_	0.2
J2033+1734	336.2	1.7	$5.5 \cdot 10^{-28}$	$5.2 \cdot 10^{-27}$	$7.6\cdot 10^{-8}$	0.92
J2039-3616	610.7	1.7	$7.6 \cdot 10^{-28}$	$7.6 \cdot 10^{-27}$	$3.3 \cdot 10^{-8}$	0.65
J2043+2740	20.8	1.5	$6.3 \cdot 10^{-26}$	$1.7 \cdot 10^{-25}$	$5.6 \cdot 10^{-4}$	0.32
J2045+3633	63.1	5.6	$6.2 \cdot 10^{-28}$	$9.1 \cdot 10^{-27}$	$1.2 \cdot 10^{-5}$	0.34
J2047+1053	466.6	2.8	$6.4 \cdot 10^{-28}$	$7.0 \cdot 10^{-27}$	$8.5 \cdot 10^{-8}$	0.69
J2053 + 4650	158.9	3.8	$7.8 \cdot 10^{-28}$	$4.6 \cdot 10^{-27}$	$6.6 \cdot 10^{-7}$	0.92
J2055+3829	957.3	4.6	$1.1 \cdot 10^{-28}$	$1.2 \cdot 10^{-26}$	$5.8 \cdot 10^{-8}$	0.36
J2124 - 3358	405.6	0.4	$2.3\cdot10^{-27}$	$8.0 \cdot 10^{-27}$	$2.0 \cdot 10^{-8}$	0.28
J2129 - 5721	536.7	7.0	$2.6 \cdot 10^{-28}$	$7.8 \cdot 10^{-27}$	$1.8 \cdot 10^{-7}$	0.41
J2144 - 5237	396.7	1.7	$6.5 \cdot 10^{-28}$	$6.0 \cdot 10^{-27}$	$6.0 \cdot 10^{-8}$	0.63
J2145 - 0750	124.6	0.8	$1.3 \cdot 10^{-27}$	$6.5 \cdot 10^{-27}$	$3.3 \cdot 10^{-7}$	0.52
J2150 - 0326	569.7	-	-	$8.9 \cdot 10^{-27}$	-	0.46
J2205 + 6012	828.0	3.5	$6.5 \cdot 10^{-28}$	$8.9 \cdot 10^{-27}$	$4.3 \cdot 10^{-8}$	0.7
J2214 + 3000	641.2	0.6	$2.7 \cdot 10^{-27}$	$6.8 \cdot 10^{-27}$	$9.3 \cdot 10^{-9}$	0.92
J2222 - 0137	60.9	0.3	$2.0 \cdot 10^{-27}$	$7.2 \cdot 10^{-27}$	$5.0 \cdot 10^{-7}$	0.91
J2229 + 2643	671.6	1.8	$3.1 \cdot 10^{-28}$	$1.1 \cdot 10^{-26}$	$4.2 \cdot 10^{-8}$	0.19
J2229 + 6114	38.7	3.0	$3.3 \cdot 10^{-25}$	$1.3 \cdot 10^{-26}$	$2.4 \cdot 10^{-5}$	0.8
J2234 + 0611	559.2	1.5	$8.2 \cdot 10^{-28}$	$1.3 \cdot 10^{-26}$	$5.9\cdot 10^{-8}$	0.071
J2234 + 0944	551.4	0.8	$1.9 \cdot 10^{-27}$	$7.6 \cdot 10^{-27}$	$1.9\cdot 10^{-8}$	0.68
J2235 + 1506	33.5	1.5	$6.5 \cdot 10^{-28}$	$2.3 \cdot 10^{-26}$	$2.9\cdot 10^{-5}$	0.53
J2236 - 5527	289.5	2.0	$4.6 \cdot 10^{-28}$	$5.0 \cdot 10^{-27}$	$1.2 \cdot 10^{-7}$	0.78
J2241 - 5236	914.6	1.1	$1.2 \cdot 10^{-27}$	$1.4 \cdot 10^{-26}$	$1.7\cdot 10^{-8}$	0.097
J2256 - 1024	871.6	1.3	$1.3\cdot 10^{-27}$	$1.6 \cdot 10^{-26}$	$2.7\cdot 10^{-8}$	0.057
J2302 + 4442	385.2	0.9	$1.5 \cdot 10^{-27}$	$7.0 \cdot 10^{-27}$	$3.9\cdot 10^{-8}$	0.39
J2317 + 1439	580.5	2.2	$3.3 \cdot 10^{-28}$	$7.5 \cdot 10^{-27}$	$4.6 \cdot 10^{-8}$	0.72
J2322 + 2057	415.9	1.0	$6.5\cdot10^{-28}$	$6.2 \cdot 10^{-27}$	$3.4\cdot 10^{-8}$	0.77
J2322 - 2650	577.5	0.2	$1.2 \cdot 10^{-27}$	$7.0 \cdot 10^{-27}$	$4.6 \cdot 10^{-9}$	0.78

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