The Temporal Selfish Herd:

Predation risk whilst aggregations form

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Abstract

The hypothesis of the selfish herd has been highly influential to our understanding of animal aggregation. Various movement strategies have been proposed by which individuals might aggregate to form a selfish herd as a defence against predation, but although the spatial benefits of these strategies have been extensively studied, little attention has been paid to the importance of predator attacks that occur while the aggregation is forming. We investigate the success of mutant aggregation strategies invading populations of individuals using alternative strategies, and find the invasion dynamics depend critically on the timescale of movement. If predation occurs early in the movement sequence, simpler strategies are likely to prevail. If predators attack later, more complex strategies invade. If there is variation in the timing of predator attacks (through variation within or between individual predators), we hypothesise that groups will consist of a mixture of strategies, dependent upon the distribution of predator attack times. Thus, behavioural diversity can evolve and be maintained in populations of animals experiencing a diverse range of predators differing solely in their attack behaviour. This has implications for our understanding of predator-prey dynamics, as the timing of predator attacks will exert selection pressure on prey behavioural responses, to which predators must respond.

Keywords: selfish herd, aggregation, anti-predator behaviour, group living
Aggregation into groups of individuals is a widespread phenomenon across many animal species. There are a number of well-recognised benefits to aggregation through mechanisms that act to reduce predation risk (Krause & Ruxton 2002), including the dilution (Foster & Treherne 1981), encounter-dilution (Turner & Pitcher 1986) and confusion (Miller 1922; Krakauer 1995) effects, where the presence of other animals acts to reduce the risk to any given individual.

However, there are also potential costs to forming aggregations, of which the most commonly considered are reduction in resource uptake rate through competition; increased aggression; local resource depletion and increased detection by predators (for a review, see Krause & Ruxton 2002 and references therein). Thus, many taxa use grouping facultatively in response to the strength of perceived predation risk, initiating or enhancing aggregation in response to heightened threat (Foster & Treherne 1981; Watt et al. 1997; Viscido & Wethey 2002). The process of forming an aggregation can take a non-trivial amount of time, being dependent at least on the finite rates of turning and movement of the individuals concerned (James et al. 2004, Wood 2010). Thus it may commonly be that predators attack while the aggregation is forming. In contrast, existing theory, almost without exception, ignores this case and focuses on stable groups (that are either permanently maintained or are the behavioural outcome of the process of aggregation studied here).

A particularly influential body of theory for understanding the anti-predatory benefits of aggregation has been the Selfish Herd hypothesis stemming from the
classic paper of Hamilton (1971). This hypothesis assumes that the relative risk of
two individuals can be evaluated by comparison of the areas around them that
include all points closer to that individual than to any other (the so called ‘domains
of danger’). There has been important recent work refining the definition of domains
of danger (Beecham & Farnsworth 1999; James et al. 2004) and evaluating the types
of behavioural patterns that generate aggregations through the Selfish Herd effect
(Morton et al. 1994; Viscido et al. 2002; James et al. 2004; Reluga & Viscido 2005;
Wood & Ackland 2007; Morrell & James 2008). Many of these latter works take an
evolutionary approach, comparing the relative predation risk of interacting prey
adopting different strategies. However, implicitly or explicitly, these previous works
evaluate the relative effectiveness of different behavioural strategies only after the
process of aggregation has resulted in a stable group configuration. Here we aim to
generalise this to the biologically realistic case where attacks occur while
aggregations are still in the process of forming.

Facultative group formation may be triggered by cues that provide either
information about general risk of attack or warning of an impending specific attack.
An example of the first case may be aggregation driven by lower environmental light
levels (triggered by cloud formation or impending dusk) that are correlated with
enhanced attack rates by predators and/or reduced ability to detect or evade attacks
that do occur (Lima 1988; Metcalfe & Ure 1995). An example of the second might be
a predator that has to break from cover and travel a distance across open ground
before making contact with the prey (such as a cheetah stalking prey through long
grass before attacking; Schaller 1968). As soon as the predator breaks cover it is
likely to be much more easily detectable than it was previously. In response to such
detection there may be sufficient time for the prey to initiate (and perhaps even
complete) the process of aggregation before the predator has closed on the prey;
however sometimes the prey may still be in the process of aggregating when the
predator strikes. This last situation is an exemplar of the type of phenomenon
modelled in this paper.

As discussed above, the process of aggregation can be thought of as being triggered
by cues that a specific attack is imminent. However, the point at which individual
prey are at risk from the attack may be later than that (Bednekoff & Lima 1998).
Implicit in the concept of the domain of danger and its modifications is the issue of
target selection by the predator. A relatively large domain of danger indicates a large
relative risk of being the target of a particular attack (Hamilton 1971; Morton et al.
1994). If we take the example of a cheetah breaking cover from some trees and
closing in across grassland on a number of gazelle, it is likely that distance from cover
to any prey is sufficient that there may be changes in the relative positioning and
behaviour of the gazelle before the cheetah has closed sufficiently to tackle any one
individual. Hence, in such cases it is likely to be advantageous to the cheetah to delay
selection of a particular gazelle to target in the attack until some time into the
closing phase of its attack. It is at this moment of target selection that the relative
predation risks of prey in different positions (relative to others) most directly impacts
on the outcome of the attack for specific prey individuals (Bednekoff & Lima 1998).
Thus it is at this point in the predation sequence that the relative effectiveness of
different aggregation strategies is evaluated in our model. This moment may well
occur while the process of aggregation is still ongoing. Neill & Cullen (1974) and Lima (2002) both discuss the value of clearly separating predator strategy from tactics.

Our paper can be seen as a small step in correcting the current imbalance of research focus on the first of these. We deal not with the larger scale question of how animals trade-off predation risk and resource exploitation, but the finer-scale issue of identification of the anti-predator tactics that would be useful in different circumstances.

Throughout this paper, the timing of attacks refers to the timing of the moment of target selection by the predator relative to the time when the predator could first be detected by the prey (causing the prey to initiate defensive aggregation; Bednekoff & Lima 1998). We demonstrate the importance of considering the temporal aspect of movement decisions in the reduction of individual risk within groups of animals. We investigate the relative success of different movement rules, and the success of a mutant strategy invading a population of individuals using an alternative strategy. We explore a variety of rules of increasing complexity, since some complex movement rules have been criticized (Morton et al. 1994; Viscido et al. 2002) on the basis that they may be cognitively too demanding for animals to follow. We find that the invasion dynamics depend critically on the timescale of movement, and focus our evaluation of these results on the evolutionary consequences of variation in attack time.

Methods
We use the agent-based modelling framework described by James et al. (2004) and Morrell & James (2008) as the basis for our simulation model of aggregation behavior. $N$ point-like agents (prey individuals; we use $N=20$ as the default here) are placed in a two-dimensional circular arena of radius $R$ (measured in m, although the model is applicable to any unit) following a uniform random distribution. The density of individuals (per m$^2$) within the group, $d$, is given by $N/\pi R^2$. We investigate the effect of altering $N$ and $d (R)$ on the results in the electronic supplementary material. Each agent is surrounded by a two-dimensional domain of danger (a limited domain of danger, LDOD) in the shape of a circle of radius $r$, with a maximum area $A_{max} = \pi r^2$. We use the LDOD framework (James et al. 2004), rather than one where peripheral individuals have infinite domains of danger, as it is thought to more closely resemble predation risk in the wild (James et al. 2004; Morrell & James 2008). Only isolated individuals (those at least $2r$ from any others) have an LDOD area of $A_{max}$. For other individuals, the circular LDOD is reduced by any bisector generated by an agent within a distance of $2r$, giving an LDOD area $A$. In each simulation, each agent is allocated a movement rule from those defined below.

We consider three different movement rules (a subset of previously proposed rules and those considered in Morrell & James (2008)). In line with Hamilton’s (1971) original ideas, and to allow for comparison with other published studies (Morton et al. 1994; Viscido et al. 2002; James et al. 2004; Morrell & James 2008), we do not explicitly model predator behaviour: agents do not receive any directional information regarding the predator’s approach direction. Such directional information has been shown to result in a movement decision that comprises both
movement away from the predator, and movement towards other individuals within
the group (Viscido et al 2001). Here, we focus our attention on the more
controversial aspect of movement towards other individuals, rather than simply
away from the predator. In addition the habitat is assumed to be homogenous, with
no areas of cover that could potentially be used by the prey for protection.

The rules we consider are:

1) **Nearest Neighbour (NN):** Each agent moves directly towards its closest
   neighbour (Hamilton 1971). NN is the simplest rule we consider.

2) **Multiple Nearest Neighbour (nNN):** Individuals move towards the average
   location of several ($n$) nearest neighbours (Morton et al. 1994). For simplicity,
   we consider only $n=3$ here.

3) **Local Crowded Horizon (LCH):** Each individual moves towards the area with
   the densest concentration of conspecifics, depending on their positions
   relative to the focal individual. Individuals calculate the distance to their (up
to) 20 closest neighbours, and close neighbours have a strong influence on
   movement direction, while distant group-mates exert a much weaker
   influence. We use the perception function suggested by Viscido et al. (2002)
as being biologically plausible: \[ f(x) \] , where $x$ is the distance from the
   focal individual and $k=0.375$ (Viscido et al. 2002). The influence of each
   neighbour is weighted by $f(x)$.

In our simulations, $N_{NN}$ agents used the NN rule, $N_{3NN}$ agents used the 3NN rule, and
$N_{LCH}$ agents used the LCH rule ($N_{NN} + N_{3NN} + N_{LCH} = N$).
In each timestep $t$, until a maximum $t_{\text{max}}$ (here, $t_{\text{max}} = 10$ seconds), each agent identifies its target location, based on the movement rule it is following, and then moves at a speed of 0.15 m/s towards that target location (the approximate swimming speed of a three-spined stickleback; James et al. 2004; Morrell & James 2008). Each timestep in our simulations lasts 0.1 seconds. The start of the simulation ($t = 0$) represents the point at which the agents begin moving. All individuals move simultaneously, as is likely to occur in nature, rather than sequentially, and thus each agent updates its target location and direction in every timestep. Bode et al (in press) demonstrate that under higher predation threat, synchronous behaviour becomes increasingly probable. LDOD areas are calculated after every timestep and for every individual. We ran 1000 simulations for each set of parameter values. All simulations were run in C, and resulting data were analysed using Matlab® R2007b (Mathworks 2007).

At each timestep, we calculated the total LDOD area (the sum of $A$ for all individuals, $A_{\text{tot}}$). We then calculated the proportion of $A_{\text{tot}}$ occupied by each individual, to give a measure of the way predation risk is distributed among individuals. For each timestep, we then calculated the mean proportion of $A_{\text{tot}}$ for all individuals using each strategy. Finally, we calculated the mean and standard error of these values across 1000 replicate simulations. This method allows us to compare the relative success of strategies in reducing individual risk: if the mean proportion of $A_{\text{tot}}$ occupied by individuals using one strategy is less than the mean proportion of $A_{\text{tot}}$...
occupied by individuals using an alternative strategy, then the first strategy is more successful at reducing individual risk.

Results

Proportion of risk: Mixed-strategy population

Figure 1 shows how the proportion of the total LDOD area ($A_{tot}$) occupied by individuals using each strategy changes over the course of 10 seconds of movement, when each strategy is equally represented in the population ($N_{NN} = N_{3NN} = N_{LCH} = 7$). Figure 1 indicates that the relative success of the different movement rules is dependent on the time elapsed since the start of prey movements towards each other. This can be thought of as the time at which the predator closes on and makes its attack on the moving prey group. Time $t = 0$, when the prey start moving, can be thought of the time when the prey first detect the presence of the predator and/or cues of imminent attack. At very rapid predator attack times (< 1 second after detection), NN and 3NN individuals do equally well, and are more successful than LCH individuals in the population (figure 1). If predators attack more slowly (after between 1 and 5 seconds of movement), 3NN individuals do considerably better than individuals using other rules. After 5 seconds of movement, LCH individuals are most successful. Thus, if we considered only what happened when the population reached equilibrium (i.e. when movement ceases), we could conclude that the LCH strategy was the most successful, yet the 3NN strategy performs better for a considerable proportion of the movement time. Thus selection pressure on movement rules depends on the characteristic interval that prey have for
aggregative movements between them first detecting the predator and the predator being in a position to capture an individual.

 Mutant invasions

We next consider the ability of ‘mutant’ rules to begin to invade a population using a different movement rule. In each set of simulations, 19 individuals use the ‘population strategy’, and one individual uses an alternative strategy. We investigate all 6 potential mutant-population combinations. Figure 2 illustrates the ability of the mutant rules to invade each population type, showing the mean proportion of the total LDOD area \( A_{tot} \) occupied by the mutant and population members.

The ability of a mutant using one strategy to invade a population using an alternative strategy is highly dependent on the time at which the invasion is considered. A NN population (figure 2b & d) is stable against invasion by both the 3NN (2b) and LCH (2d) mutant for the first approximately 1.5 seconds of movement. After this time, the 3NN mutant can successfully invade, but the population is stable against invasion by the LCH mutant for intervals less than approximately 4 seconds. A 3NN population (figure 2a & f) is always stable against invasion by NN mutants (2a) and against LCH mutants for intervals less than approximately 7 seconds (2f). If the predator attacks with a longer interval than this, the LCH mutant can invade the population. Finally, in a population of LCH individuals (figure 2c & e), both NN and 3NN mutants can invade if predators attack rapidly (< 1 second for NN, < 2 seconds for 3NN), but if the predator attacks after more than 2 seconds of movement has taken place, a LCH population will be stable against invasion.
Invasion dynamics

We now consider what happens as the number of mutants in a population increases (either through individuals using different strategies entering the group, individuals switching strategy, or through reproduction where parental strategies are passed on to offspring). We initially consider a single mutant individual using one strategy invading a population using an alternative strategy (thus considering the strategies in a pair-wise game), then increase the number of mutants (5 and 10 mutant individuals in a total population of 20). As before, we calculate the mean proportion of the total LDOD area occupied by individuals using each strategy. We then calculate the difference in these values as (mutant mean – population mean), giving a positive value where the population is stable against invasion, and a negative value where the mutant is able to invade. This is shown in figure 3, where each panel represents a different mutant-versus-population comparison, with three different mutant frequencies.

At the start of each predator attack, there are initial intervals of a few tenths of a second where invasion is possible in all populations (t<0.3). These occur when the individuals have only just begun movement, and are close to being randomly positioned in the arena. There is a possibility, then, that a mutant using any strategy could invade a population using any alternative strategy, if predators attack in the first moments after detection by the prey (for example, an ambush predator).

We now consider whether populations are stable against invasion after potentially adaptive movement has taken place. If we consider pairs of populations in turn, we
can investigate whether a population using strategy ‘A’ is stable against a mutant using strategy ‘B’ and vice versa. A single NN mutant can invade a 3NN population (figure 3a, squares) only in the first moments of movement, and thus 3NN is stable against NN. NN populations are stable against 3NN (figure 3b) only if the predator attacks within the first two seconds, otherwise, the 3NN mutant can invade. When NN plays LCH (figure 3c), the LCH population is stable after 1.5 seconds of movement, while a NN population is stable against invasion by a single mutant for intervals less than 4.5 seconds (figure 3d). In the final combination, 3NN can invade LCH for around 2.5 seconds after movement begins (figure 3e), while being stable against a LCH mutant unless the interval is greater than approximately 7.5 seconds (figure 3f).

If a mutant can invade a population, then that mutant can increase in frequency in the population, and there is the potential for the mutant strategy to become the dominant strategy in the population or for a combination of strategies to co-exist. Figures 3a-f also show the invasion success of mutants as their numbers increase to 5 (circles) and then 10 (triangles). Our results show that once a mutant strategy has gained a foothold in the population, the range of intervals over which that strategy is more successful than the original population strategy increases (the areas where the difference between the means is negative increases). We consider first the case where predator attack times are fixed (i.e. the predator always attacks at a certain point in time), and discuss how each pair-wise combination of strategies is likely to evolve:
**NN and 3NN:** For the majority of predator attack times, a 3NN population is stable against invasion by NN, and a 3NN mutant can invade a NN population. However, if predators attack rapidly, invasion by a NN mutant is possible, and a NN population is stable (Figure 3a and b). If NN initially invades, then it can increase in numbers until the population consists of 10 NN and 10 3NN individuals (figure 3a). For slower (later) predator attack times (larger values of $t$), the opposite is true: 3NN mutants can increase in number, and persist at increasingly rapid attack times (figure 3b).

**NN and LCH:** A single NN individual can invade a LCH population at rapid predator attack times and remains more successful at these times as its numbers increase (figure 3c). A single LCH individual can successfully invade a NN population after 4.5 seconds (figure 3d), and remains more successful at later attack times as numbers increase. When the group is equally divided between the two strategies, there is a very small period of time (at around 2 seconds) where success of the two strategies is similar (the point at which the triangles on figures 3c and 3d cross the ‘zero’ line). For intervals of this length, it is possible that a mixed group of individuals might persist, unless random drift allows the numbers of one or the other to increase to fixation. Otherwise, the population is likely to fix at NN (if attack times are rapid) or LCH (if attack times are slower).

**3NN and LCH:** A similar pattern is seen for the remaining strategy combination: 3NN can increase in numbers if predators attack rapidly (figure 3e), while LCH can increase if predators attack later (figure 3f). When the group consists of half 3NN and half LCH, there is again a small period of time where strategies could co-exist, but
generally, we would expect the population to evolve to either 3NN (if attacks are rapid) or LCH (if attacks are slow).

Discussion

Our results suggest that the consideration of the timing of predator attacks (relative to the movement speed of the prey) is critically important in understanding the anti-predator responses of prey. The timing parameter studied in our model is the delay between prey first being aware of impending attack and an individual actually being struck by the predator. This will be influenced both by the nature of the predator and by the environment. For predators that attack from protective cover, the greater the distance between such cover and the prey group the greater the attack time. Thus we would expect this attack time to be longer in open environments (like Steppe grasslands, tundra, savannah, lakes and seas) than more complex environments where prey can less easily avoid potential hiding places of their predators (like scrubland, forest, or narrow rivers and streams). While we found that complex strategies are generally favoured over longer attack times, no defence is effective at very short attack times (against ambush predators). This is because there is insufficient time between predator detection and attack for a significant amount of adaptive movement to take place, and individuals remain close to their random starting positions. The benefits of potentially adaptive movement are only seen later in the movement sequence. Complex strategies are not immediately favoured, particularly in low density groups (see electronic supplementary material), due to the fact that individuals using these rules can be left moving ‘alone’ with no reduction in LDOD area, for a longer time period, as their strategy does not take
them directly towards another individual (thereby rapidly reducing LDOD area). With
the exception of the initial moments of the movement sequence, we found no
evidence that multiple strategies might coexist in a population at any given attack
time, suggesting that variation in predator attack timing would be necessary to allow
for multiple strategies to coexist.

Our results also suggest that there may be positive frequency dependence to rule
success. A strategy can invade across a wider range of attack times if it starts at a
higher frequency. Thus, both simple and complex rules are favoured when they are
already abundant in the population. A population consisting predominantly of one
strategy is much more stable against invasion than one consisting of a mixture of
strategies. This suggests that each strategy is most successful when in a group
containing others playing the same strategy, and may work against polymorphism at
any fixed attack time, again suggesting that a mixture of attack times is needed to
select for mixed responses in prey.

Overall, if predator attack times are fixed, then there are very few opportunities for a
mixture of different strategies to persist in the population. A second, and perhaps
more likely, possibility is that predator attack times are not fixed, but that predators
may attack a group across a range of times. Together, our results point to the
following hypothesis: If predators are fixed in their attack strategy (i.e. they always
attack at the same point in time) we predict that prey populations should evolve
towards a single, evolutionarily stable movement rule. However, if predator attacks
are unpredictable in time, either because different individual predators have
different, fixed, attack times, different species of predators differ in their hunting methods and therefore attack timing, or other factors (such as distance from cover) cause variation in attack timing, then we predict mixed responses in prey. Some prey individuals may use simple rules, and others more complex rules (a polymorphism), or individuals may respond using alternative rules (a mixed solution), perhaps dependent upon other factors, such as the immediate size and density of the group, or their own individual perceived risk. For example, individuals may use their distance to neighbours to choose which rule to use; using one rule when close to a neighbour, and a different rule if isolated. In a group consisting of individuals using NN and LCH, for example, the individuals using LCH would be safer on those occasions where predators attack slowly, while those using NN would be safer on those occasions where predators attack more rapidly, thus, prey could select their strategy based on the distance between the predator and the group. The overall success of the two strategies and the dynamics of the population evolution would be dependent on the distribution of predator attack times.

Many species are preyed upon by a variety of predators differing in their attack behaviour, and where multiple predators are present, prey are likely to evolve a range of risk-sensitive responses (Lima & Bednekoff 1999; Relyea 2003). Vervet monkeys (Cercopithecus aethiops), under threat from leopards, martial eagles and pythons, show predator-specific alarm calls and anti-predator responses (Struhsaker 1967; Seyfarth et al. 1980). In fish, guppies (Poecilia reticulata) fall prey to a variety of other organisms, and respond in a risk-sensitive manner (Botham et al. 2008).

Thus, we may expect different movement rules to evolve in response to different
predators. Individuals of the same predatory species may also differ consistently in their attack strategies (Sih et al. 2004). While some variation in attack times can be attributed to predator species or strategy, variation in attack timing is also likely to result from random factors, such as the distance from the prey group at which the predator is first detected. Testing this hypothesis is a fascinating route for future study.

Previous studies have shown that individuals using simpler strategies (such as NN) can achieve protection through encounter-dilution effects (Morrell & James 2008), and here we show that these individuals can also benefit at the expense of others in the group (i.e. through the selfish herd effect), given the right ecological conditions. Using an evolutionary genetic algorithm Reluga & Viscido (2005) demonstrated that complex averaging rules could evolve from simpler ones, but considered only equilibrium DOD areas once the aggregation had formed, and not attacks that occur while the aggregation is in the process of forming. Empirical evidence for the use of different movement rules is limited (Morrell & James 2008), although in three-spine sticklebacks, individuals appear to prefer neighbours that can be reached more quickly over those that are spatially closer (Krause & Tegeder 1994).

In line with previous explorations of the selfish herd, we assume here that predators appear at random and attack the closest individual, so that risk is related entirely to LDOD area. In reality, predators may target specific individuals within a group, or certain positions within the group may be more risky than others. Peripheral individuals should theoretically be more at risk than those in the centre of a group.
(Hamilton 1971; Vine 1971), something that has received support across taxa
(Stankowich 2003; Morrell & Romey 2008; but see Parrish 1989). An individual’s
position within a group may therefore affect the best way for it to respond to a
 predator attack, and thus movement rules may also be state-dependent (Rands et al.
2004), perhaps related to each individual’s perception of its position within the
group or level of risk (LDOD area). Vigilance and the detection of predators by prey
may also affect optimum movement decisions. If predators delay target selection
until after some individuals have detected and responded to the predator (Bednekoff
& Lima 1998), any delay in responding may also influence optimal movement rules.
Here we have shown the importance of closing speed of the predator relative to the
movement speed of prey on selection on anti-predator grouping behaviours.
Interestingly, Wood (2010) demonstrates a similar strong influence of predator
speed on the final shape of aggregations predicted by plausible prey movement
rules.

We also assume that all individuals begin moving at the same point in time, and at
the same speed, when in many animal groups there is variation in both ‘starting
time’ and movement speed. We suggest that the optimal movement rule for any
given individual should depend on its escape speed. A fast-moving individual may
benefit by using a simple rule, particularly if predators attack quickly. Presumably, a
fast-NN animal could easily invade a population using slow-NN, leading to the
evolution of faster escape responses. The speed of decision-making may also be
important: complex movement rules have been criticised (Morton et al. 1994;
Viscido et al. 2002) on the basis that they may be cognitively too demanding for
animals to follow. Incorporating a ‘thinking time’ into each movement step could account for the complexity of the calculations.

Our findings have implications for our understanding of predator-prey dynamics, as the timing of a predator attack relative to the detection of the predator by the prey, and the prey response, is critical in determining the optimal escape decision of the prey. Early and late attacking predators may exert different selection pressures on prey, resulting in a mixture of escape strategies within a single prey population. The movement rules used to escape from predators could also influence positioning outside attack periods, allowing individuals to choose a position in a group which allows for successful reduction of risk when attacks occur. Clearly, the ability of prey to respond appropriately to predators will be critical for their fitness, but equally, predators that behave unpredictably (by attacking at different times) may ensure that a single optimal prey response cannot evolve, and leave a mixture of different escape strategies within a population. We have adopted a modelling framework in this study that allows effective comparison with previous relevant studies. However, it should be acknowledged that this represents a highly idealised description of any natural system. As the body of theory on the selfish herd becomes more and more substantial, the need to explore how well the predictions of idealised models transfer to system-specific, more-realistic case studies grows also. In our modelling framework we do not consider predator success and thus cannot evaluate selection pressures on the predator, thus, the longer-term evolutionary consequences of the aggregative tactics explored here are also worthy of exploration within a co-evolutionary modelling framework.
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References


Figure legends

Figure 1: Proportion of risk: Mean (± 2 SE) proportion of total LDOD area occupied by individuals using NN (squares), 3NN (triangles) and LCH (circles), when all strategies are equally represented in the population. Parameter values: \( N_{NN} = N_{3NN} = N_{LCH} = 7, d = 4 \)

Figure 2: Mean (± 2 SE) proportion of total LDOD area occupied by the mutant (open shapes) and an average population member (filled shapes), for each possible combination of mutant (open circles) and population strategy (filled squares). a) A NN mutant in a population of 3NN (‘NN v 3 NN’); b) 3NN v NN; c) NN v LCH; d) LCH v NN; e) 3NN v LCH; f) LCH v 3NN. Other parameter values: \( N = 20, N_m = 1, d = 4 \)

Figure 3: Invasion dynamics: Invasion success as mutant numbers increase, measured as the difference in the mean proportion of total LDOD area occupied by mutants and population members. The horizontal line at zero indicates equal success (measured as proportion of total LDOD area); positive values indicate that the population is stable against invasion by the mutant, and negative values that the mutant can invade the population. Squares: \( N_{mut} = 1 \), circles \( N_{mut} = 5 \) and triangles: \( N_{mut} = 10 \). a) NN v 3NN b) 3NN v NN, c) NN v LCH, d) LCH v NN, e) 3NN v LCH and f) LCH v 3NN. Error bars represent 1 standard deviation. Parameter values: \( N = 20, d = 4 \)
Figure 1
Figure 2
Figure 3

Graph a: Difference in mean proportion of total LC3D-II area, \( A_{\text{m}} \), occupied by mutants and population members.

Graph b: Similar to Graph a, but with a different scale.

Graph c: Difference in mean proportion of total LC3D-II area, \( A_{\text{m}} \), with a different scale.

Graph d: Similar to Graph c, with a different scale.

Graph e: Difference in mean proportion of total LC3D-II area, \( A_{\text{m}} \), with a different scale.

Graph f: Similar to Graph e, with a different scale.

Time (seconds)
Using identical methodology to that in the main paper, we also consider the effect of altering population size and density. In each of the panels in figure S1, we alter one population parameter relative to figure 1. As density decreases (to $d = 2$, figure S1a), the simpler strategies remain the most successful at rapid predator attack times. As population density increases ($d = 10$, figure S1b; qualitatively equivalent to increasing the radius of the LDOD, or the distance from which predators can successfully attack), LCH becomes much more successful over a wider time range. Only at very short attack times can the 3NN individuals outperform the LCH individuals. If we decrease population size while maintaining density at $d = 4$ (fig S1c; population size has been shown previously to have an effect on rule success independent of density; Morrell & James 2008), NN performs badly at all attack times, while LCH and 3NN have similar success at rapid attack times, but LCH outcompetes 3NN at longer attack times. If we increase population size (fig S1d) simpler rules have increased success over more complex rules over a longer period at the start of simulations.

Thus, at lower population densities, and in larger populations, simpler rules are able to invade populations using more complex rules (and are stable against invasion) over a greater range of predator attack times. When groups are already compact (higher population densities), more complex rules are needed for a mutant individual to benefit at the expense of a population using simpler rules, but again, the timing of the predator attack is critically important in determining the invasion success of alternative strategies.
Figure S1: Population parameters: The effect of altering population size and density on the relative success of different strategies (NN - squares, 3NN - triangles and LCH - circles). Panels show: a) Low density population: $N_{NN} = N_{3NN} = N_{LCH} = 7$, $d=2$, b) High density: $N_{NN} = N_{3NN} = N_{LCH} = 7$, $d=10$, c) Small population: $N_{NN} = N_{3NN} = N_{LCH} = 4$, $d=4$ and d) Large population: $N_{NN} = N_{3NN} = N_{LCH} = 15$, $d=4$. 